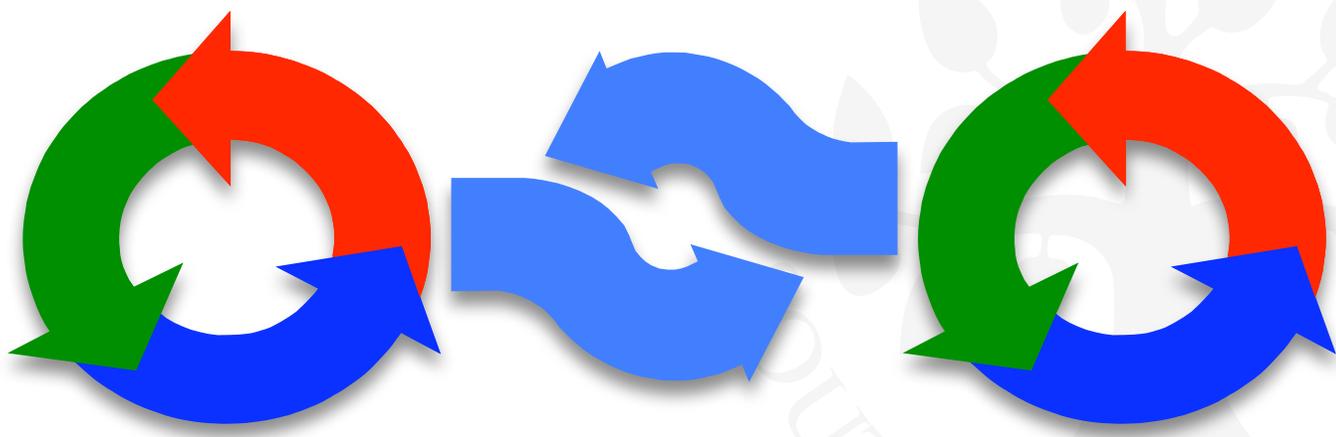
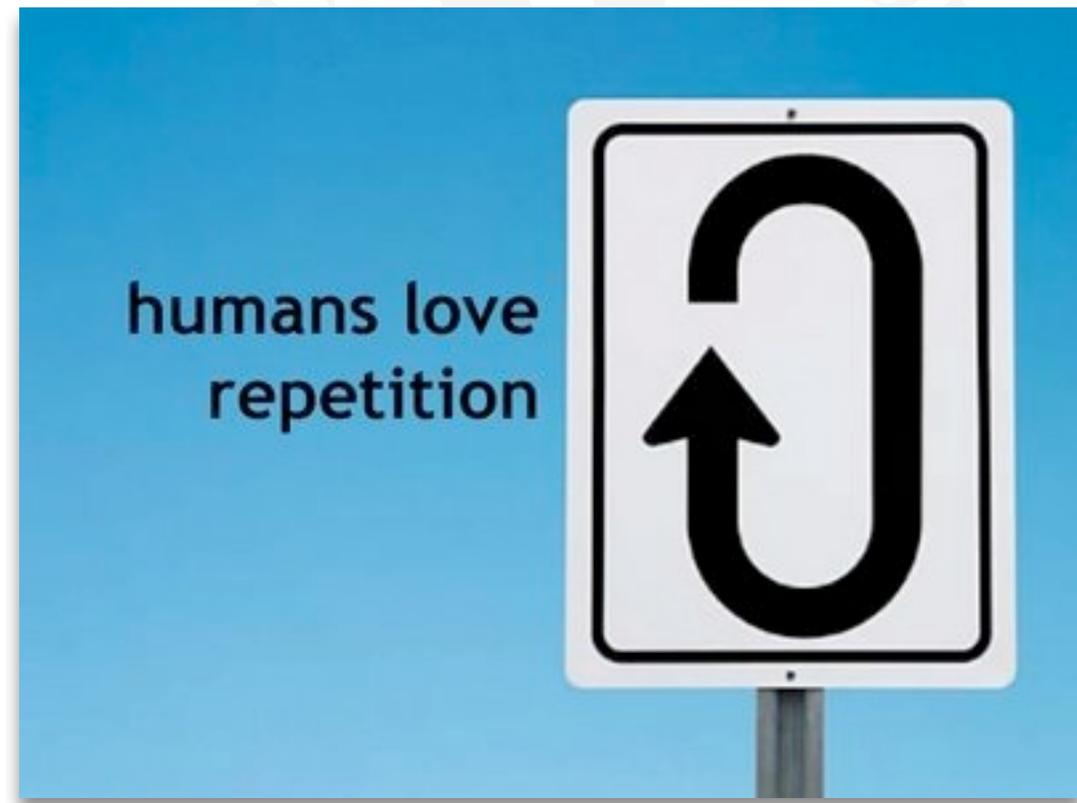


# Deadlock



## But First: Repetition

# Monitors and Condition Synchronisation



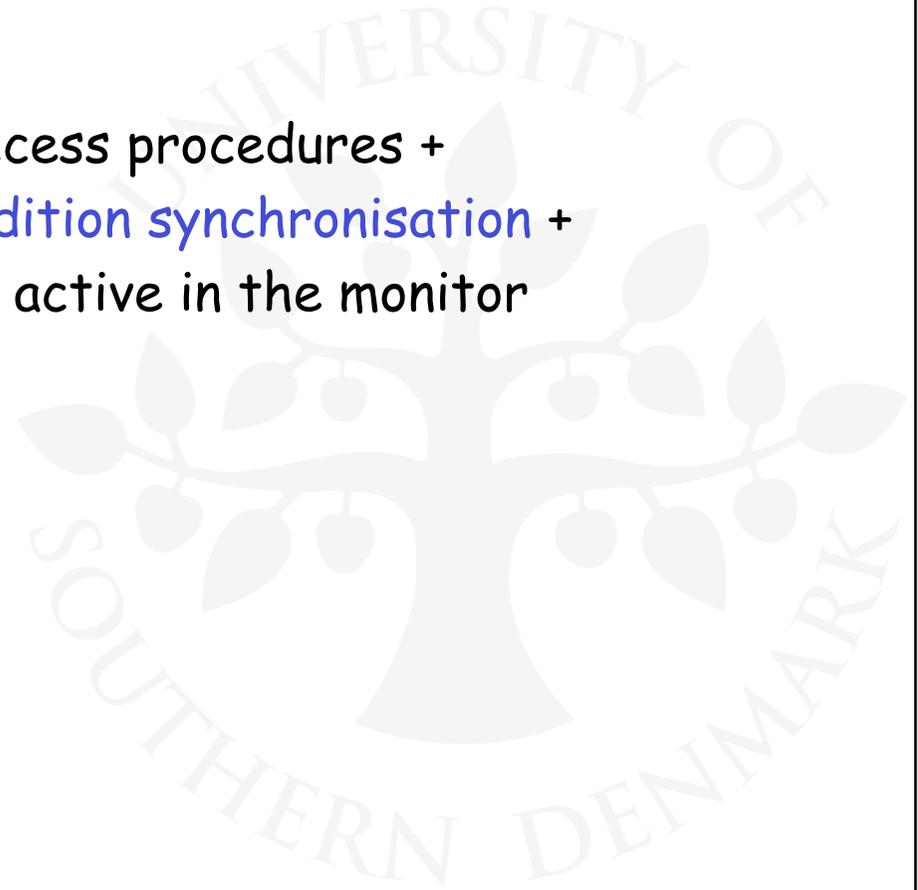
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encapsulated data + access procedures +  
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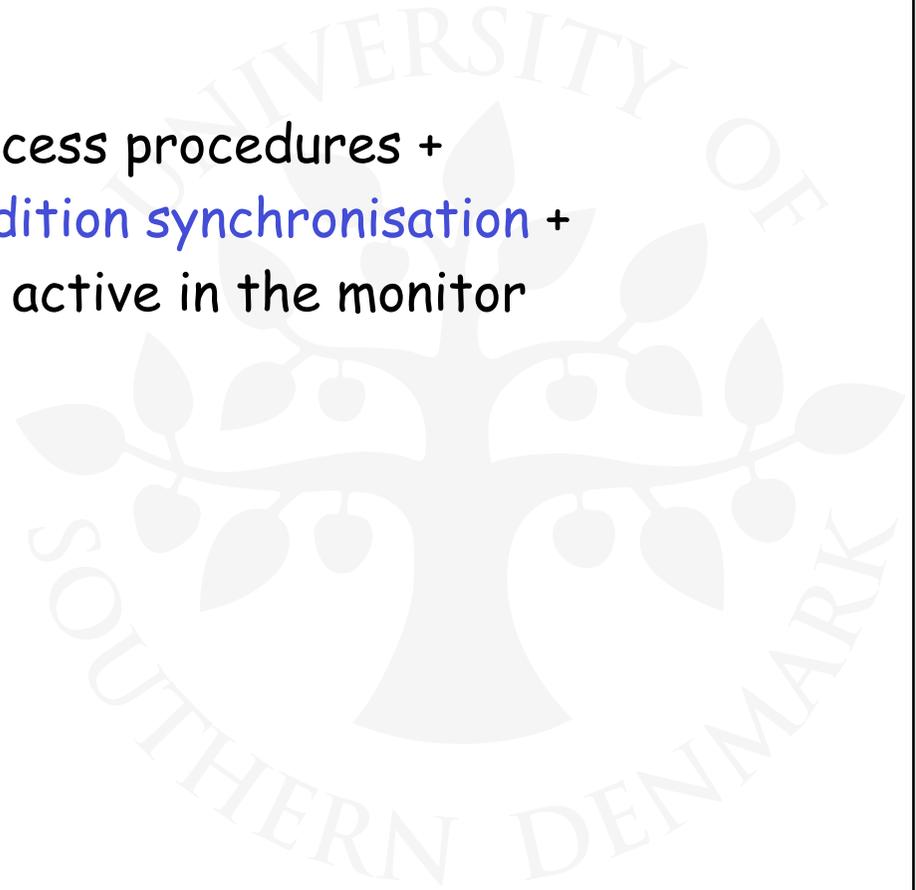


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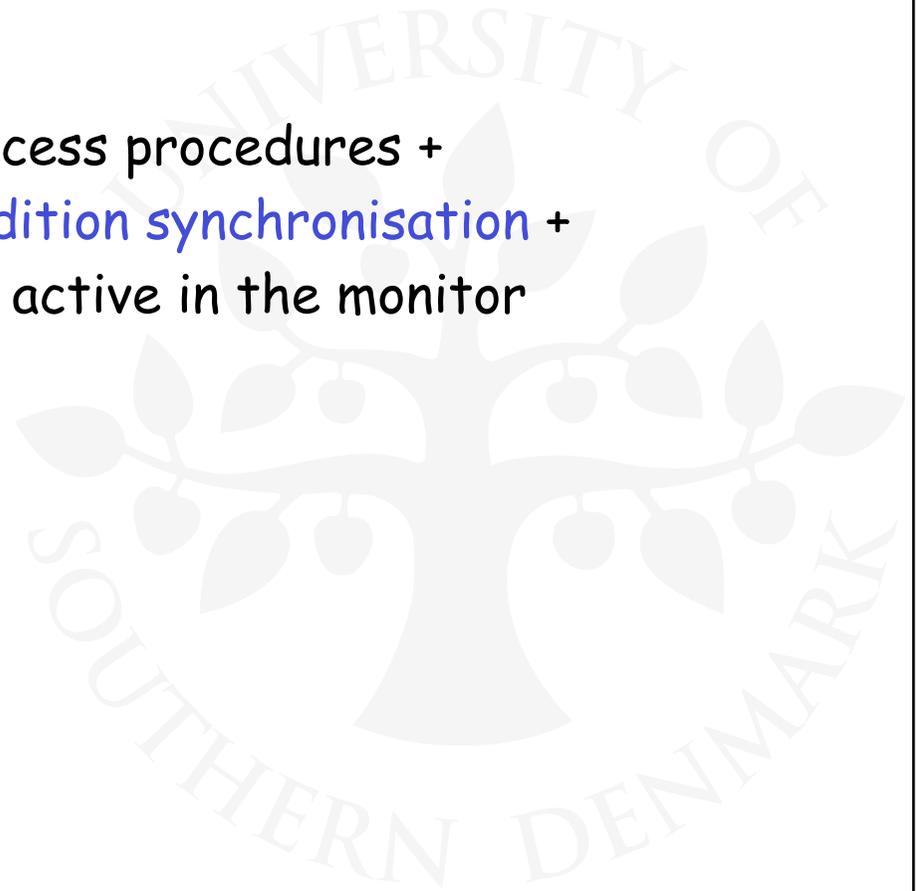
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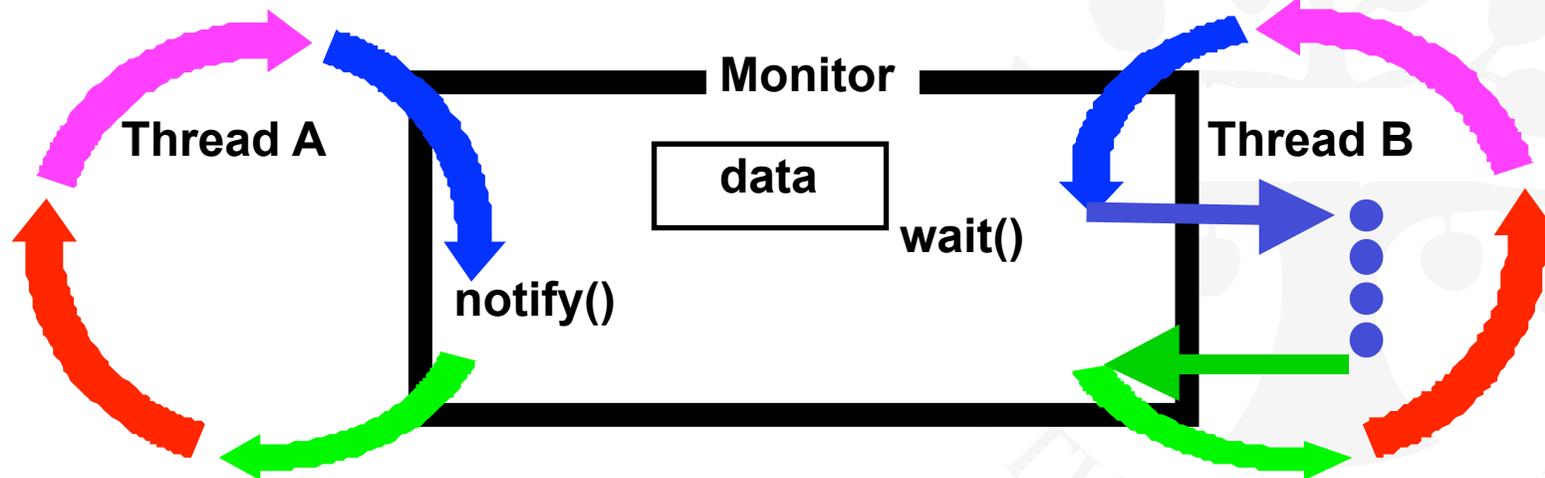
nested monitors

Models: guarded actions

Practice: private data and synchronized methods (exclusion).  
`wait()`, `notify()` and `notifyAll()` for condition synchronisation.  
single thread active in the monitor at a time

# Wait (), Notify (), And NotifyAll ()

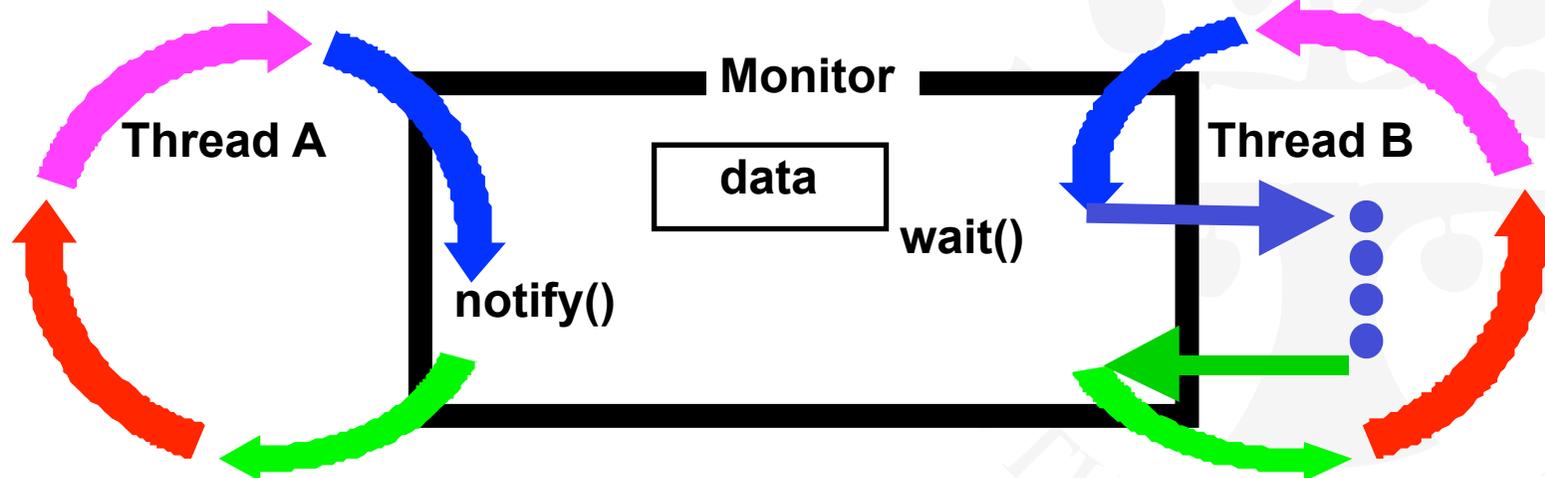
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public final void wait() throws InterruptedException;
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# Wait(), Notify(), And NotifyAll()

