

## Exercise 1

Scalability

Assume the following hypothetical overhead function for an algorithm (as usual  $W$  denotes the problem size).

$$T_O = p^2 \cdot \sqrt{W} + p \cdot \sqrt{W}$$

Assume that maximal degree of concurrency of the algorithm is  $2^{\sqrt{W}}$ .

- a) Determine the parallel computation time  $T_P$  (as a function in  $W$  and  $p$ ).
- b) Determine the isoefficiency function due to the overheads  $T_O$ .
- c) Determine the isoefficiency function due to the maximal concurrency.
- d1) Determine the number of processes  $p'$ , for which the parallel runtime is minimal.
- d2) Determine the runtime when using  $p'$  processes (cmp. d1).
- d3) Determine the asymptotic efficiency (as a function in  $W$ ) when using  $p'$  processes. What is the efficiency for arbitrary large problem sizes  $W$  when using  $p'$  processes?

## Exercise 2

Prim's minimum spanning tree

In the parallel formulation of Prim's minimum spanning tree algorithm (Section 10.2), the maximum number of processes that can be used efficiently on a hypercube is  $O(n/\log(n))$ . By using  $O(n/\log(n))$  processes the run time is  $O(n \log(n))$ .

- a) What is the run time if you use  $O(n)$  processes?
- b) What is the minimum parallel run time that can be obtained on a message-passing parallel computer?
- c) How does this time compare with the run time obtained when you use  $O(n/\log(n))$  processes?