1. In general, much better.



- 1. In general, much better.
- 2. If it was not approved, do the re-exam. No retries on the re-exam.

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- 1. In general, much better.
- 2. If it was not approved, do the re-exam. No retries on the re-exam.

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3. It is due at 8:15 on November 2.

- 1. In general, much better.
- 2. If it was not approved, do the re-exam. No retries on the re-exam.
- 3. It is due at 8:15 on November 2.
- 4. Read all comments, even if it was approved.

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New assignment

Assignment 3 is available.



New assignment

- Assignment 3 is available.
- It is due at 8:15 on November 5.

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Comments about first assignment

If it was not approved:

1. You need to do the redo, by 8:30 on October 29.

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Comments about first assignment

If it was not approved:

 $1. \ \mbox{You need to do the redo, by 8:30 on October 29.}$

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2. Fix all problems with your original assignment.

Comments about first assignment

If it was not approved:

- 1. You need to do the redo, by 8:30 on October 29.
- 2. Fix all problems with your original assignment.
- 3. Turn in new version via Blackboard and graded version to your "instruktor".

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4. You will only be allowed a redo on one more assignment.

Encouragement to study

http://www.tv2fyn.dk/arkiv/2015/10/14?video_id=85676&autoplay=1

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Is this course giving you a good overview of what computer science is?

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- A. Very useful.
- B. Somewhat useful.
- C. I needed an overview, but this course is not giving it.
- D. I did not need an overview, but it is still good.
- E. I did not need an overview and do not want one.

Vote at m.socrative.com. Room number 415439.

What is your opinion about the pace of the lectures?

- A. Much too fast.
- B. A little too fast.
- C. Close to right.
- D. A little too slow.
- E. Much too slow.

Vote at m.socrative.com. Room number 415439.

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How difficult is the course?

- A. Much too difficult.
- B. A little too difficult.
- C. A good level.
- D. A little too easy.
- E. Much too easy.

Vote at m.socrative.com. Room number 415439.

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What do you think about U50A?

- A. It's a terrible lecture hall.
- B. It's still bad, but better with screens and microphone.

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- C. It's OK.
- D. It's good now.

Vote at m.socrative.com. Room number 415439.

1. What do you like about the course?



1. What do you like about the course?

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2. What can be improved?

- 1. What do you like about the course?
- 2. What can be improved?
- 3. Any comments I should give your "instruktor"s?

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Classical bin packing

Use as few bins as possible: Item sizes: $n \times [1/2, \epsilon]$ Bin size: 1



Result by First-Fit algorithm:



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Dual bin packing

Given a fixed number of bins, pack as many items as possible.

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```
Bin size: 1
Number of bins: 4
Item sizes:
```

```
\begin{array}{c|c} \frac{1}{4}, \frac{1}{4}, \frac{1}{4} \\ \hline \frac{5}{12}, \frac{1}{3} \\ \hline \frac{5}{12}, \frac{1}{3} \\ \hline \frac{5}{12}, \frac{1}{3} \\ \hline \frac{5}{12}, \frac{1}{3} \\ \hline \frac{1}{3}, \frac{1}{3}, \frac{1}{3} \end{array}
```

Can they all be there?

Bin packing

First-Fit is an on-line algorithm:

It handles requests without looking at future requests.

Solving bin packing optimally is NP-hard.

Brute force takes a long time.

Approximation algorithms: First-Fit-Decreasing, even better...

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Special case: all sizes multiples of $\frac{1}{12}$.

Fill one bin completely if possible.

First-Fit for dual bin packing

```
procedure First-Fit-Dual(List):
{ Input: List is a list of items with sizes \leq 1 }
{ Output: Number of rejected items }
```

```
k := \text{number of bins } \{ \text{ all empty } \}
Count := 0 { number rejected }
get next item x and remove from list
i := 1
while (i \le k and x does not fit in bin i)
i := i + 1
if (i \le k)
then put x in bin i
else Count := Count+1
return(Count)
```

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First-Fit for dual bin packing (correct)

```
\label{eq:procedure First-Fit-Dual(List):} $$ { Input: List is a list of items with sizes $\leq 1 $} $$ { Output: Number of rejected items }
```

```
k := number of bins { all empty }
Count := 0 { number rejected }
while there are still items in the list
begin
```

```
get next item x and remove from list

i := 1

while (i \le k \text{ and } x \text{ does not fit in bin } i)

i := i + 1

if (i \le k)

then put x in bin i

else Count := Count+1

end

return(Count)
```

2 standard methods for accessing data:

- sequential access
- random access: access via index or ID (key) for data element

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Questions

1. What can be done using only Sequential access?

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2. How can one implement Random access?

Merge Sort

procedure MergeSort(*A*, *f*, *l*):