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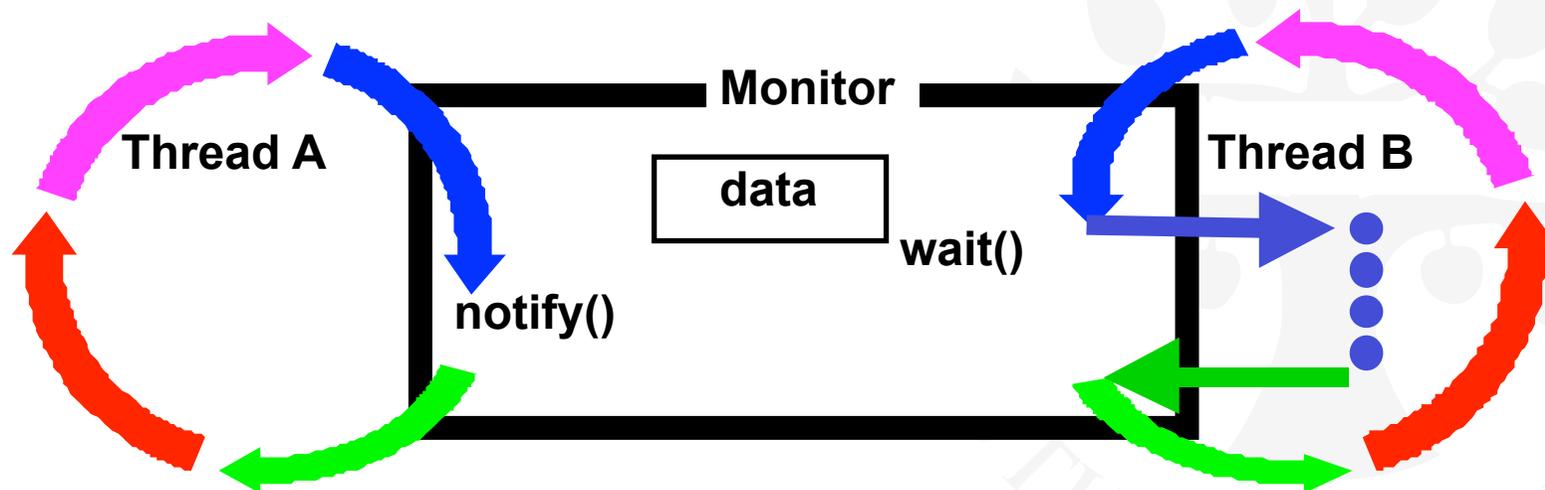




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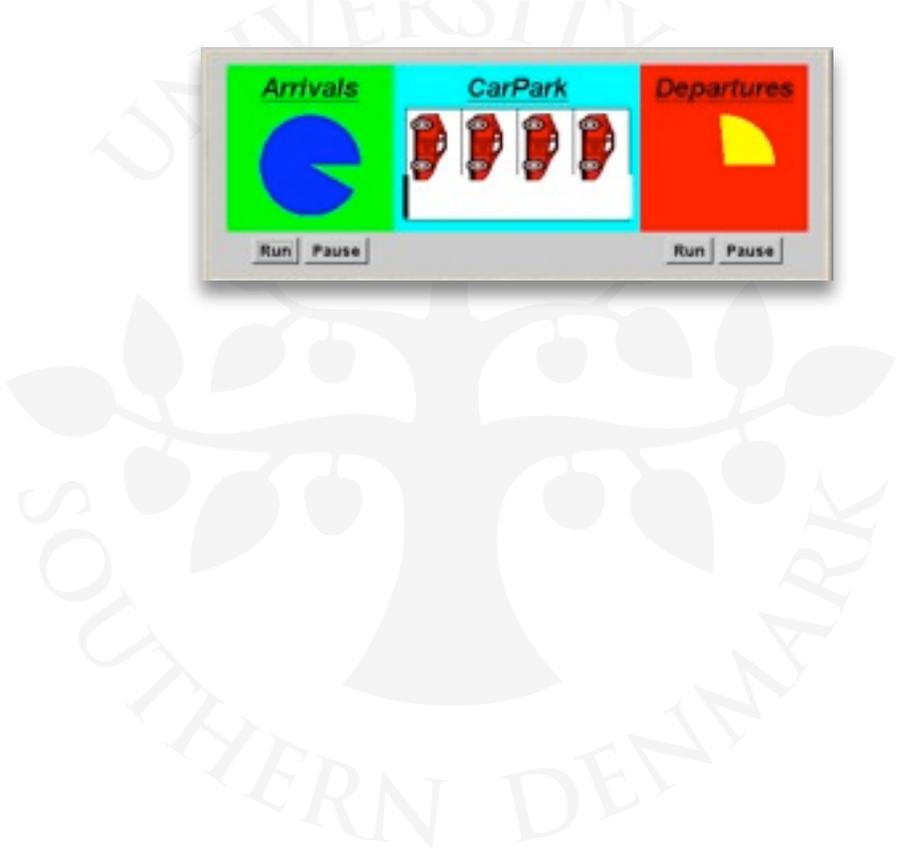
```
public final void notify();
```

```
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# Condition Synchronisation (in Java)



```
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```



*notify() instead of notifyAll() ?*

1. Uniform waiters - everybody waits on the same condition
2. One-in, one-out

*What goes wrong with notify and 8xDepartures, 5xArrivals?*



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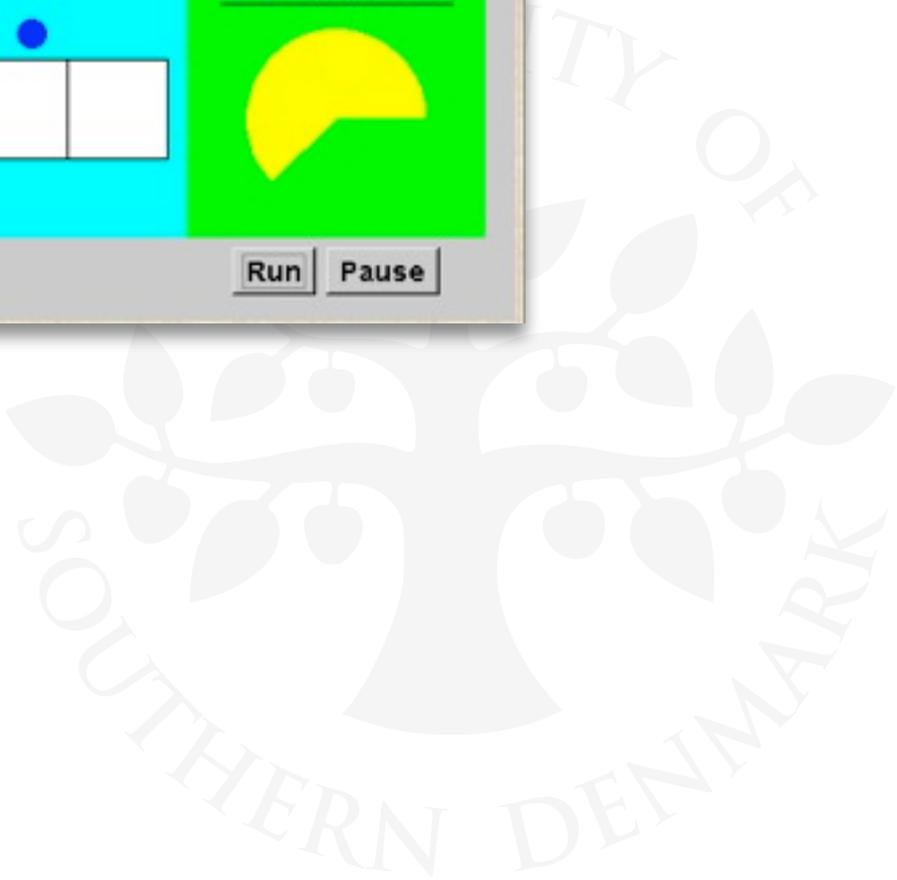
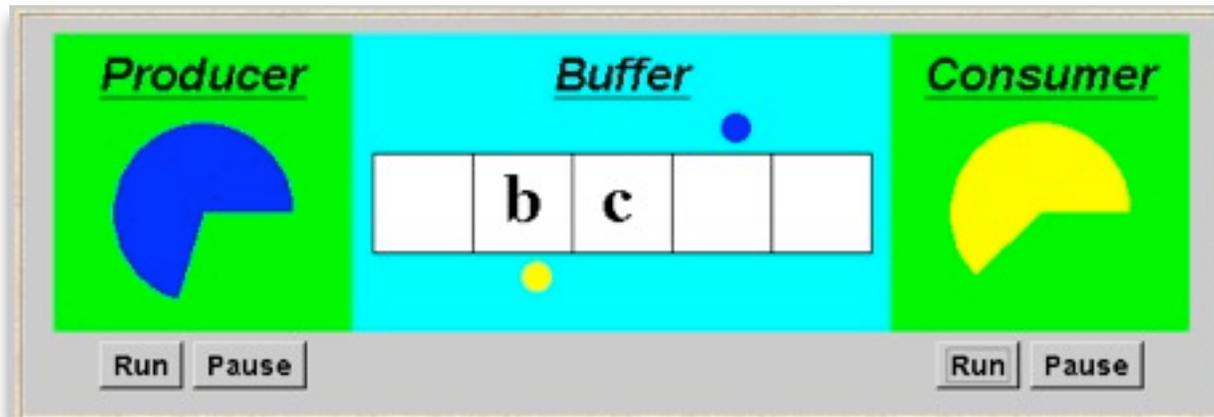
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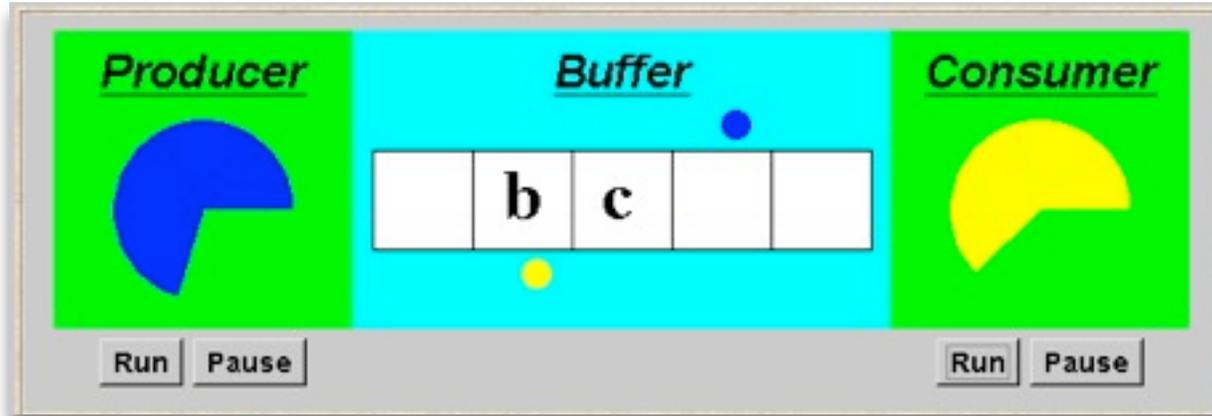
```
sem.down(); // decrement (block if counter = 0)
```

```
sem.up(); // increment counter (allowing one blocked thread to pass)
```

# Nested Monitors - Bounded Buffer Model



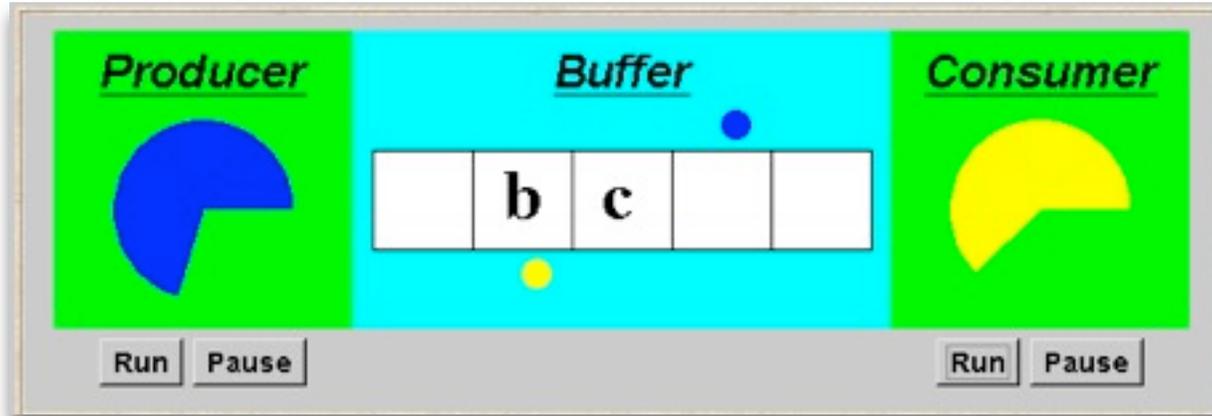
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LTSA's (analyse safety) predicts a possible **DEADLOCK**:

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States Composed: 28 Transitions: 32 in 60ms
Trace to DEADLOCK:
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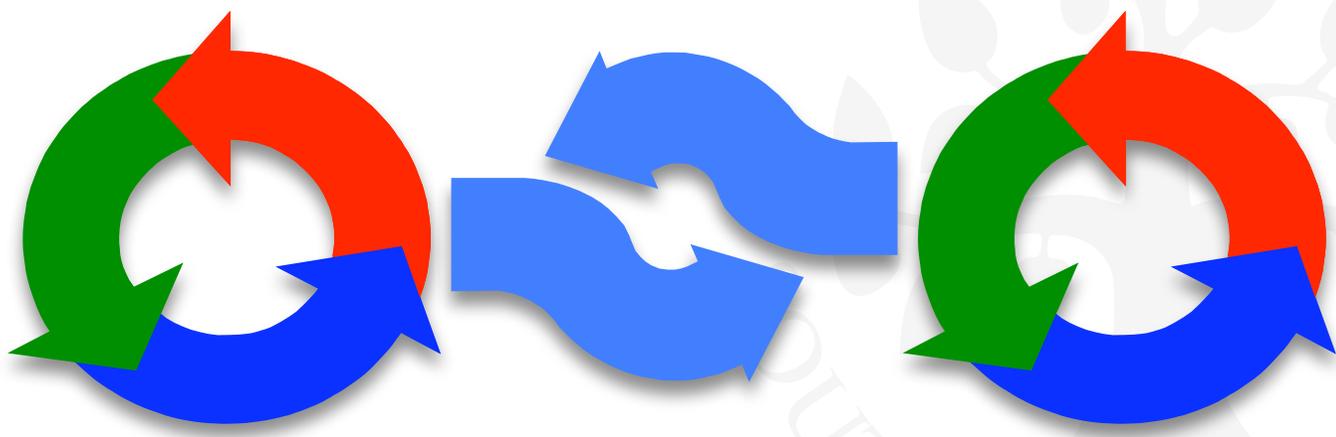


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This situation is known as the **nested monitor problem**.

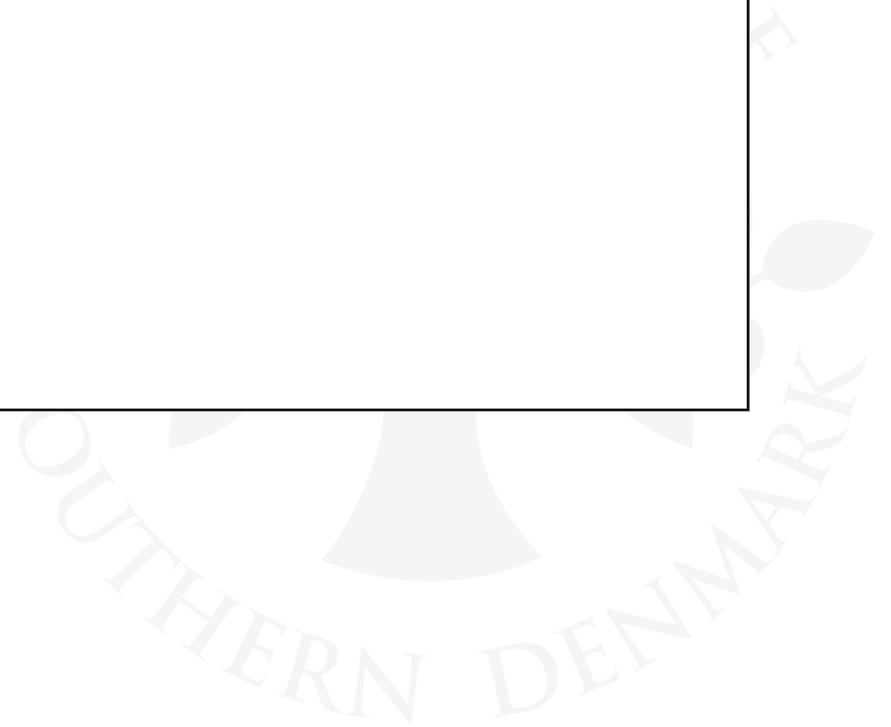
# Deadlock



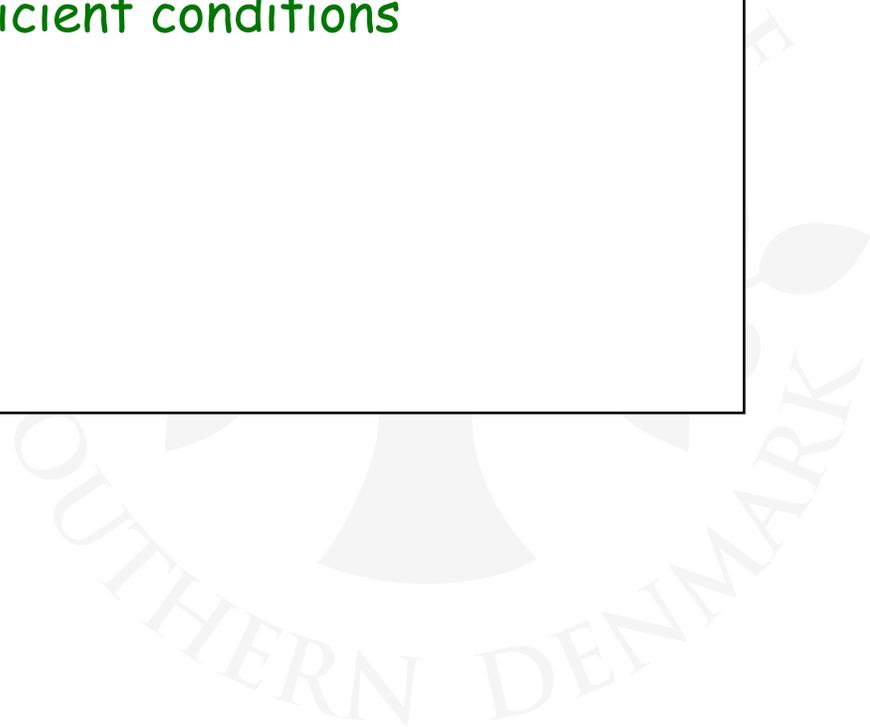
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**Aim:** deadlock avoidance - to design systems where deadlock cannot occur.

