- Problems
  - Travelling salesman problem (TSP).
  - The assignment problem.
  - Set covering.
  - Feedback arc-set (FAS).
  - Graph partitioning (GP).
  - Maximum Clique and Independent set.
  - Vertex colouring.
  - Edge-colouring.
  - Vertex cover.
  - Max k-satisfiability (even max 2-SAT is NP-hard).
  - Minimum spanning strong subdigraph and minimum spanning 2edge-connected subgraph.
  - Minimum maximum degree spanning trees.
  - Knapsack, Bin packing and cutting steel plates.
  - The travelling tournament problem.
- Neighbourhoods
  - 1-opt, 2-opt, k-opt for TSP, GP, QAP, FAS etc
  - Eksponential neighbourhoods for TSP via minimum weight matching:
    - 1. Given tour  $v_1u_1v_2u_2\ldots v_ku_kv_1$  with cost function c on the edges.
    - 2. Form a complete bipartite graph G with partition  $V = \{v_1, v_2, \ldots, v_k\}$ and  $U = \{u_1, u_2, \ldots, u_k\}$ .
    - 3. Assign the weight  $c(v_i u_j) + c(u_j v_{i+1})$  to the edge  $v_i u_j$  for  $1 \le i, j \le k$  indices are modulo k.
    - 4. Find a minimum weight perfect matching M in G in polynomial time.
    - 5. Let  $\pi$  be the permutation so that  $M = \{v_1 u_{\pi(1)}, v_2 u_{\pi(2)}, \dots, v_k u_{\pi(k)}\}$
    - 6. Take  $v_1 u_{\pi(1)} v_2 u_{\pi(2)} \dots v_k u_{\pi(k)} v_1$  as the new tour.
    - 7. Repeat the procedure above
  - Pyramidal tours for TSP: these have the form  $v_1v_{i_1}v_{i_2}\ldots v_{i_r}v_nv_{j_1}v_{j_2}\ldots v_{j_{n-r-2}}$ . Where  $i_1 < \ldots < i_r$  and  $j_1 > \ldots > j_{n-r-2}$ . The best pyramidal tour can be found on polynomial time using dynamic programming.
  - Kempe chains for colouring problems