```
{ Input: Array A with first index f and last index I }
{ Output: Sorted array, A, with same entries as input A }
```

```
if (f < l) then

m := (f + l) \text{ div } 2

MergeSort(A, f, m)

MergeSort(A, m + 1, l)

MergeArrays(A[f..m], A[m + 1..l], C)

Copy C to A
```

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```
MergeSort(A, 1, length(A));
```

Analysis of Merge Sort

Let T(n) be the maximum number of comparisons MergeSort uses if length(A)= n.

$$T(n) \leq T\left(\left\lceil \frac{n}{2} \right\rceil\right) + T\left(\left\lfloor \frac{n}{2} \right\rfloor\right) + M\left(\left\lceil \frac{n}{2} \right\rceil, \left\lfloor \frac{n}{2} \right\rfloor\right)$$

$$\leq T\left(\left\lceil \frac{n}{2} \right\rceil\right) + T\left(\left\lfloor \frac{n}{2} \right\rfloor\right) + \left(\left\lceil \frac{n}{2} \right\rceil + \left\lfloor \frac{n}{2} \right\rfloor - 1\right)$$

$$\leq T\left(\left\lceil \frac{n}{2} \right\rceil\right) + T\left(\left\lfloor \frac{n}{2} \right\rfloor\right) + n - 1$$

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 $T(n) \in \Theta(n \log n).$

Analysis of Merge Sort

$$T(n) \leq T\left(\left\lceil \frac{n}{2} \right\rceil\right) + T\left(\left\lfloor \frac{n}{2} \right\rfloor\right) + n - 1$$

Prove by induction: $T(n) \le n \log_2(n)$, if $n = 2^j$ for some integer j

Base case: n = 1. $1 \cdot \log_2(1) = 0 = T(1)$.

Induction hypothesis: For all k < n, where $k = 2^{i}$, $T(k) \le k \log_2(k)$.

Induction step (prove for *n*):

$$T(n) \leq T\left(\left\lceil \frac{n}{2} \right\rceil\right) + T\left(\left\lfloor \frac{n}{2} \right\rfloor\right) + n - 1$$

$$\leq 2T\left(\frac{n}{2}\right) + n - 1$$

$$\leq 2\frac{n}{2}\log_2\left(\frac{n}{2}\right) + n - 1$$

$$\leq n(\log_2 n - 1) + n - 1$$

$$\leq n\log_2 n$$

Analysis of Merge Sort

 $T(n) \leq n \log_2(n)$, if $n = 2^j$ for some integer j.

If $n \neq 2^j$ for any integer j, $T(n) \leq T(n')$ where n' is the next power of 2 larger than n.

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In general $T(n) \leq (2n) \log_2(2n) \leq 2n \log_2 n + 2n$. So $T(n) \in \Theta(n \log n)$. Merging more than 2 lists

Problem:

Input: 3 lists, A, B and C are sorted. Output: 1 sorted list, D, containing the entries of $A \cap B \cap C$.

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Intersecting 3 lists

Input: 3 lists, A, B and C are sorted.

Output: 1 sorted list, D, containing the entries of $A \cap B \cap C$.

Merge Step:

- Compare current records of A, B and C.
- ▶ If all the same, put record in *D*. Advance to next record in all of *A*, *B* and *C*.

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If current in A is smaller than current in either B or C, advance to next record in A. (Do same for B and C.) procedure MergeFiles(A, B, C): open(A); open(B); open(C); fA,fB,fC := false; if (isEndOfFile(A) and isEndOfFile(B)) then Stop with C empty if (not isEndOfFile(A)) then currentA := readNext(A); fA:= true; if (not isEndOfFile(B)) then currentB := readNext(B); fB := true; while (fA and fB) do if (currentA \leq currentB) then writeNext(currentA,C)

if (not isEndOfFile(A)) then currentA := readNext(A)
else fA := false

else

writeNext(currentB,*C*)

if (not isEndOfFile(B)) then currentB := readNext(B)
else fB := false

Starting with the current record in the input file which is not at EOF copy the remaining records to C close(A); close(B); close(C)

Random access API

random access: access via ID (key) for data element

Operations:

```
findElm(ID)
insertElm(ID,elementData)
deleteElm(ID)
open()
close()
```

Examples:

- dictionaries in Python
- arrays in Java with ID = index in array

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