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**Necessary condition:**

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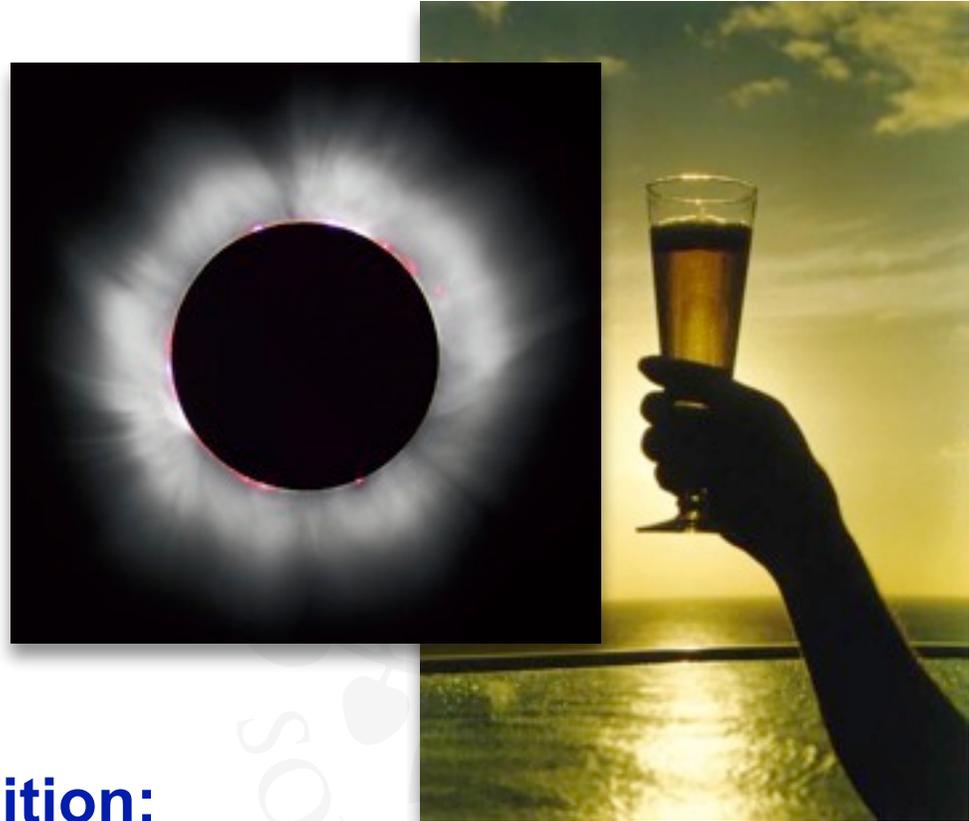
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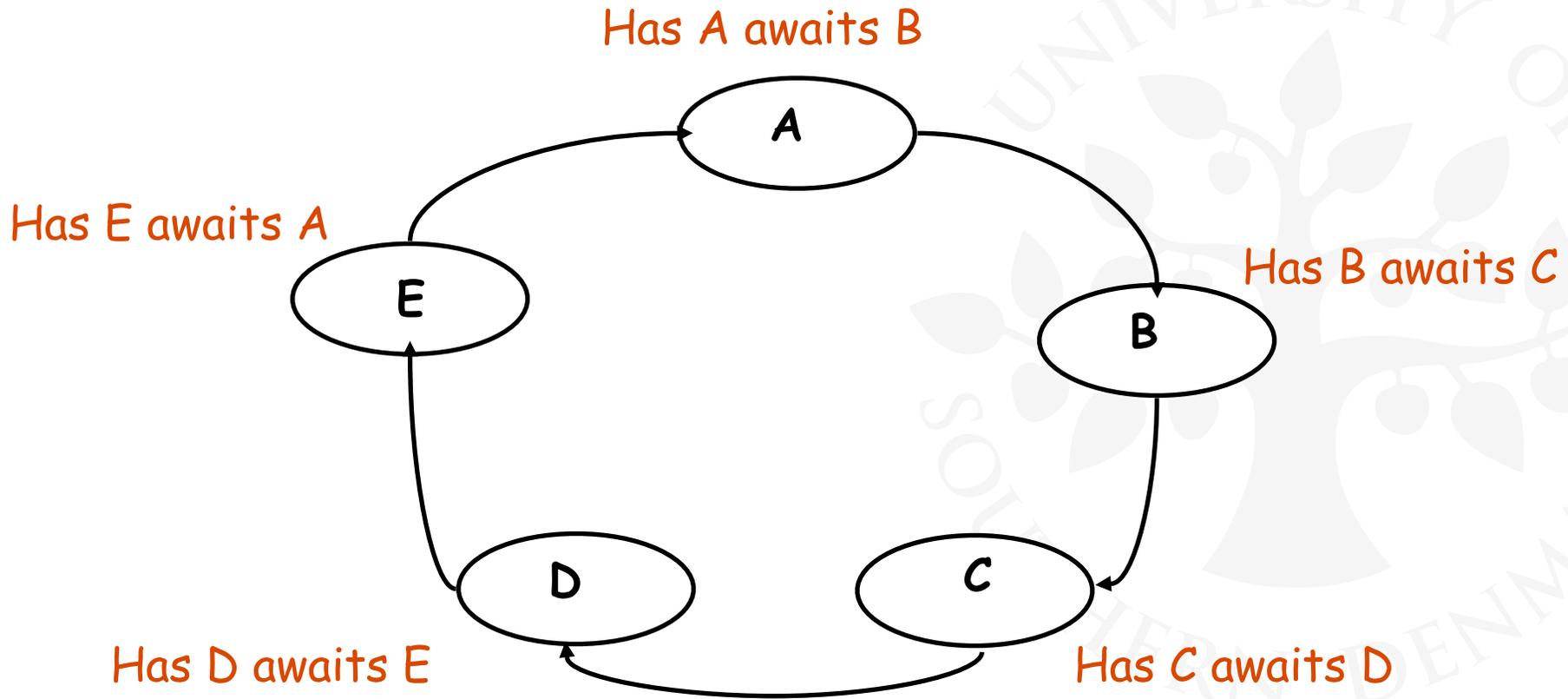
# Wait-For Cycle

A





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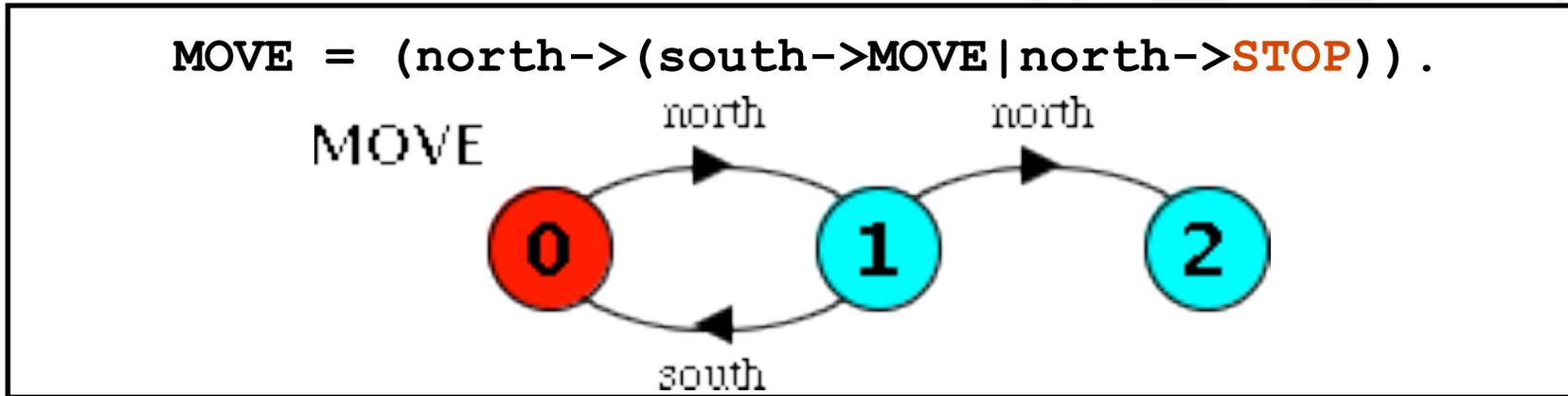
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```
MOVE = (north->(south->MOVE | north->STOP)) .
```

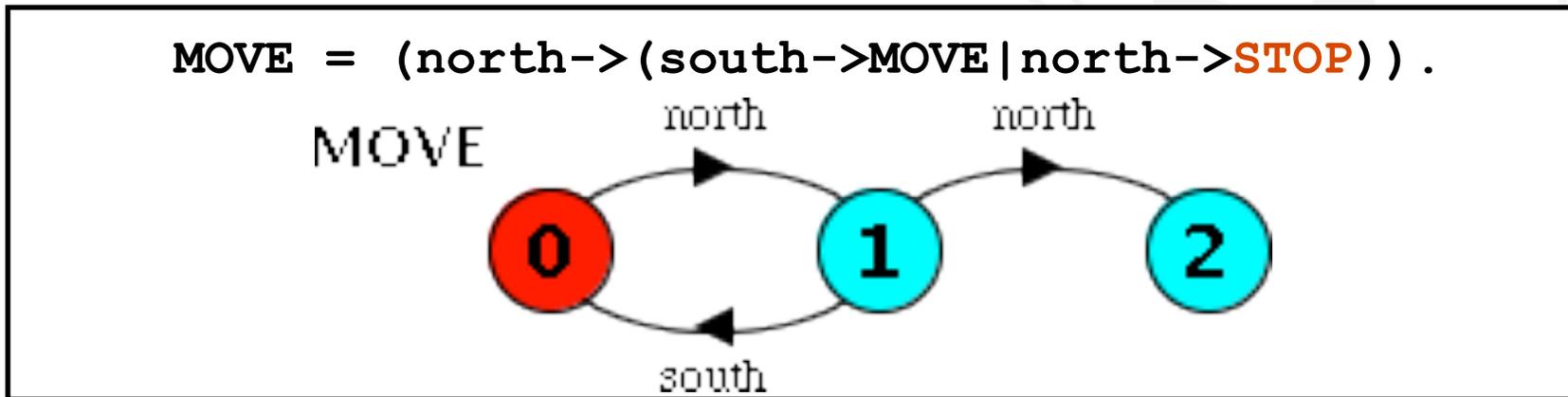
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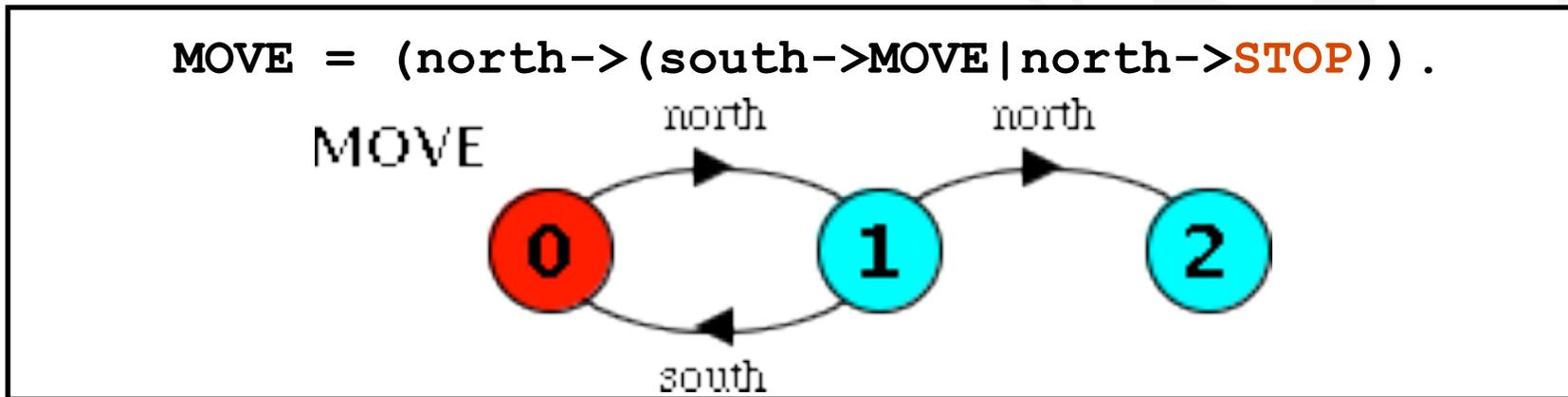
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- ◆ Analysis using **LTSA**:

Shortest path to DEADLOCK:

Trace to **DEADLOCK**:  
north  
north

# Deadlock Analysis - Parallel Composition

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$  \begin{aligned}  P &= (x \rightarrow y \rightarrow P) . \\  Q &= (y \rightarrow x \rightarrow Q) . \\    D &= (P    Q) .  \end{aligned}  $
---



# Deadlock Analysis - Parallel Composition

- ◆ In practice, deadlock arises from **parallel composition** of interacting processes.

```
P = (x -> y -> P) .  
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|| D = (P || Q) .
```

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RESOURCE = (get-> put-> RESOURCE) .
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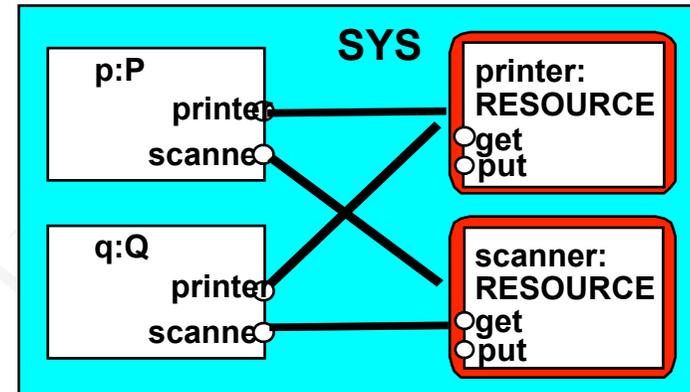
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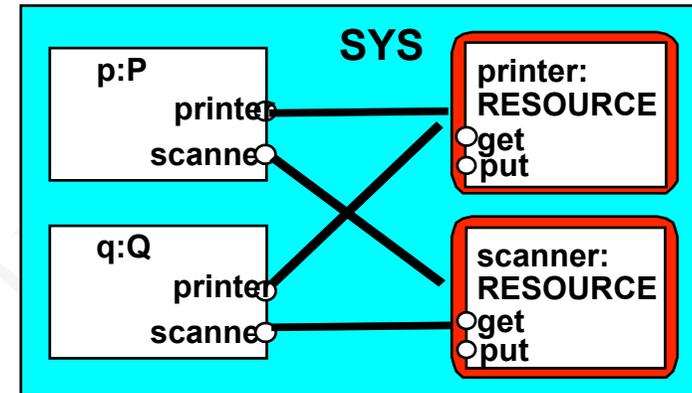
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```

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```

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P = (printer.get-> scanner.get-> copy-> printer.put-> scanner.put-> P) .
```

```
Q = (scanner.get-> printer.get-> copy-> scanner.put-> printer.put-> Q) .
```

```

||SYS = (p:P || q:Q || {p,q}::printer:RESOURCE ||
{p,q}::scanner:RESOURCE) .
    
```

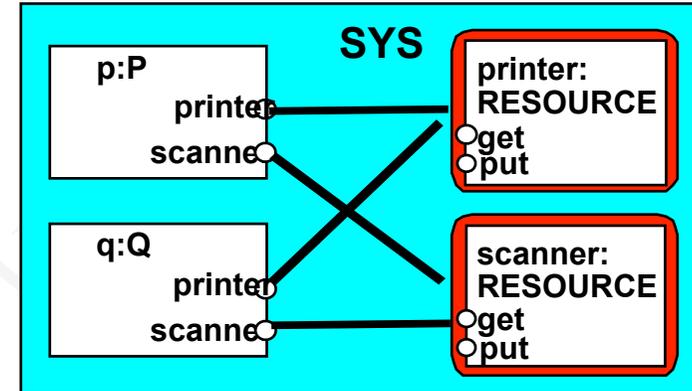
**Deadlock trace?**

# Deadlock Analysis - Parallel Composition

- ◆ In practice, deadlock arises from **parallel composition** of interacting processes.

```

P = (x -> y -> P) .
Q = (y -> x -> Q) .
||D = (P || Q) .
    
```



```
RESOURCE = (get-> put-> RESOURCE) .
```

```
P = (printer.get-> scanner.get-> copy-> printer.put->
```

Trace to DEADLOCK:

```

p.printer.get
q.scanner.get
    
```

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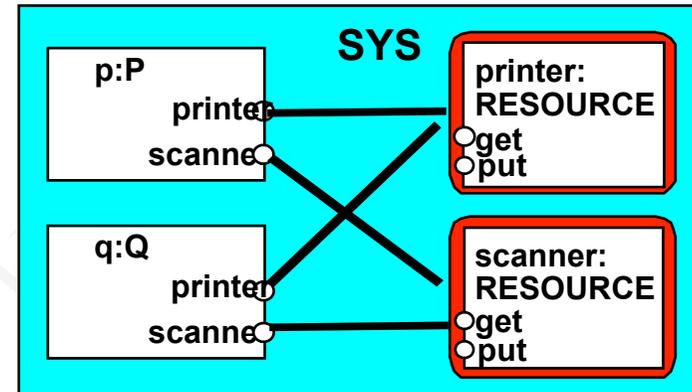
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Deadlock trace?

Avoidance...



# Recall The 4 Conditions

- 1. Mutual exclusion condition (aka. "Serially reusable resources"):**  
the processes involved share resources which they use under mutual exclusion.
- 2. Hold-and-wait condition (aka. "Incremental acquisition"):**  
processes hold on to resources already allocated to them while waiting to acquire additional resources.
- 3. No preemption condition:**  
once acquired by a process, resources cannot be "pre-empted" (forcibly withdrawn) but are only released voluntarily.
- 4. Circular-wait condition (aka. "Wait-for cycle"):**  
a circular chain (or cycle) of processes exists such that each process holds a resource which its successor in the cycle is waiting to acquire.

# Deadlock Analysis – Avoidance (#1 ?)

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◆ Ideas?



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### ◆ Ideas?

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**Deadlock?**

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Deadlock?



Scalability?

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# Deadlock Analysis – Avoidance (#2 ?)

## 2. Hold-and-wait condition (aka. "Incremental acquisition"):

processes hold on to resources already allocated to them while waiting to acquire additional resources.



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     copy->  
     scanner.put->  
     printer.put->
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Deadlock?



Efficiency/Scalability?

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Deadlock?



Efficiency/Scalability?



# Deadlock Analysis – Avoidance (#3 ?)

## 3. No pre-emption condition:

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**Deadlock?**



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Deadlock?



