

# Constraint Programming

Marco Kuhlmann & Guido Tack

Lecture 2

# Historical notes

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1963

Sketchpad

1978

Alice

1980

Chip

1986

CLP(R)

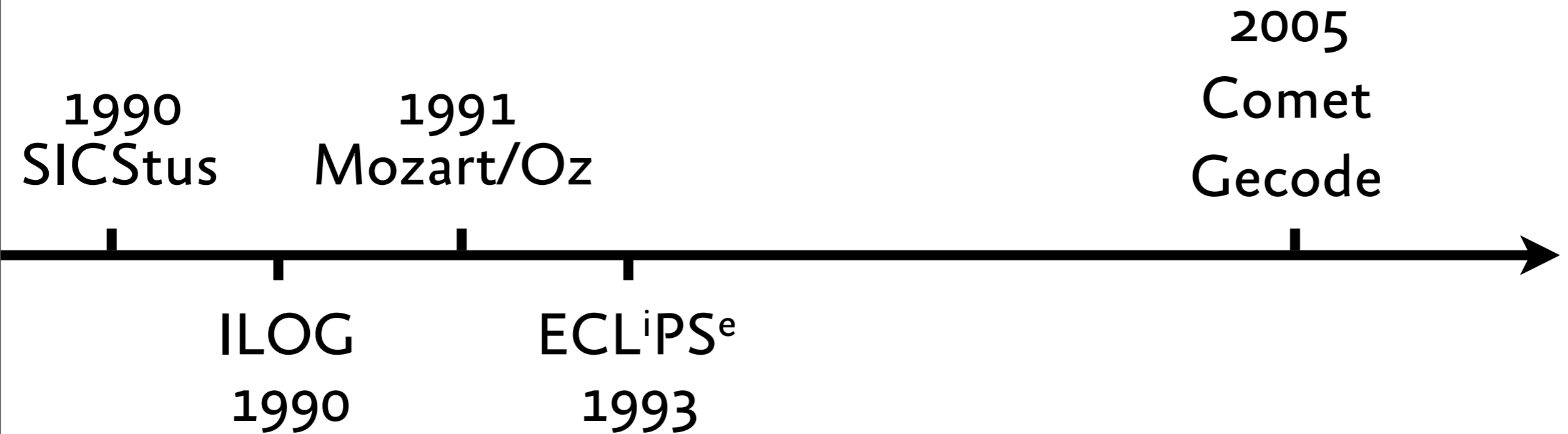
early research

constraint *logic* programming

please ignore the scale...

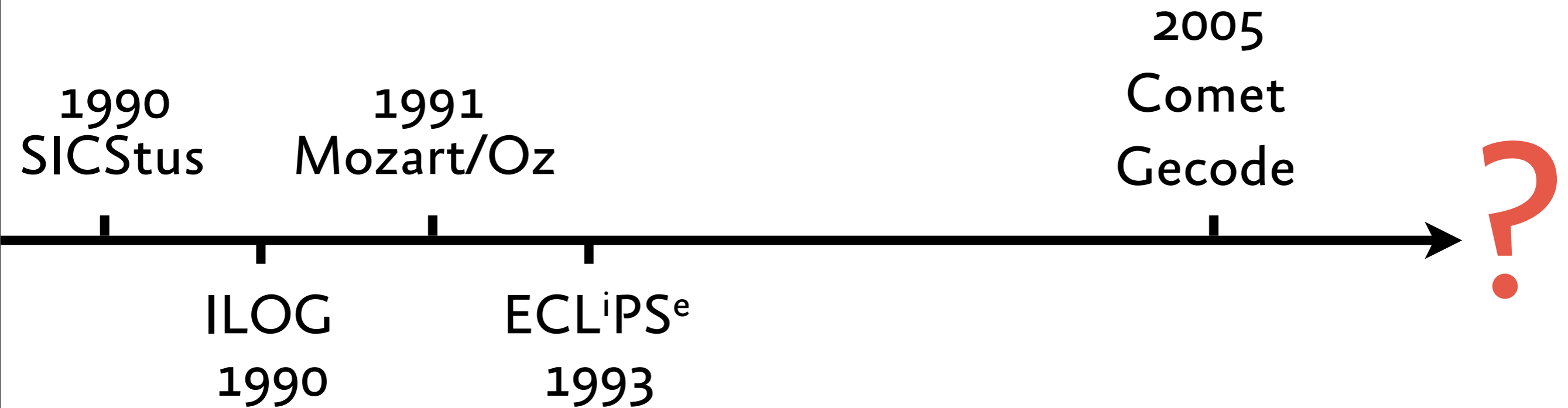
# Historical notes

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# Logic Programming

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foo(a).

foo(b).

g(X) :- X=[Y, Z], foo(Y), foo(Z).

# Logic Programming

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foo(a).

foo(b).

g(X) :- X=[Y, Z], foo(Y), foo(Z).

| ?- g(X).

