Locally Dense Independent Sets in Regular Graphs of Large Girth

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Abstract

For an integer $d \geq 3$ let $\alpha(d)$ be the supremum over all α with the property that for every $\epsilon > 0$ there exists some $g(\epsilon)$ such that every *d*-regular graph of order *n* and girth at least $g(\epsilon)$ has an independent set of cardinality at least $(\alpha - \epsilon)n$.

Extending an approach proposed by Lauer and Wormald (Large independent sets in regular graphs of large girth, J. Comb. Theory, Ser. B 97 (2007), 999-1009) and improving results due to Shearer (A note on the independence number of triangle-free graphs, II, J. Comb. Theory, Ser. B 53 (1991), 300-307) and Lauer and Wormald, we present the best known lower bounds for $\alpha(d)$ for all $d \geq 3$.