Progress?

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Deadlock?



Progress?



# Deadlock Analysis – Avoidance (#4 ?)

## 4. Circular-wait condition (aka. "Wait-for cycle"):

a circular chain (or cycle) of processes exists such that each process holds a resource which its successor in the cycle is waiting to acquire.



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**Deadlock?**

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Deadlock?



Scalability/Progress/...?

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Deadlock?



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Deadlock?



Scalability/Progress/...?



General solution: "sort" resource acquisitions



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```

Deadlock?



Scalability/Progress/...?

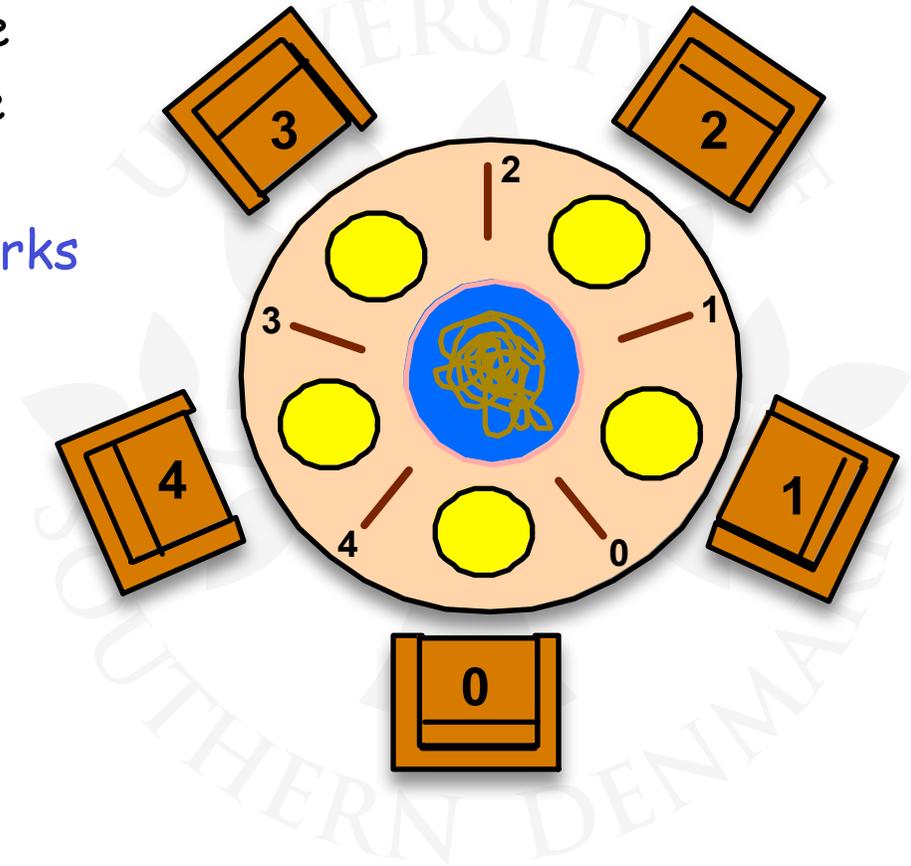


General solution: "sort" resource acquisitions

**BUT Sort by... ..what?**

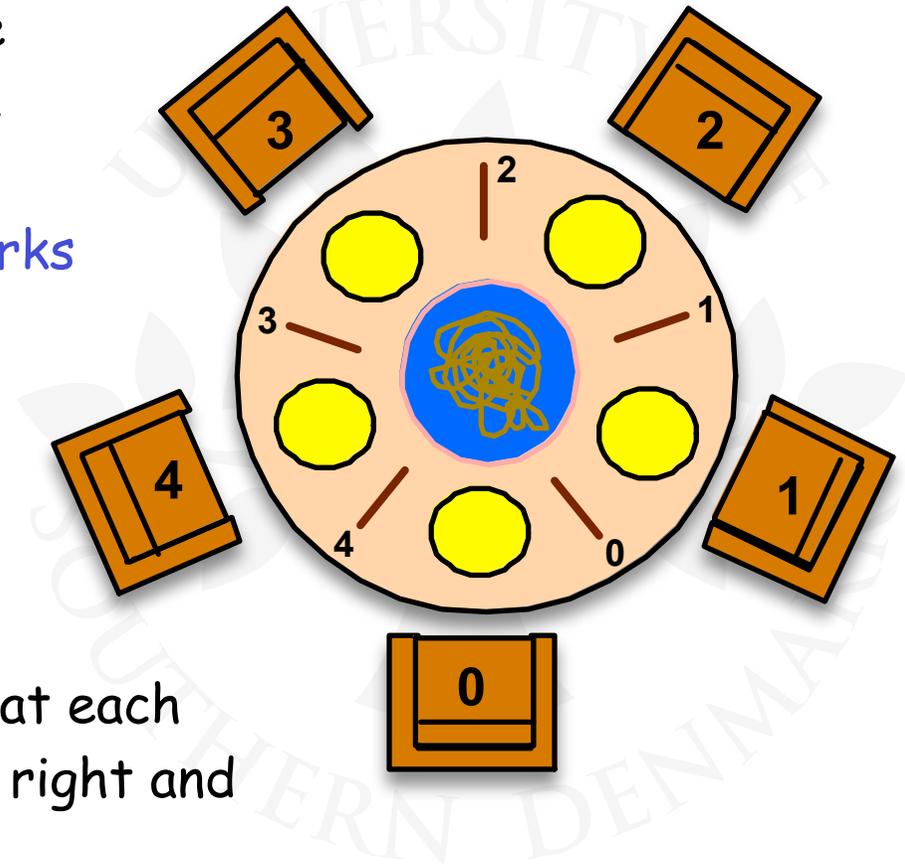
## 6.2 Dining Philosophers

Five philosophers sit around a circular table. Each philosopher spends his life alternately **thinking** and **eating**. In the centre of the table is a large bowl of spaghetti. A philosopher needs **two forks** to eat a helping of spaghetti.



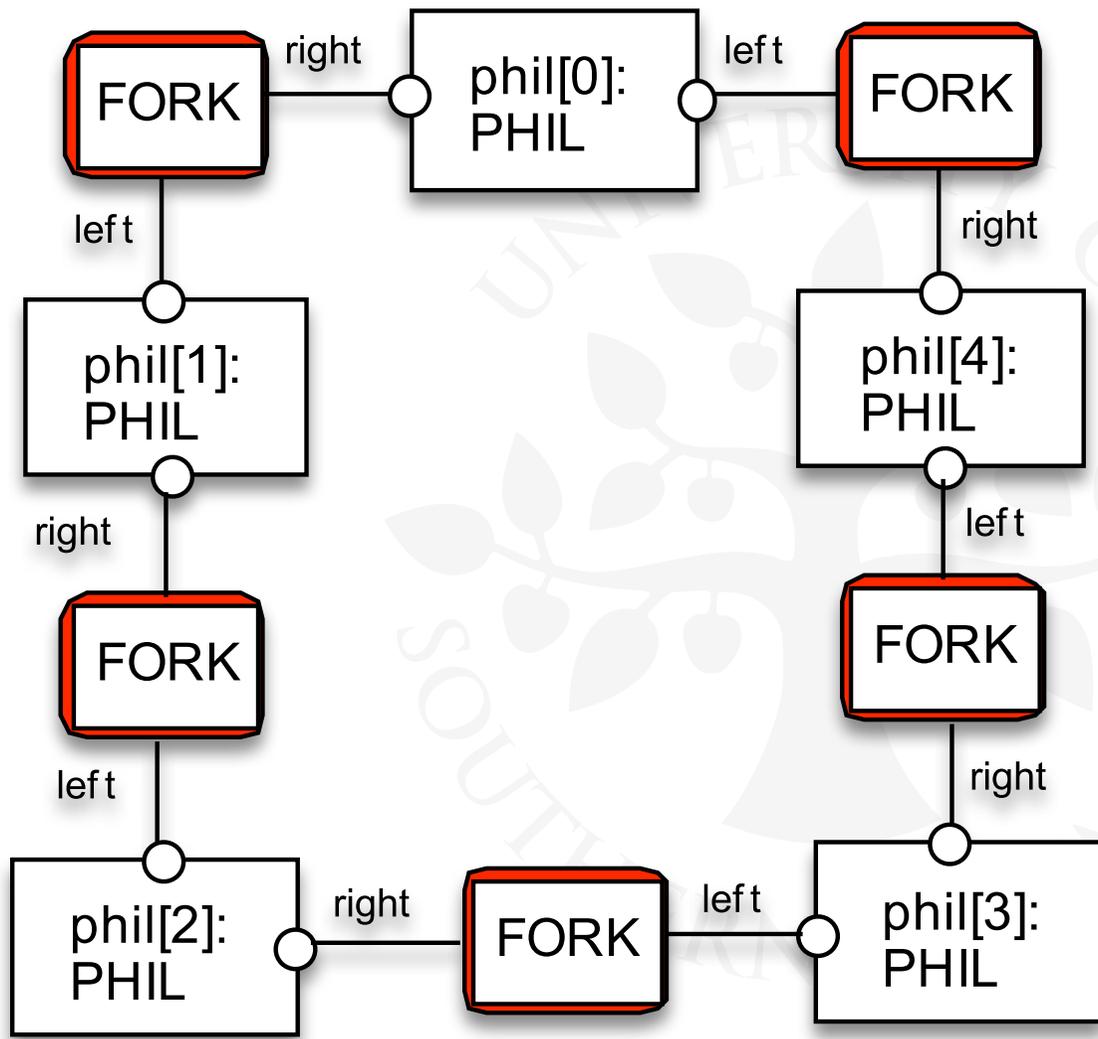
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One fork is placed between each pair of philosophers and they agree that each will only use the fork to his immediate right and left.

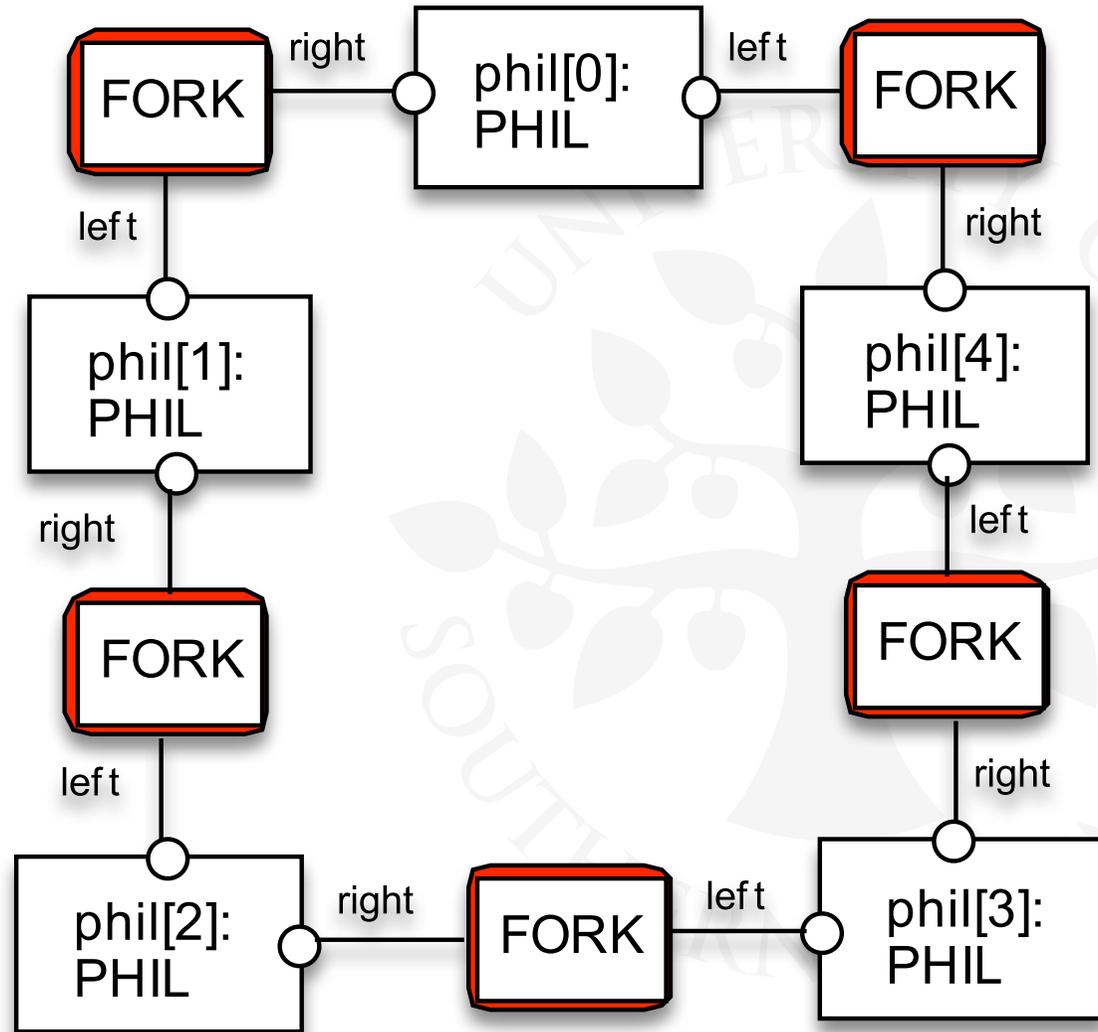
# Dining Philosophers - Model Structure Diagram





# Dining Philosophers - Model Structure Diagram

Each **FORK** is a **shared resource** with actions **get** and **put**.

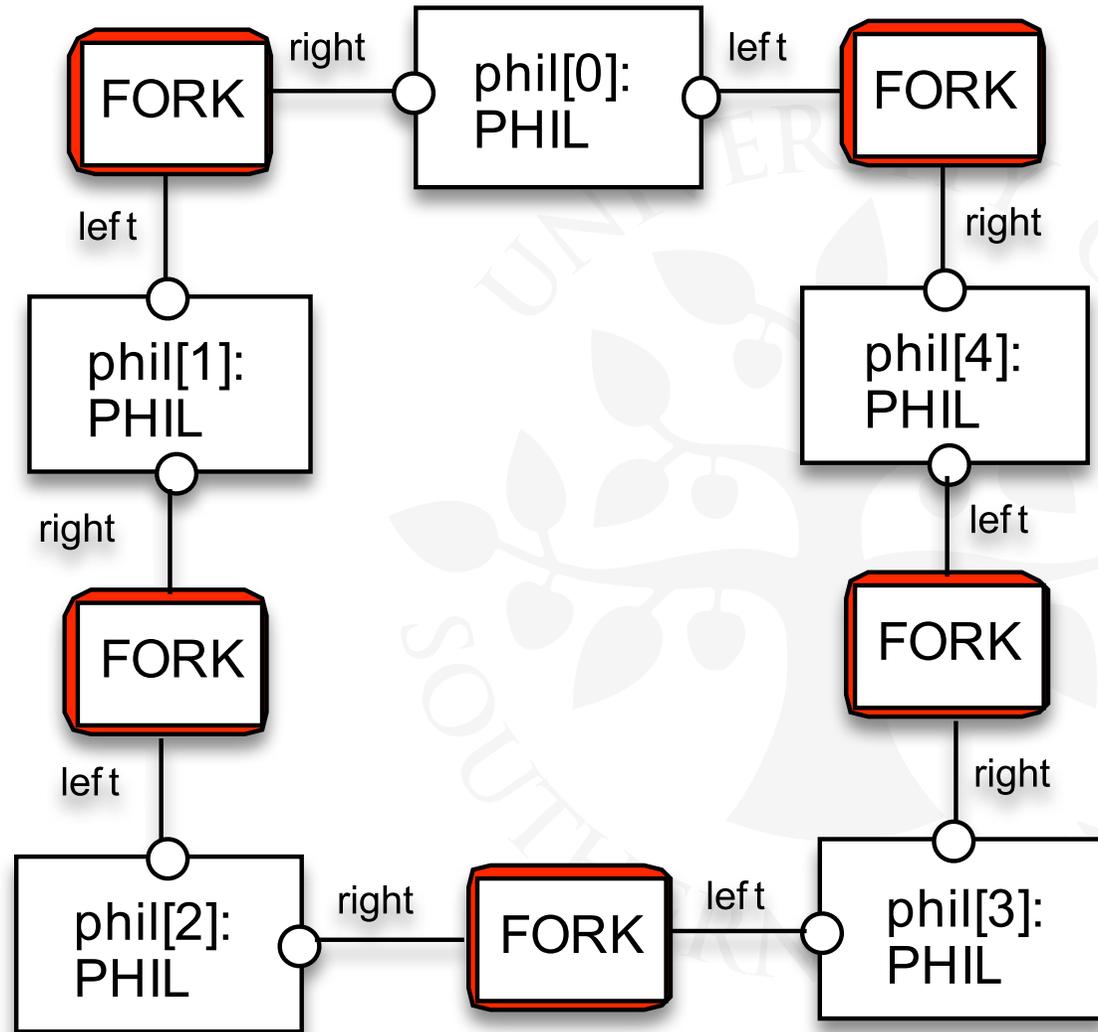




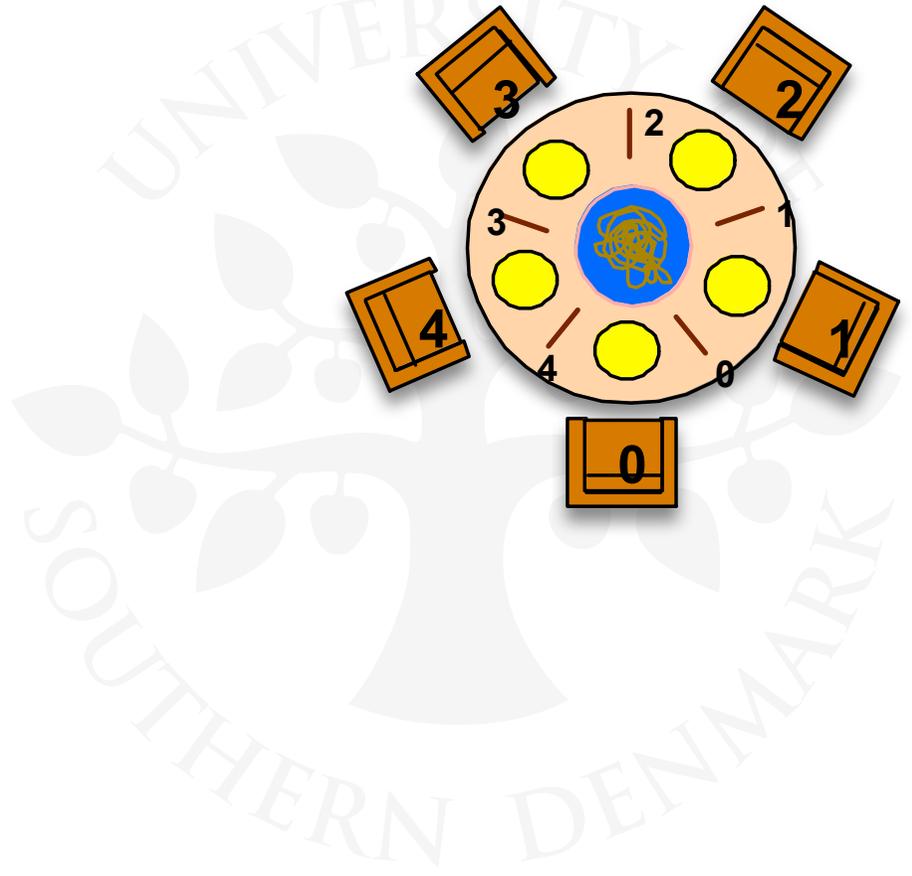
# Dining Philosophers - Model Structure Diagram

Each **FORK** is a **shared resource** with actions **get** and **put**.