X = [a, a] ? ;

X = [a, b] ? ;

X = [b, a] ? ;

X = [b, b]

# Constraint Logic Programming

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```
foo(X) :- fd_domain(X, 1, 3).  
g(Y,Z) :- foo(Y), foo(Z), Y #< Z,  
          fd_labeling([Y,Z]).
```

# Constraint Logic Programming

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```
foo(X) :- fd_domain(X, 1, 3).  
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```

```
| ?- g(X,Y).
```

```
X = 1
```

```
Y = 2 ? ;
```

```
X = 1
```

```
Y = 3 ? ;
```

```
X = 2
```

```
Y = 3
```



# Constraint Logic Programming

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**Model:**

constraint program

=

logic program

=

logical formula

# Constraint Logic Programming

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Languages/Systems:

GNU Prolog, BProlog, SICStus  
Prolog, ECLiPS<sup>e</sup>

# Concurrent Constraint Programming

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- Von-Neumann architecture: store *values*
  - operations: read and write

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  - operations: read and write
- cc architecture: store *constraints*
  - operations: ask and tell
  - communication through variables

# Concurrent Constraint Programming

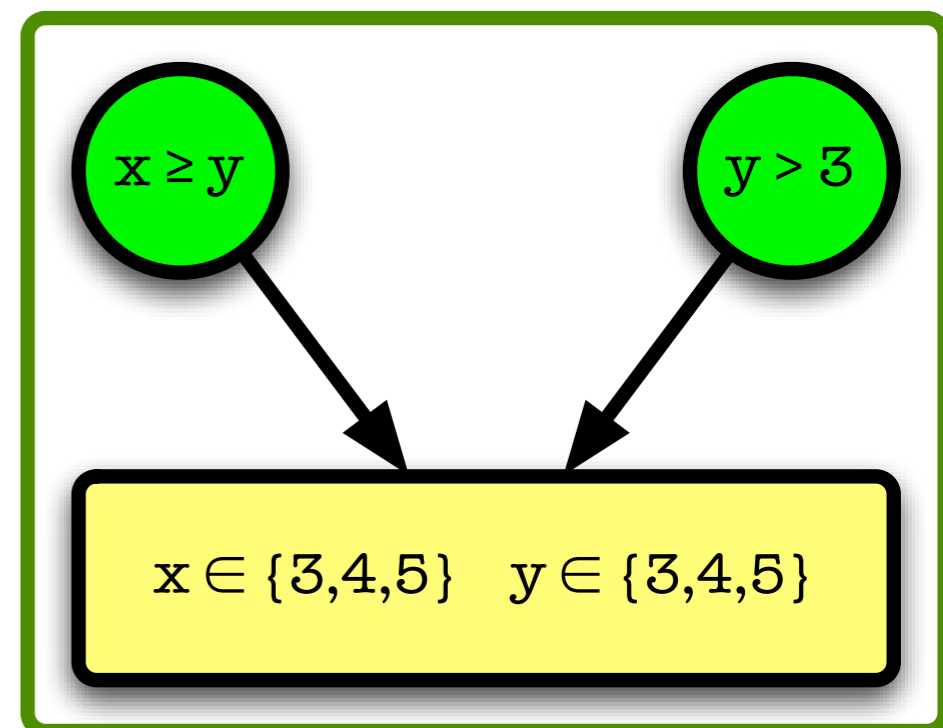
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- Languages/systems:
  - cc(FD), AKL, Mozart/Oz

# Concurrent Constraint Programming

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  - operations: read and write
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# Constraint Programming with Gecode/J

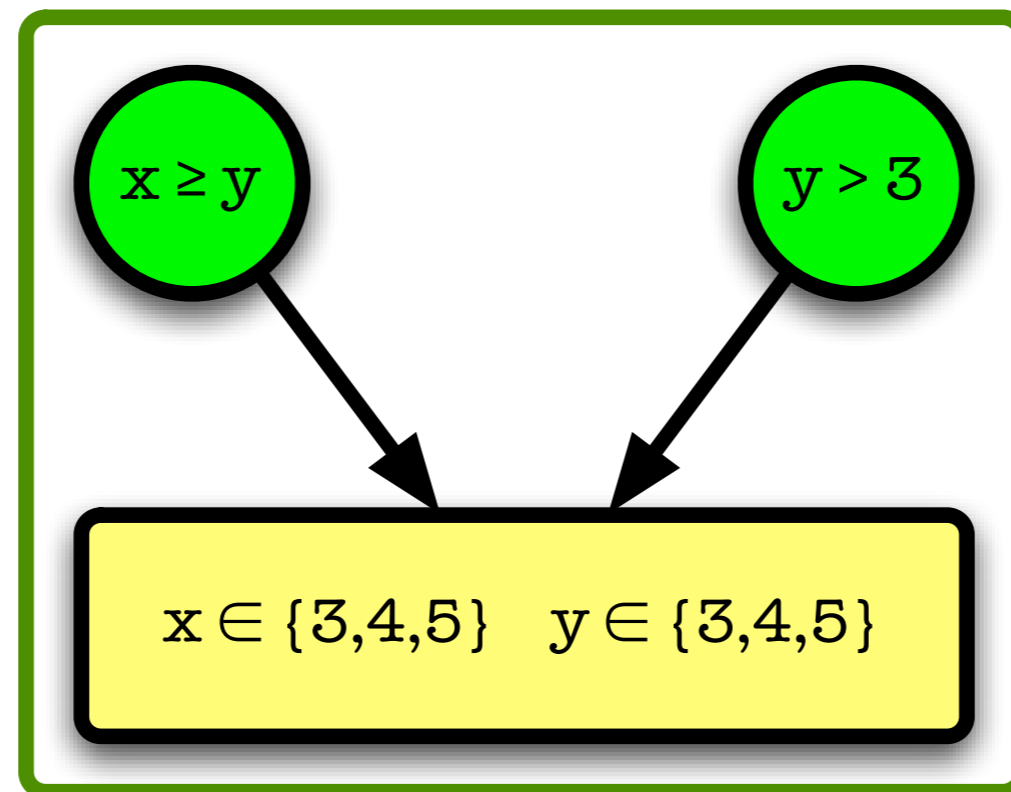
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- **Quick reminder of last lecture**
- **Walk-through for *Send More Money***
- **Some modeling techniques**
- **Presentation of first graded lab**



# Computation Space

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constraint store with connected propagators