When hungry, each **PHIL** must first get his right and left forks before he can start eating.

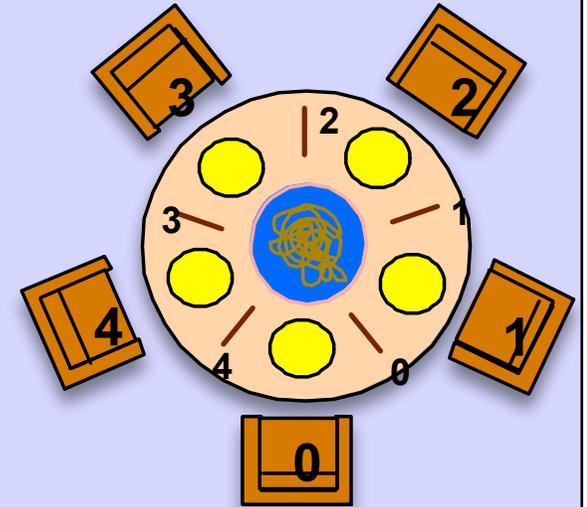


# Dining Philosophers - Model



# Dining Philosophers - Model

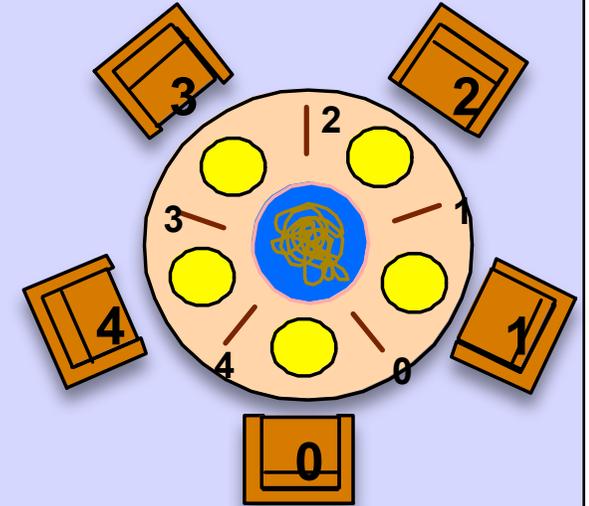
const N = 5



# Dining Philosophers - Model

```
const N = 5
```

```
FORK = (get-> put-> FORK) .
```

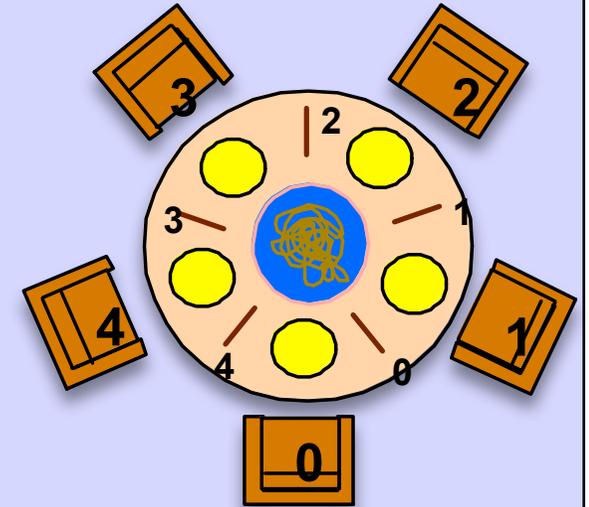


# Dining Philosophers - Model

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const N = 5
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```
FORK = (get-> put-> FORK) .
```

```
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```

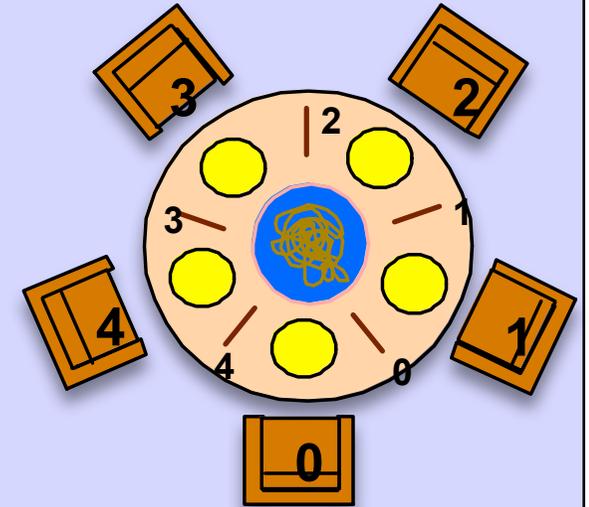


# Dining Philosophers - Model

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```

```
FORK = (get-> put-> FORK) .
```

```
PHIL = (sit          ->
        right.get   ->
        left.get    ->
```

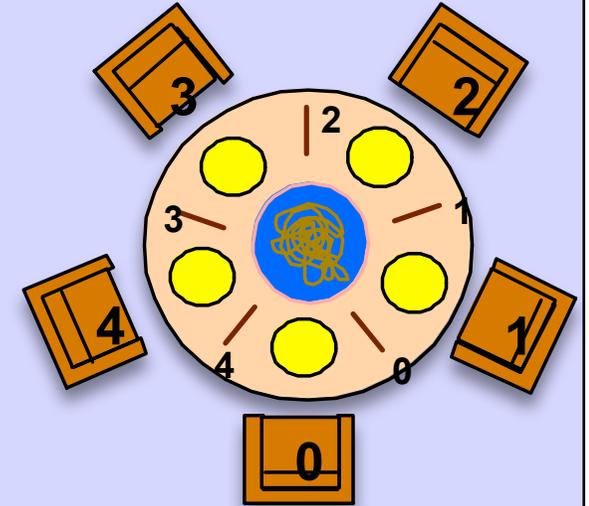


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```
FORK = (get-> put-> FORK) .
```

```
PHIL = (sit          ->  
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        left.get    ->  
        eat         ->
```

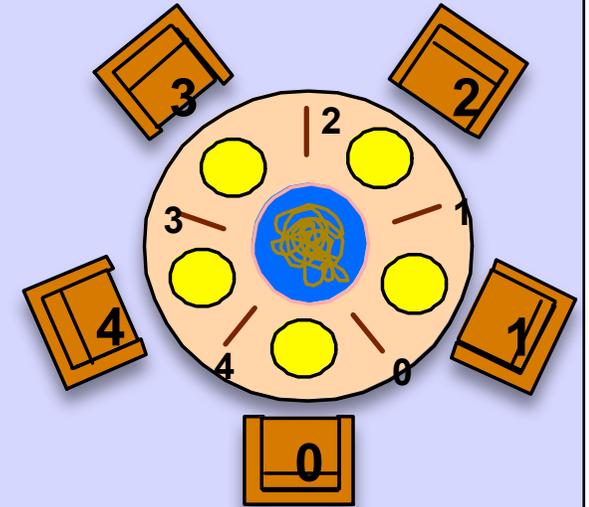


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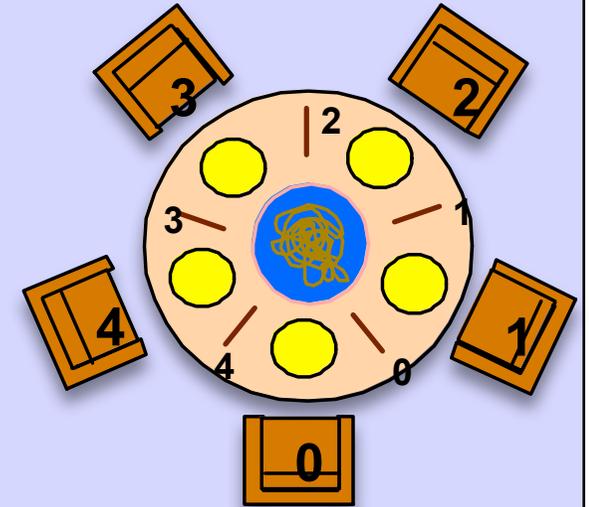


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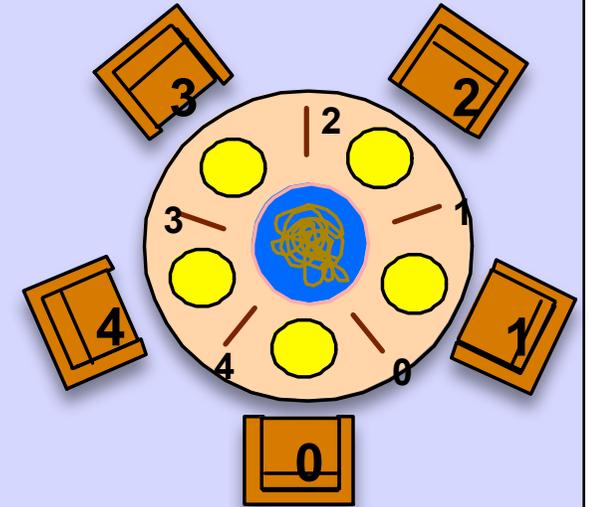
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FORK = (get-> put-> FORK) .

PHIL = (sit          ->
        right.get   ->
        left.get    ->
        eat         ->
        left.put    ->
        right.put   ->
        arise       -> PHIL) .

```



# Dining Philosophers - Model

```

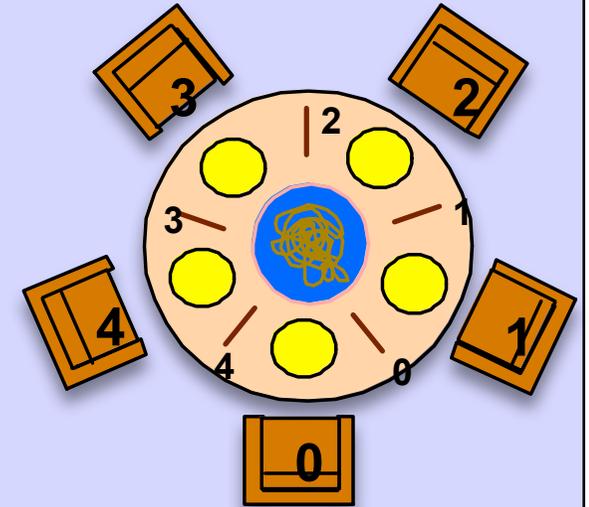
const N = 5

FORK = (get-> put-> FORK) .

PHIL = (sit          ->
        right.get   ->
        left.get    ->
        eat         ->
        left.put    ->
        right.put   ->
        arise       -> PHIL) .

|| DINING_PHILOSOPHERS =

```



# Dining Philosophers - Model

```

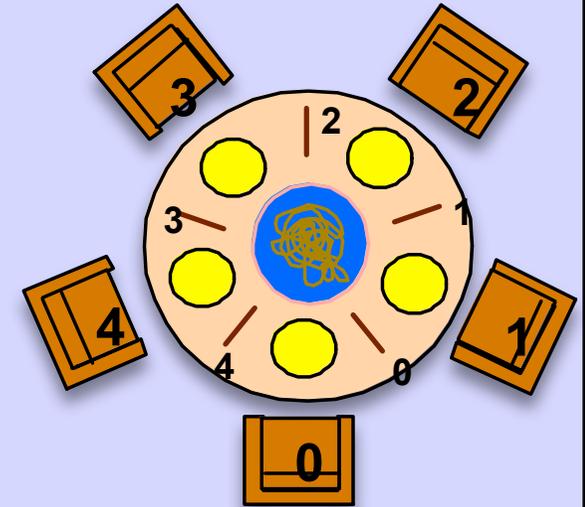
const N = 5

FORK = (get-> put-> FORK) .

PHIL = (sit          ->
        right.get   ->
        left.get    ->
        eat         ->
        left.put    ->
        right.put   ->
        arise       -> PHIL) .

||DINING_PHILOSOPHERS =
  forall [i:0..N-1] (phil[i]:PHIL ||

```



# Dining Philosophers - Model

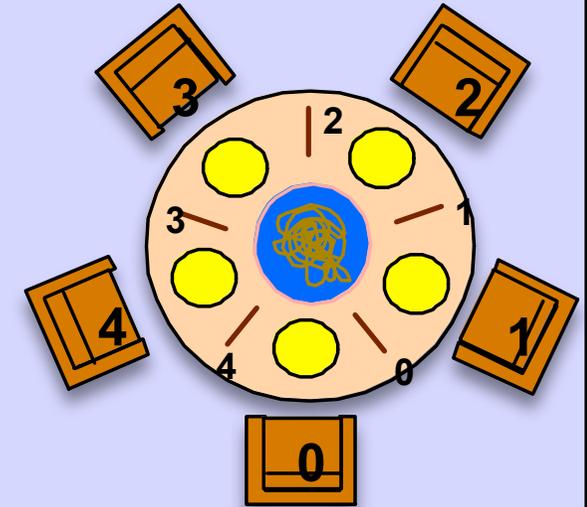
```

const N = 5

FORK = (get-> put-> FORK) .

PHIL = (sit          ->
        right.get  ->
        left.get   ->
        eat        ->
        left.put   ->
        right.put  ->
        arise      -> PHIL) .

```



```

||DINING_PHILOSOPHERS =
  forall [i:0..N-1] (phil[i]:PHIL ||

```

FORK) .

# Dining Philosophers - Model

```

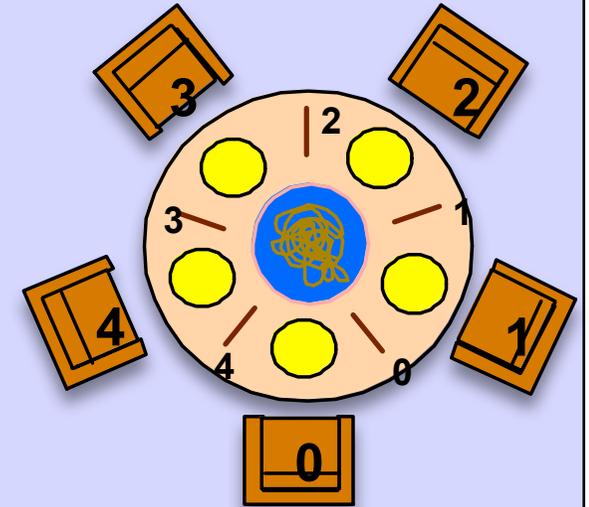
const N = 5

FORK = (get-> put-> FORK) .

PHIL = (sit          ->
        right.get  ->
        left.get   ->
        eat        ->
        left.put   ->
        right.put  ->
        arise      -> PHIL) .

||DINING_PHILOSOPHERS =
  forall [i:0..N-1] (phil[i]:PHIL ||
    { phil[i].left, phil[((i-1)+N)%N].right }::FORK) .

```

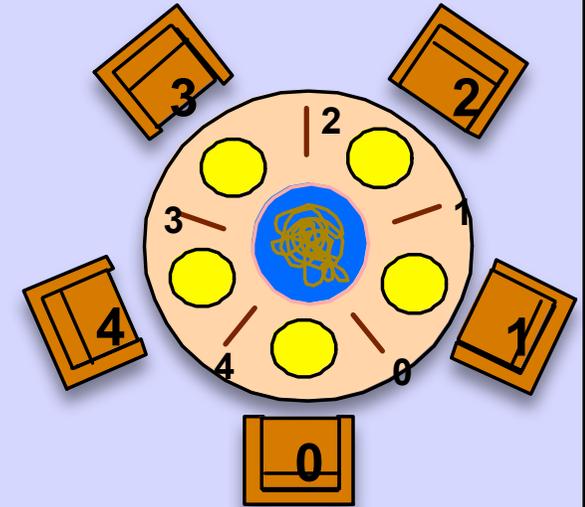


# Dining Philosophers - Model

```
const N = 5
```

```
FORK = (get-> put-> FORK) .
```

```
PHIL = (sit          ->  
       right.get    ->  
       left.get     ->  
       eat          ->  
       left.put     ->  
       right.put    ->  
       arise        -> PHIL) .
```



Can this system deadlock?

```
|| DINING_PHILOSOPHERS =
```

```
forall [i:0..N-1] (phil[i]:PHIL ||
```

```
{ phil[i].left, phil[((i-1)+N)%N].right }::FORK) .
```

# Dining Philosophers - Model Analysis



# Dining Philosophers - Model Analysis

Trace to DEADLOCK:



# Dining Philosophers - Model Analysis

Trace to DEADLOCK:  
phil.0.sit



# Dining Philosophers - Model Analysis

```
Trace to DEADLOCK:  
phil.0.sit  
phil.0.right.get
```



# Dining Philosophers - Model Analysis

**Trace to DEADLOCK:**

```
phil.0.sit
```

```
phil.0.right.get
```

```
phil.1.sit
```



# Dining Philosophers - Model Analysis

Trace to DEADLOCK:

```
phil.0.sit
```

```
phil.0.right.get
```

```
phil.1.sit
```

```
phil.1.right.get
```



# Dining Philosophers - Model Analysis

Trace to DEADLOCK:

```
phil.0.sit
```

```
phil.0.right.get
```

```
phil.1.sit
```

```
phil.1.right.get
```

```
phil.2.sit
```



# Dining Philosophers - Model Analysis

```
Trace to DEADLOCK:  
phil.0.sit  
phil.0.right.get  
phil.1.sit  
phil.1.right.get  
phil.2.sit  
phil.2.right.get
```



# Dining Philosophers - Model Analysis

Trace to DEADLOCK:

```
phil.0.sit
```

```
phil.0.right.get
```

```
phil.1.sit
```

```
phil.1.right.get
```

```
phil.2.sit
```

```
phil.2.right.get
```

```
phil.3.sit
```



# Dining Philosophers - Model Analysis

Trace to DEADLOCK:

```
phil.0.sit  
phil.0.right.get  
phil.1.sit  
phil.1.right.get  
phil.2.sit  
phil.2.right.get  
phil.3.sit  
phil.3.right.get
```



# Dining Philosophers - Model Analysis

Trace to DEADLOCK:

```
phil.0.sit  
phil.0.right.get  
phil.1.sit  
phil.1.right.get  
phil.2.sit  
phil.2.right.get  
phil.3.sit  
phil.3.right.get  
phil.4.sit
```



# Dining Philosophers - Model Analysis

Trace to DEADLOCK:

`phil.0.sit`

`phil.0.right.get`

`phil.1.sit`

`phil.1.right.get`

`phil.2.sit`

`phil.2.right.get`

`phil.3.sit`

`phil.3.right.get`

`phil.4.sit`

`phil.4.right.get`





# Dining Philosophers - Model Analysis

Trace to DEADLOCK:

```
phil.0.sit  
phil.0.right.get  
phil.1.sit  
phil.1.right.get  
phil.2.sit  
phil.2.right.get  
phil.3.sit  
phil.3.right.get  
phil.4.sit  
phil.4.right.get
```

This is the situation where all the philosophers become hungry at the same time, sit down at the table and each philosopher picks up the fork to his **right**.



# Dining Philosophers - Model Analysis

Trace to DEADLOCK:

```
phil.0.sit  
phil.0.right.get  
phil.1.sit  
phil.1.right.get  
phil.2.sit  
phil.2.right.get  
phil.3.sit  
phil.3.right.get  
phil.4.sit  
phil.4.right.get
```

This is the situation where all the philosophers become hungry at the same time, sit down at the table and each philosopher picks up the fork to his **right**.

The system can make no further progress since each philosopher is waiting for a left fork held by his neighbour (i.e., a **wait-for cycle** exists)!

# Dining Philosophers





# Dining Philosophers

Deadlock is easily  
detected in our  
*model.*





# Dining Philosophers

Deadlock is easily detected in our **model**.

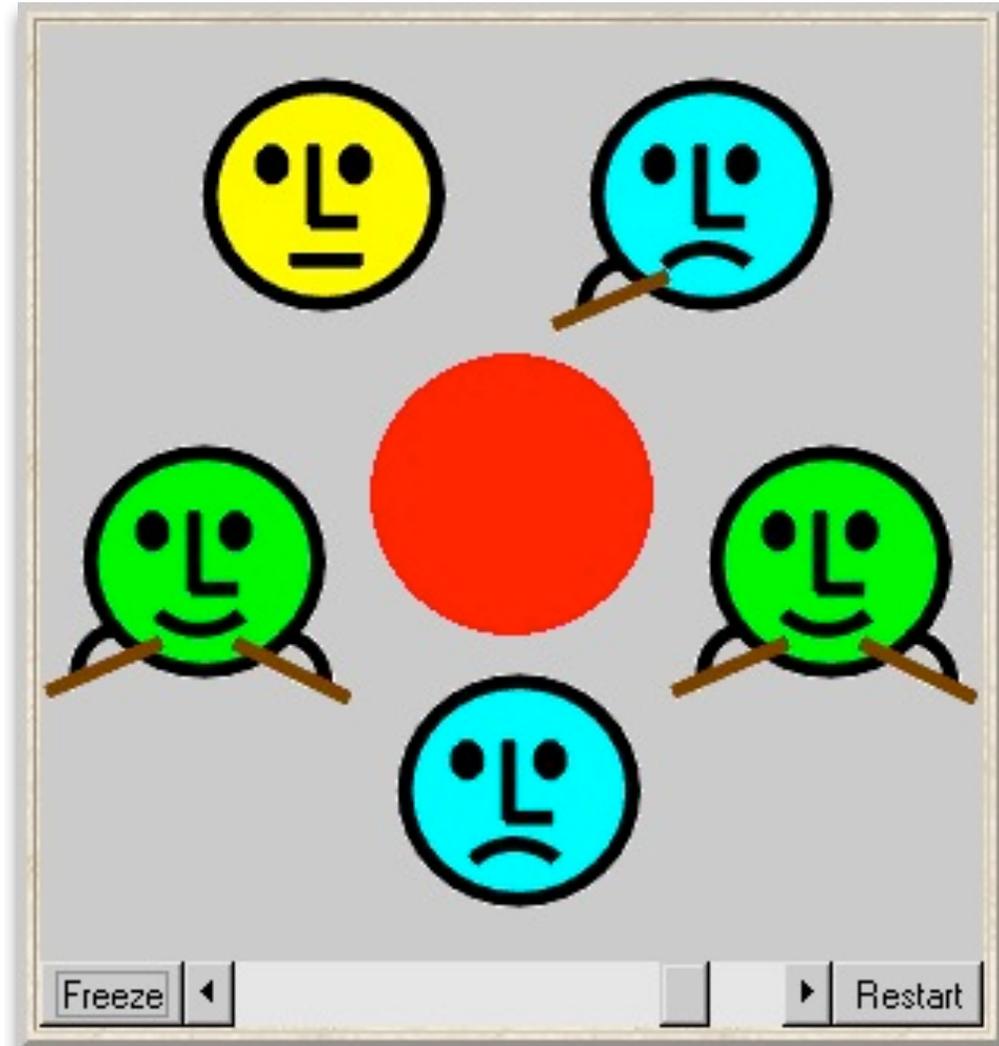
How easy is it to detect a potential deadlock in an **implementation**?



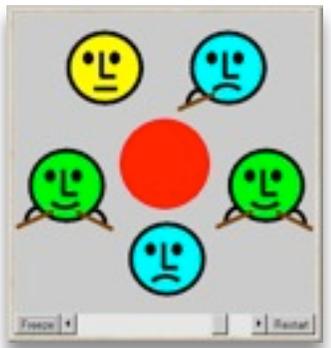
# Dining Philosophers

Deadlock is easily detected in our *model*.

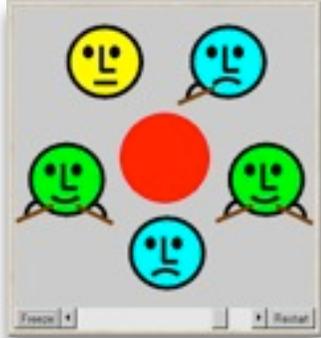
How easy is it to detect a potential deadlock in an *implementation*?



# Dining Philosophers - Implementation In Java



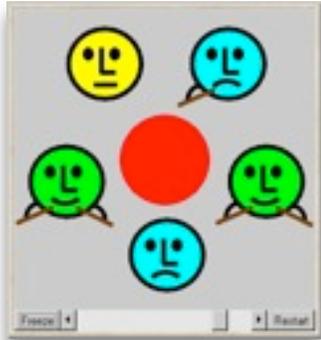
# Dining Philosophers - Implementation In Java



◆ **Philosophers:**  
active entities  
(implement as  
threads)

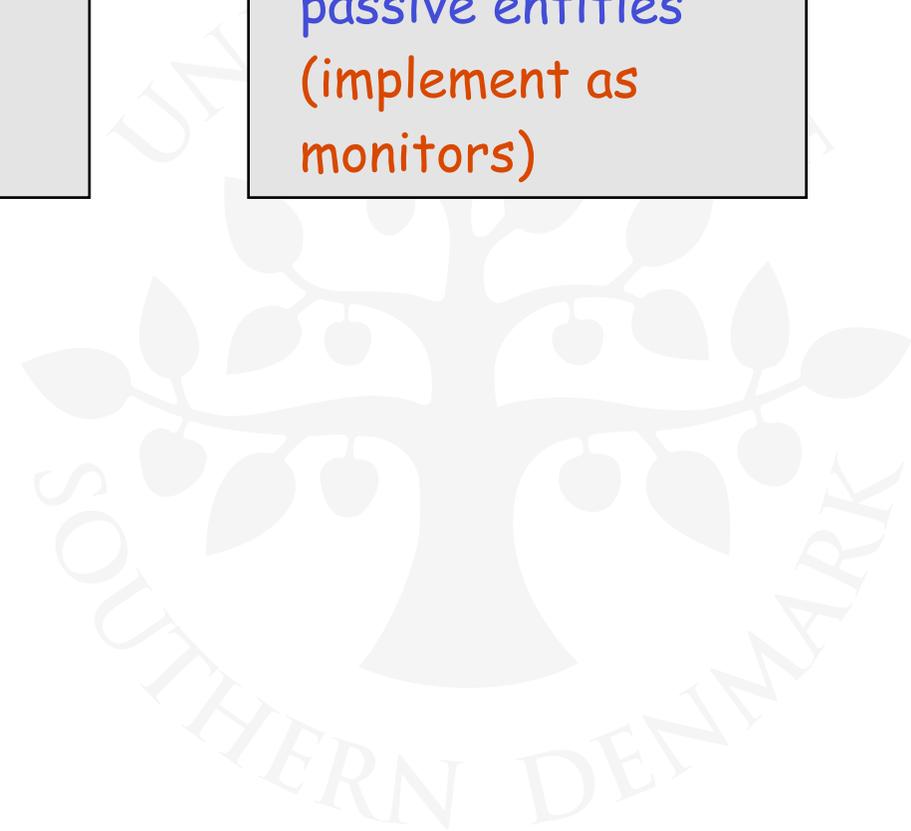


# Dining Philosophers - Implementation In Java

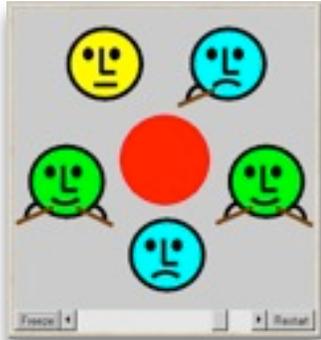


◆ **Philosophers:**  
active entities  
(implement as  
threads)

◆ **Forks:** shared  
passive entities  
(implement as  
monitors)

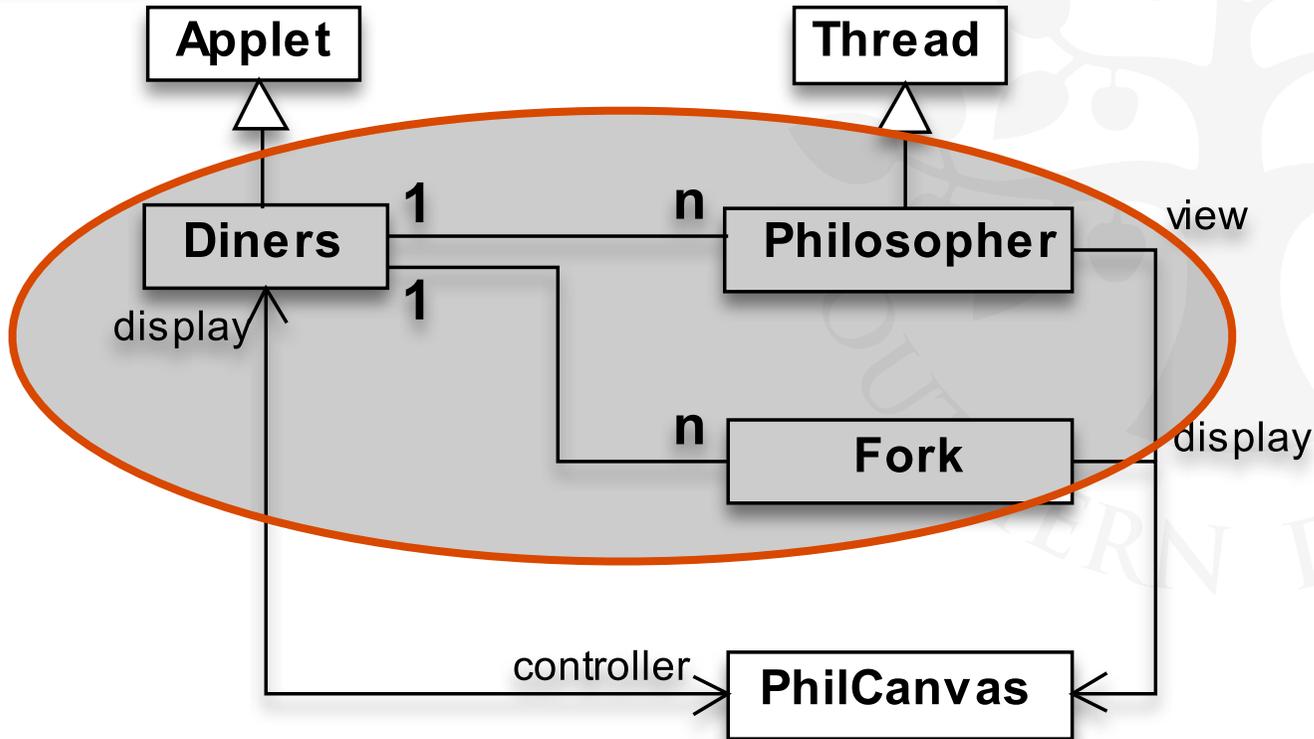


# Dining Philosophers - Implementation In Java



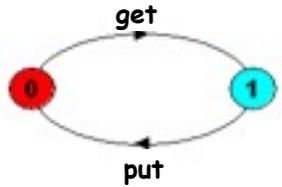
◆ **Philosophers:**  
active entities  
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◆ **Forks:** shared  
passive entities  
(implement as monitors)





# Dining Philosophers – Fork (Monitor)

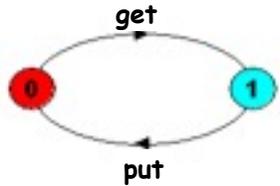


```
FORK = (get->  
        put->  
        FORK) .
```





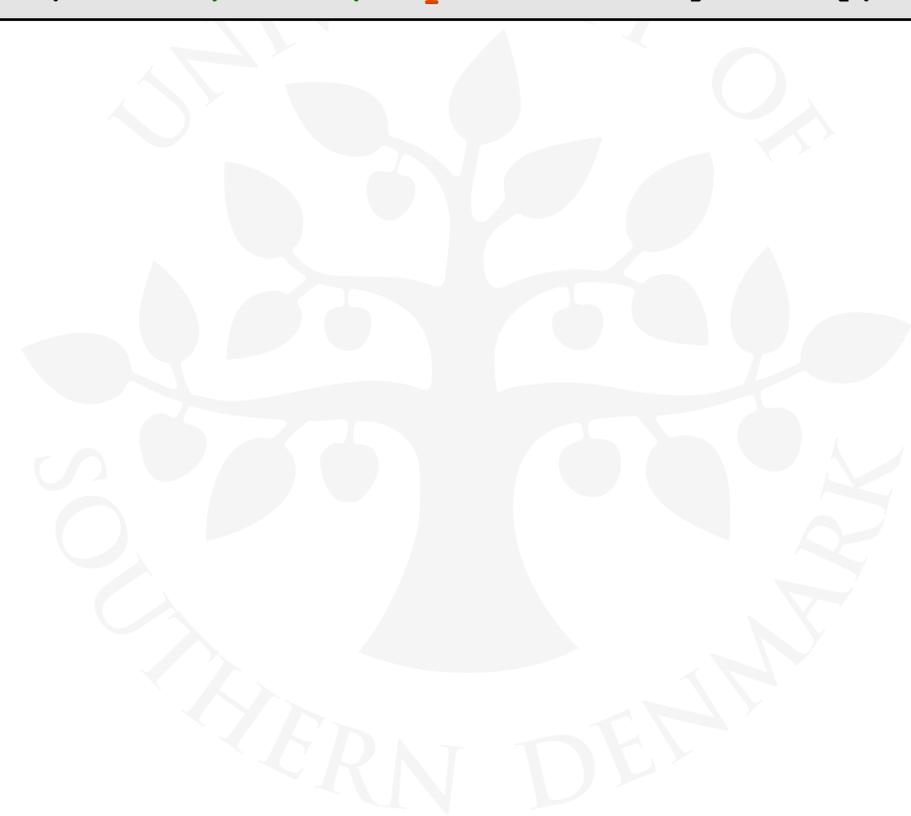
# Dining Philosophers – Fork (Monitor)



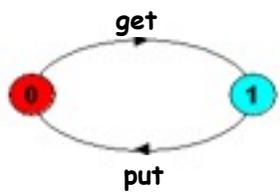
```
FORK = (get->  
        put->  
        FORK) .
```

≡

```
FORK = (FORK[FALSE] ,  
        FORK[taken:B] (when (!taken) get-> FORK[TRUE]  
                       |when (taken)  put-> FORK[FALSE]) .
```



# Dining Philosophers – Fork (Monitor)



```

FORK = (get->
put->
FORK) .
    
```

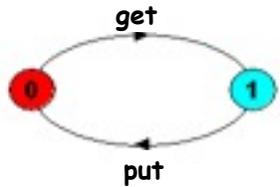
```

FORK = (FORK[FALSE] ,
FORK[taken:B] (when (!taken) get-> FORK[TRUE]
| when (taken) put-> FORK[FALSE] ) .
    
```

Not needed  
(if we always  
"get before put")



# Dining Philosophers – Fork (Monitor)



```

FORK = (get->
          put->
          FORK) .
  
```

```

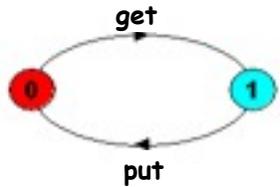
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Not needed  
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"get before put")

```

class Fork {
  private PhilCanvas display;
  
```

# Dining Philosophers – Fork (Monitor)



```

FORK = (get->
          put->
          FORK) .
    
```

```

FORK = (FORK[FALSE] ,
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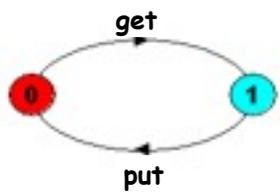
```

class Fork {
  private PhilCanvas display;
  private boolean taken = false;
}
    
```

*taken* encodes the state of the fork

# Dining Philosophers – Fork (Monitor)

Not needed  
(if we always  
"get before put")



```

FORK = (get->
          put->
          FORK).
    
```

```

FORK = (FORK[FALSE] ,
FORK[taken:B] (when (!taken) get-> FORK[TRUE]
                 | when (taken) put-> FORK[FALSE]) .
    
```

```

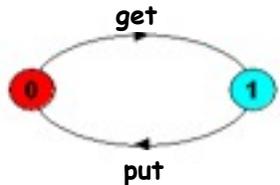
class Fork {
    private PhilCanvas display;
    private boolean taken = false;

    synchronized void get() throws Int'Exc' {
        while (taken) wait();           // cond. synch. (!)
        taken = true;
        display.setFork(identity, taken);
    }
}
    
```

*taken* encodes the  
state of the fork

# Dining Philosophers – Fork (Monitor)

Not needed  
 (if we always  
 "get before put")



```

FORK = ( get->
           put->
           FORK ) .
  
```

```

FORK = ( FORK[FALSE] ,
           FORK[taken:B] ( when (!taken) get-> FORK[TRUE]
                               | when (taken) put-> FORK[FALSE] ) ) .
  
```

```

class Fork {
  private PhilCanvas display;
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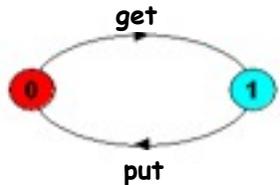
  synchronized void get() throws Int'Exc' {
    while (taken) wait();           // cond. synch. (!)
    taken = true;
    display.setFork(identity, taken);
  }

  synchronized void put() {
  
```

*taken* encodes the  
 state of the fork

# Dining Philosophers – Fork (Monitor)

Not needed  
(if we always  
"get before put")



```

FORK = ( get->
           put->
           FORK ) .
  
```

```

FORK = ( FORK[FALSE] ,
           FORK[taken:B] ( when (!taken) get-> FORK[TRUE]
                               | when (taken) put-> FORK[FALSE] ) ) .
  
```

```

class Fork {
  private PhilCanvas display;
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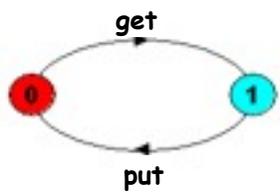
  synchronized void get() throws Int'Exc' {
    while (taken) wait();           // cond. synch. (!)
    taken = true;
    display.setFork(identity, taken);
  }

  synchronized void put() {
    taken = false;
  }
}
  
```

*taken* encodes the state of the fork

# Dining Philosophers – Fork (Monitor)

Not needed  
(if we always  
"get before put")



```

FORK = (get->
          put->
          FORK) .
    
```

```

FORK = (FORK[FALSE] ,
FORK[taken:B] (when (!taken) get-> FORK[TRUE]
                 | when (taken) put-> FORK[FALSE]) .
    
```

```

class Fork {
  private PhilCanvas display;
  private boolean taken = false;

  synchronized void get() throws Int'Exc' {
    while (taken) wait(); // cond. synch. (!)
    taken = true;
    display.setFork(identity, taken);
  }

  synchronized void put() {
    taken = false;
    display.setFork(identity, taken);
    notify(); // cond. synch. (!)
  }
}
    
```

taken encodes the state of the fork



# Dining Philosophers – Philosopher (Thread)

```
PHIL = (sit -> right.get -> left.get -> eat -> left.put -> right.put -> arise -> PHIL) .
```





# Dining Philosophers – Philosopher (Thread)

```
PHIL = (sit -> right.get -> left.get -> eat -> left.put -> right.put -> arise -> PHIL).
```

```
class Philosopher extends Thread {  
    Fork left, right;
```



# Dining Philosophers – Philosopher (Thread)

```
PHIL = (sit -> right.get -> left.get -> eat -> left.put -> right.put -> arise -> PHIL).
```

```
class Philosopher extends Thread {  
    Fork left, right;  
    public void run() {  
        try {  
            while (true) {
```



# Dining Philosophers – Philosopher (Thread)

```
PHIL = (sit -> right.get -> left.get -> eat -> left.put -> right.put -> arise -> PHIL).
```

```
class Philosopher extends Thread {  
    Fork left, right;  
    public void run() {  
        try {  
            while (true) {  
                view.setPhil(identity, view.SIT);  
                sleep(controller.sitTime());  
            }  
        }  
    }  
}
```



# Dining Philosophers – Philosopher (Thread)

```
PHIL = (sit -> right.get -> left.get -> eat -> left.put -> right.put -> arise -> PHIL).
```

```
class Philosopher extends Thread {
    Fork left, right;
    public void run() {
        try {
            while (true) {
                view.setPhil(identity, view.SIT);
                sleep(controller.sitTime());
                right.get();
                view.setPhil(identity, view.GOTRIGHT);
                sleep(500); // constant pause!
            }
        }
    }
}
```



# Dining Philosophers – Philosopher (Thread)

```
PHIL = (sit -> right.get -> left.get -> eat -> left.put -> right.put -> arise -> PHIL).
```

```
class Philosopher extends Thread {
    Fork left, right;
    public void run() {
        try {
            while (true) {
                view.setPhil(identity, view.SIT);
                sleep(controller.sitTime());
                right.get();
                view.setPhil(identity, view.GOTRIGHT);
                sleep(500); // constant pause!
                left.get();
                view.setPhil(identity, view.EATING);
                sleep(controller.eatTime());
            }
        }
    }
}
```



# Dining Philosophers – Philosopher (Thread)

```
PHIL = (sit -> right.get -> left.get -> eat -> left.put -> right.put -> arise -> PHIL).
```

```
class Philosopher extends Thread {
    Fork left, right;
    public void run() {
        try {
            while (true) {
                view.setPhil(identity, view.SIT);
                sleep(controller.sitTime());
                right.get();
                view.setPhil(identity, view.GOTRIGHT);
                sleep(500); // constant pause!
                left.get();
                view.setPhil(identity, view.EATING);
                sleep(controller.eatTime());
                left.put();
                right.put();
                view.setPhil(identity, view.ARISE);
                sleep(controller.ariseTime());
            }
        }
    }
}
```



# Dining Philosophers – Philosopher (Thread)

```
PHIL = (sit -> right.get -> left.get -> eat -> left.put -> right.put -> arise -> PHIL).
```

```
class Philosopher extends Thread {
    Fork left, right;
    public void run() {
        try {
            while (true) {
                view.setPhil(identity, view.SIT);
                sleep(controller.sitTime());
                right.get();
                view.setPhil(identity, view.GOTRIGHT);
                sleep(500); // constant pause!
                left.get();
                view.setPhil(identity, view.EATING);
                sleep(controller.eatTime());
                left.put();
                right.put();
                view.setPhil(identity, view.ARISE);
                sleep(controller.ariseTime());
            }
        } catch (InterruptedException _) {}
    }
}
```



# Dining Philosophers – Main Applet

```
||DINING_PHILOSOPHERS =  
  forall [i:0..N-1] (phil[i]:PHIL ||  
    { phil[i].left, phil[((i-1)+N)%N].right }::FORK) .
```

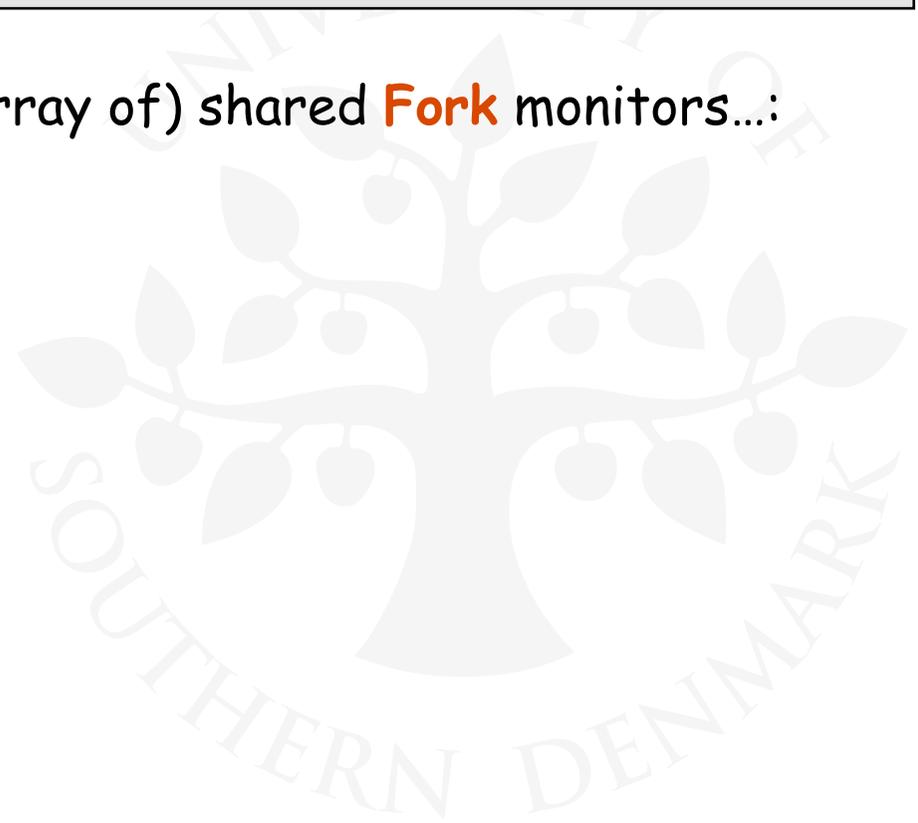




# Dining Philosophers – Main Applet

```
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  forall [i:0..N-1] (phil[i]:PHIL ||  
    { phil[i].left, phil[((i-1)+N)%N].right }::FORK) .
```

The applet's start() method creates (an array of) shared **Fork** monitors...:

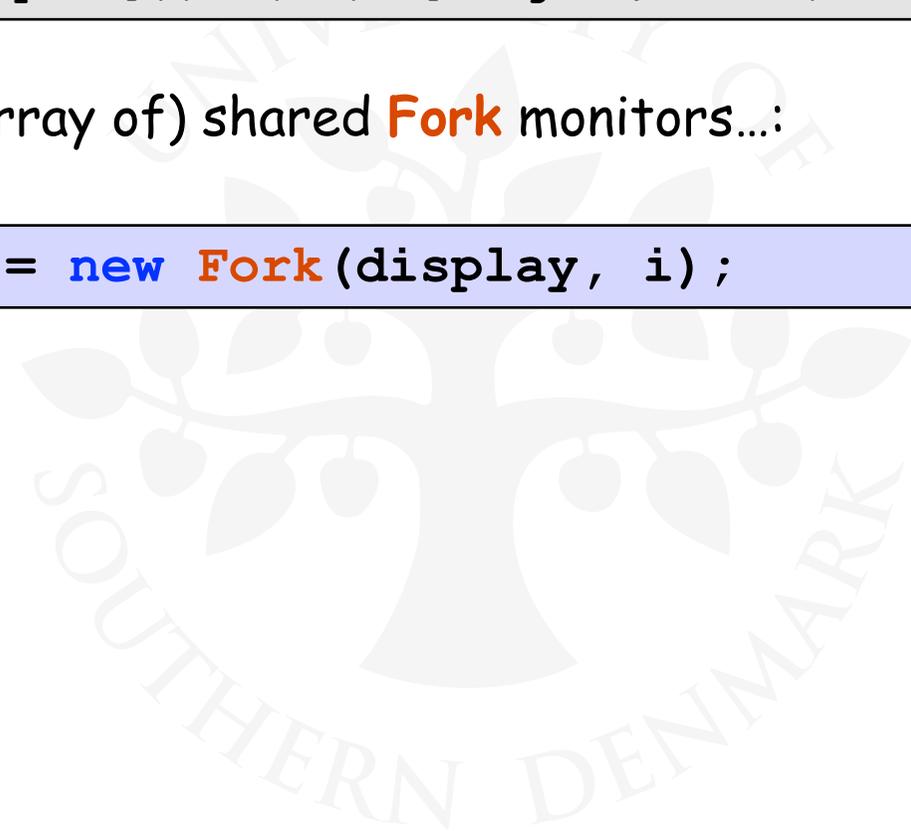


# Dining Philosophers – Main Applet

```
||DINING_PHILOSOPHERS =  
  forall [i:0..N-1] (phil[i]:PHIL ||  
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```

The applet's start() method creates (an array of) shared **Fork** monitors...:

```
for (int i=0; i<N; i++) fork[i] = new Fork(display, i);
```



# Dining Philosophers – Main Applet

```
||DINING_PHILOSOPHERS =  
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The applet's start() method creates (an array of) shared **Fork** monitors...:

```
for (int i=0; i<N; i++) fork[i] = new Fork(display, i);
```

...and (an array of) **Philosopher** threads (with refs to forks):



# Dining Philosophers – Main Applet

```
||DINING_PHILOSOPHERS =  
  forall [i:0..N-1] (phil[i]:PHIL ||  
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```

The applet's start() method creates (an array of) shared **Fork** monitors...:

```
for (int i=0; i<N; i++) fork[i] = new Fork(display, i);
```

...and (an array of) **Philosopher** threads (with refs to forks):

```
for (int i=0; i<N; i++)  
  phil[i] =  
    new Philosopher(this, i, fork[(i-1+N)%N], fork[i]);
```



# Dining Philosophers – Main Applet

```
||DINING_PHILOSOPHERS =  
  forall [i:0..N-1] (phil[i]:PHIL ||  
    { phil[i].left, phil[((i-1)+N)%N].right }::FORK) .
```

The applet's start() method creates (an array of) shared **Fork** monitors...:

```
for (int i=0; i<N; i++) fork[i] = new Fork(display, i);
```

...and (an array of) **Philosopher** threads (with refs to forks):

```
for (int i=0; i<N; i++)  
  phil[i] =  
    new Philosopher(this, i,   
      fork[(i-1+N)%N], fork[i]);
```

Diagram: The code above shows two blue curly braces. The first brace is labeled 'left' and spans from `fork[(i-1+N)%N]` to `fork[i]`. The second brace is labeled 'right' and spans from `fork[i]` to `fork[(i-1+N)%N]`.



# Dining Philosophers – Main Applet

```
||DINING_PHILOSOPHERS =  
  forall [i:0..N-1] (phil[i]:PHIL ||  
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for (int i=0; i<N; i++) fork[i] = new Fork(display, i);
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...and (an array of) **Philosopher** threads (with refs to forks):

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...and start all Philosopher threads:



# Dining Philosophers – Main Applet

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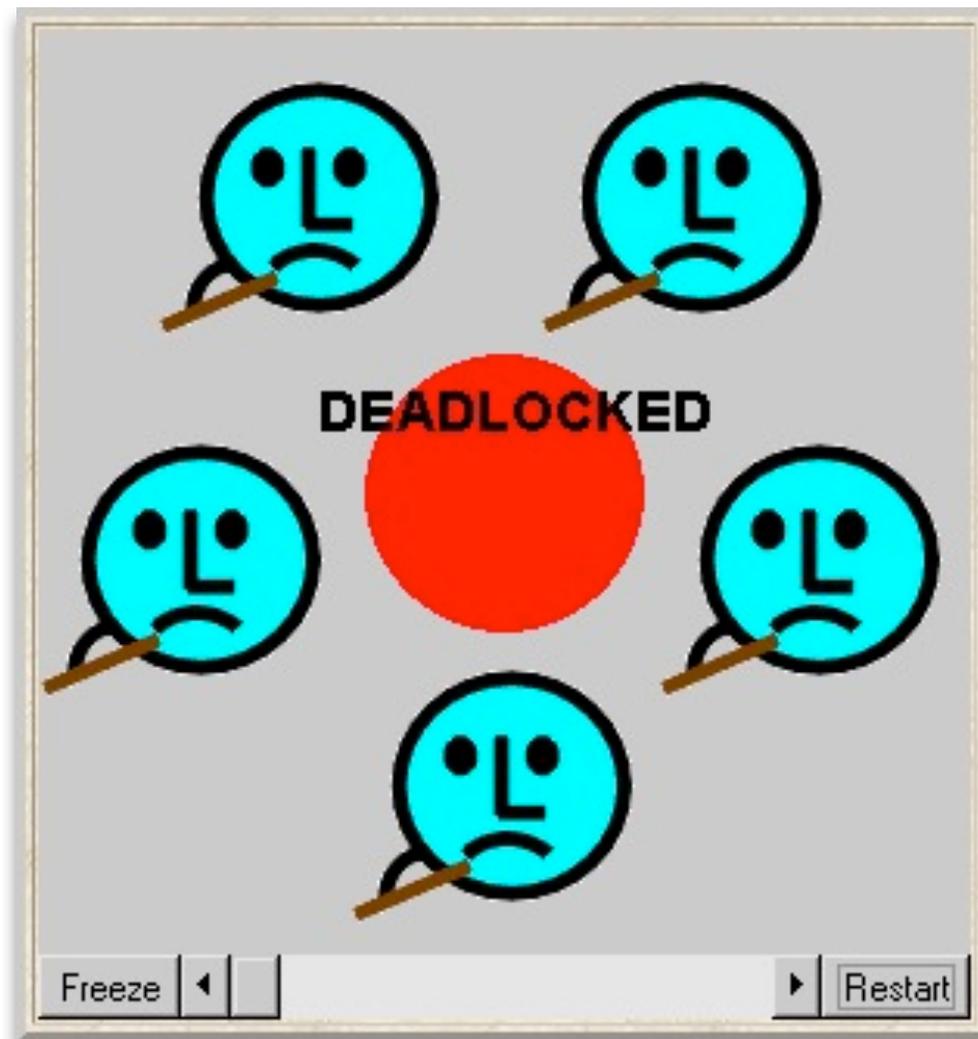
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for (int i=0; i<N; i++) phil[i].start();
```

# Dining Philosophers

To ensure deadlock occurs eventually, the slider control may be moved to the left. This reduces the time each philosopher spends thinking and eating.

This "speedup" increases the **probability** of deadlock occurring.



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Deadlock can be avoided by ensuring that a wait-for cycle cannot exist.



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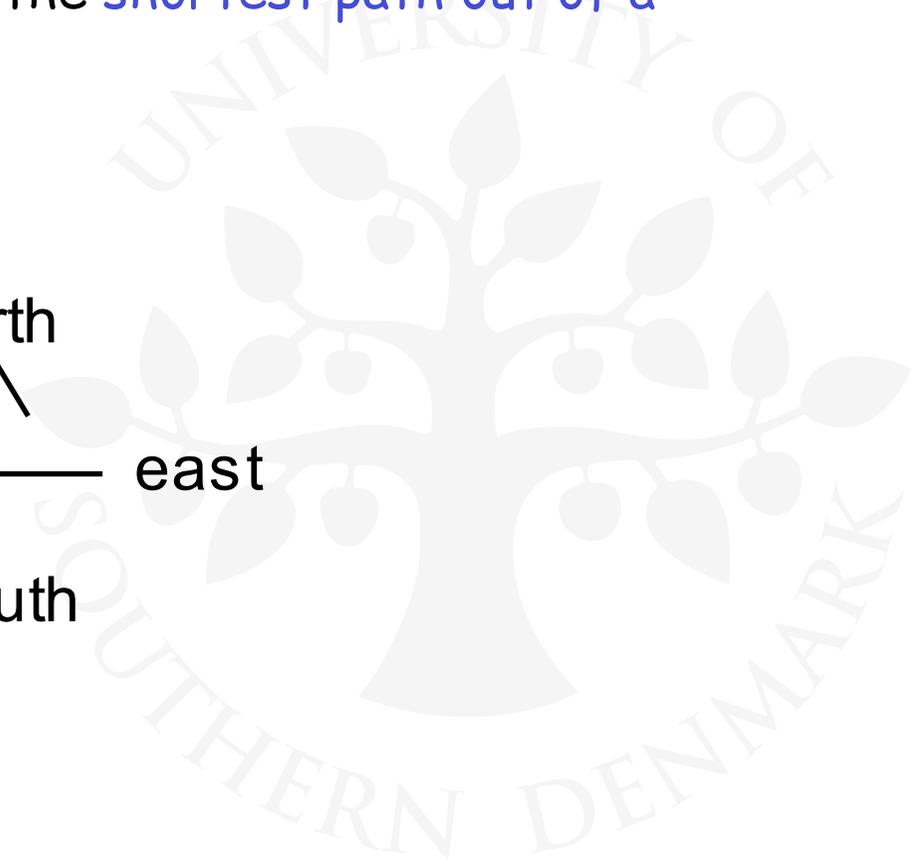
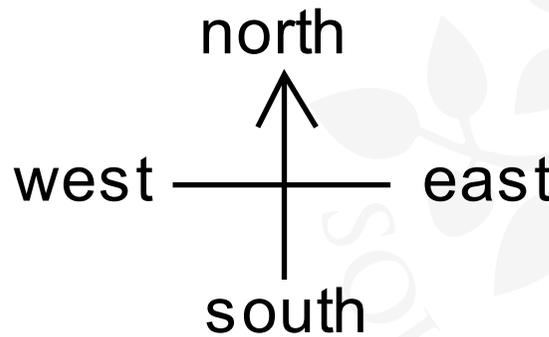
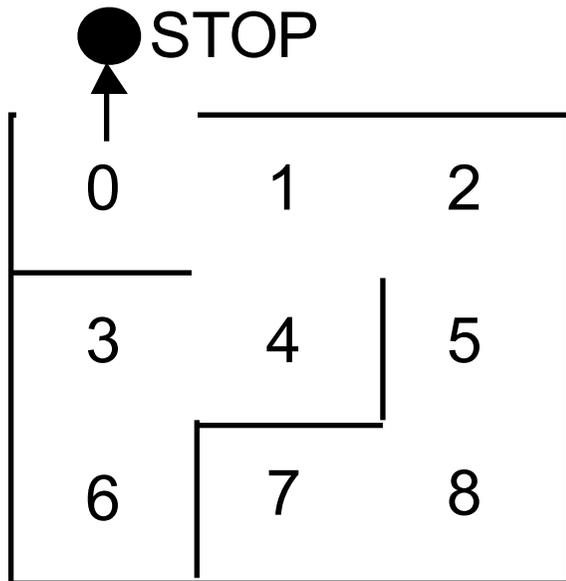
Other strategies?

1. Mutual exclusion condition
2. Hold-and-wait condition
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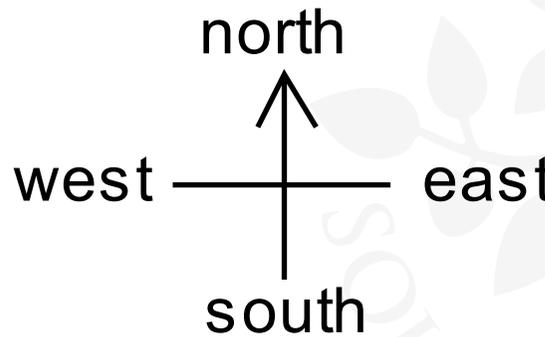
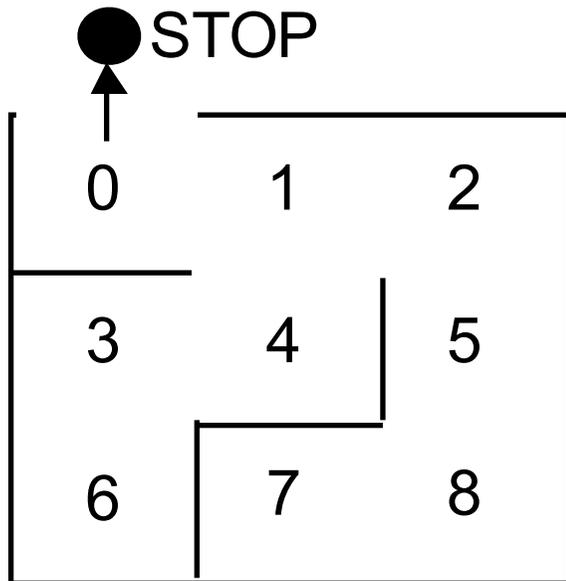
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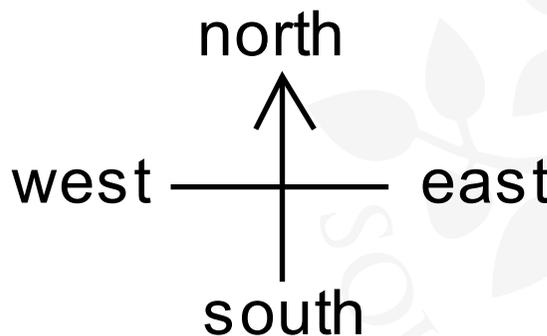
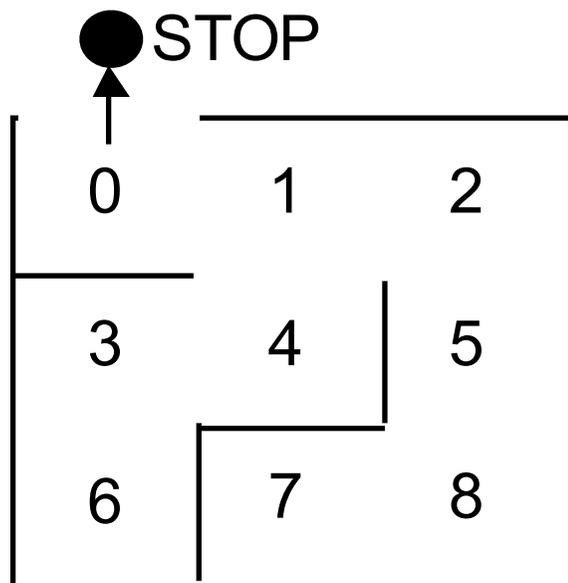
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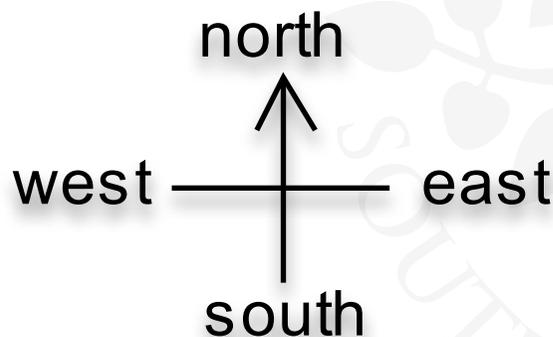
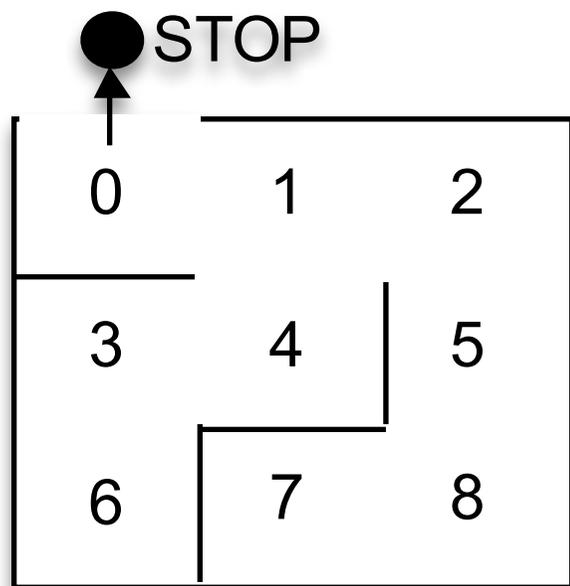
eg.  $\text{MAZE}(\text{Start}=8) = P[\text{Start}],$   
 $P[0] = (\text{north} \rightarrow \text{STOP} \mid \text{east} \rightarrow P[1]), \dots$



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|| GETOUT = MAZE (7) .

Shortest path escape  
trace from position 7 ?



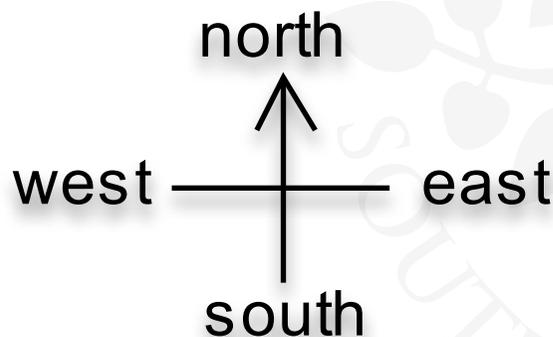
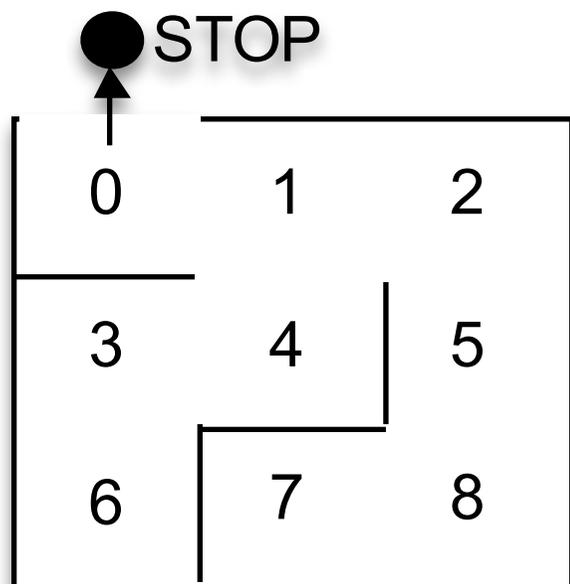
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north  
north  
west  
west  
north

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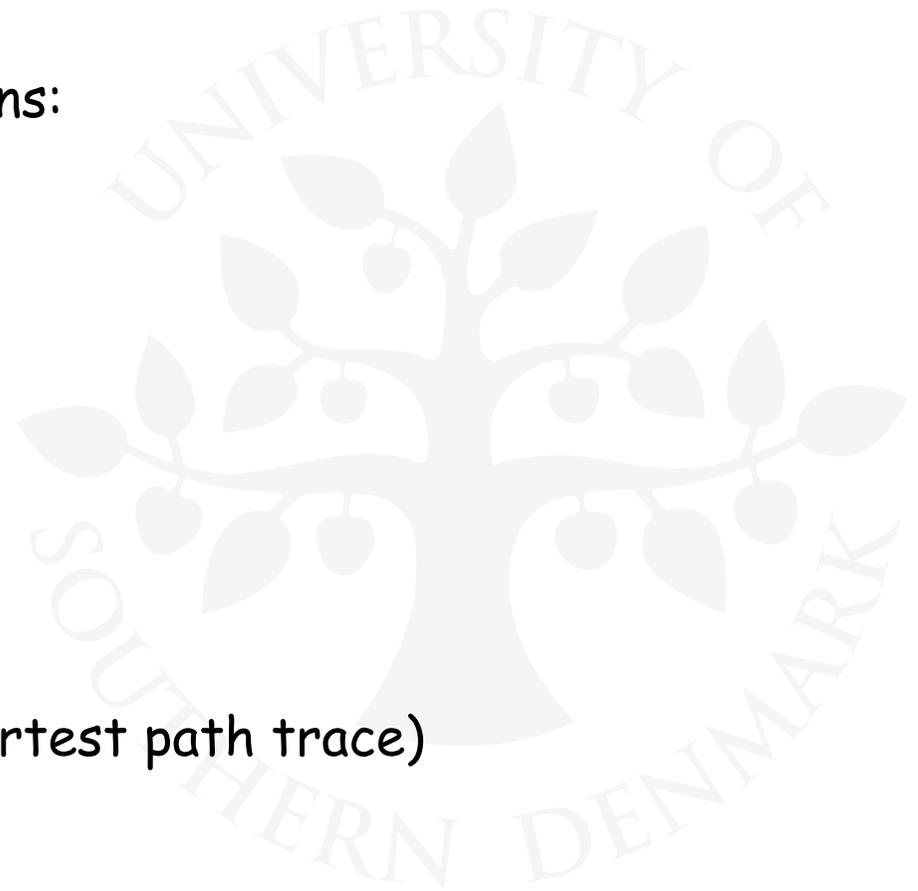
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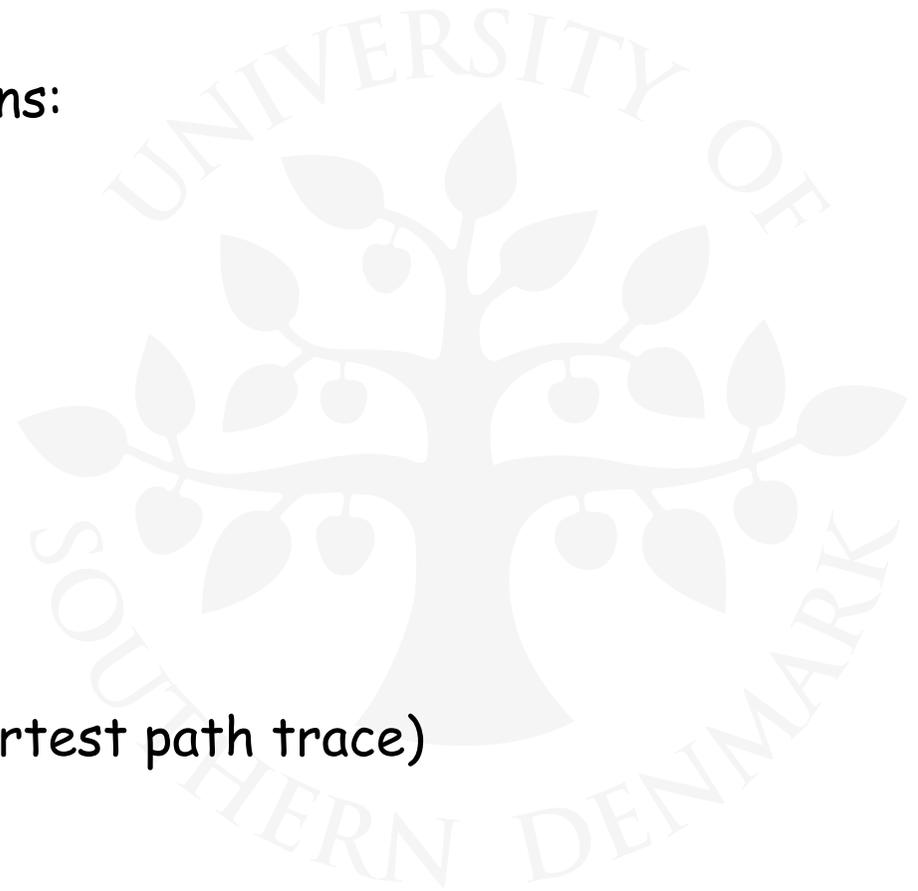
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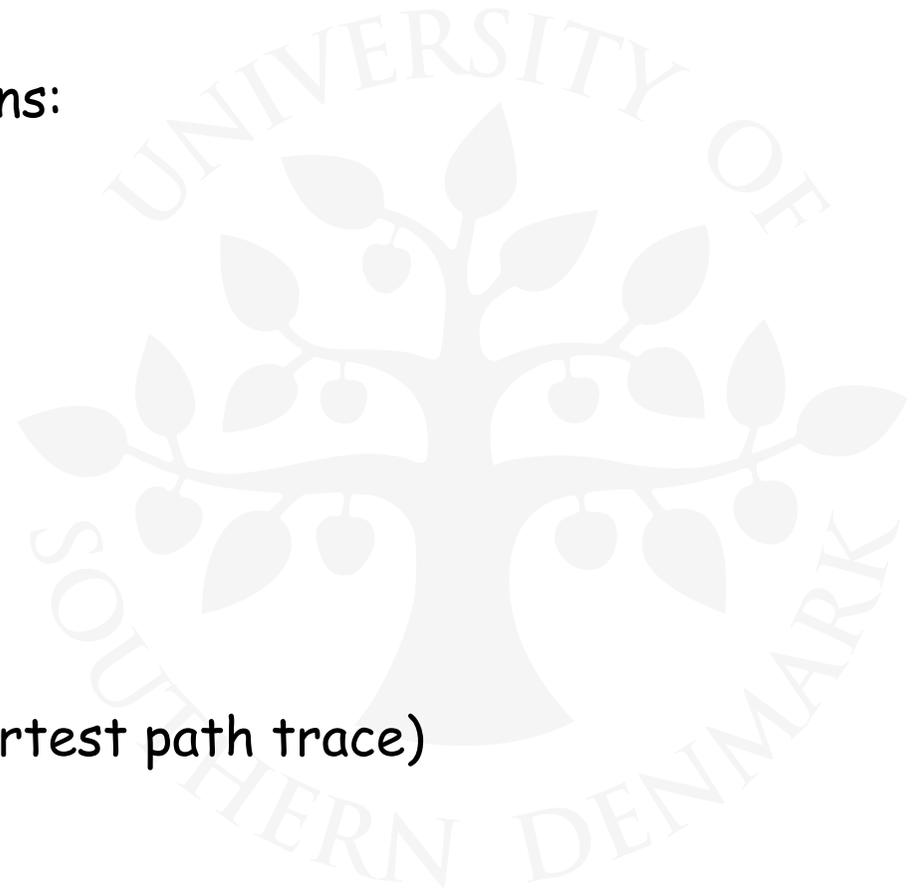
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**Aim** - deadlock avoidance:  
"Break at least one of the deadlock conditions".

## ◆ Models

- no eligible actions (analysis gives shortest path trace)

## ◆ Practice

- blocked threads