

DM204 (5 ECTS - 1st Quarter) Scheduling, Timetabling and Routing

[Skedulering, Skemalægning og Ruteplanlægning]

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Overview

Intro phase:

Theory:

- ▶ Classification of problems in
(i) Scheduling, (ii) Timetabling and (iii) Routing
- ▶ MIP modeling: Dantzig-Wolfe decomposition, extended and compact formulations
- ▶ Solution algorithm: branch and price = branch and bound + column generation via resource constraint shortest path

Training phase:

Concrete application example bus driver scheduling of the city of Milan

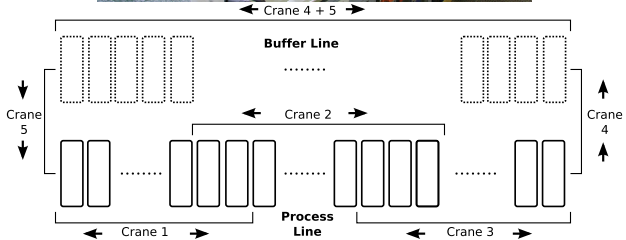
Study phase:

Implementation of solver for disruption management (AMPL & C++)

Outline

1. Problem Classification
2. Solution Approach
3. Formalities

Scheduling

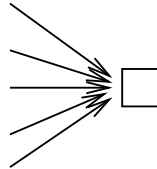


Jakob Skov, *Scheduling of an Anodizing Plant at Bang & Olufsen*.
Master Thesis, IMADA, 2007.

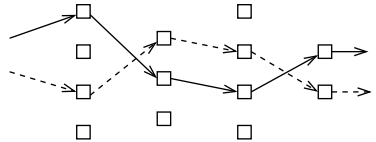
Scheduling

Allocation of scarce **resources** to **tasks** over time with the goal of optimizing some objectives

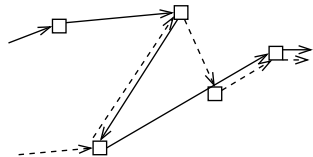
Single machine



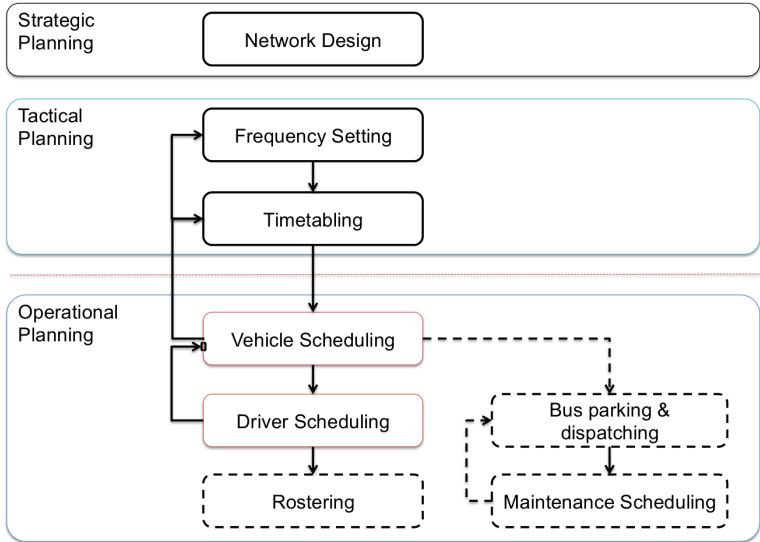
Flow shop and flexible flow shop



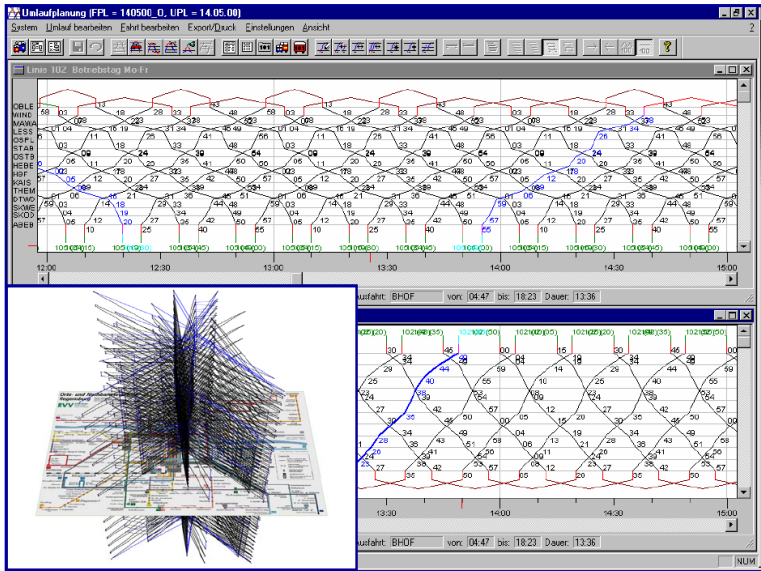
Job shop, Open shop



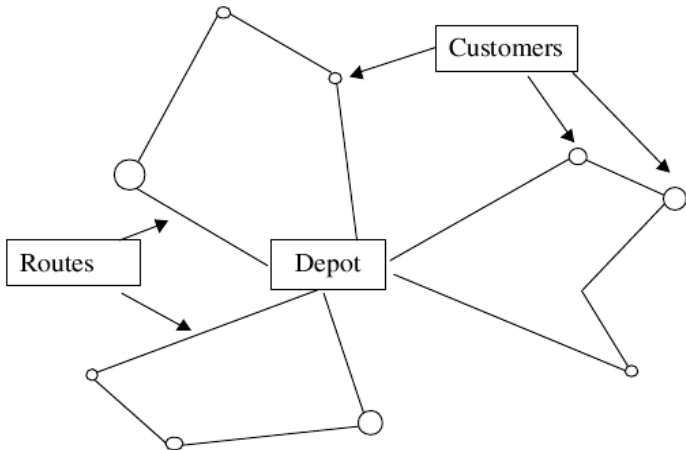
Transport Planning and Timetabling



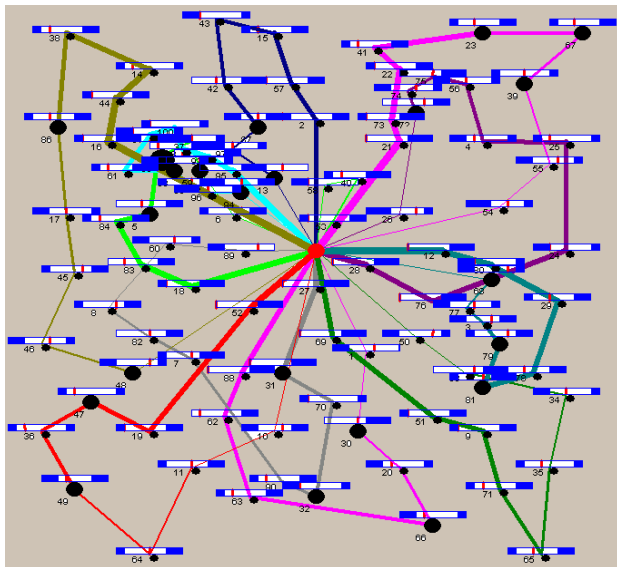
Transport Planning and Timetabling



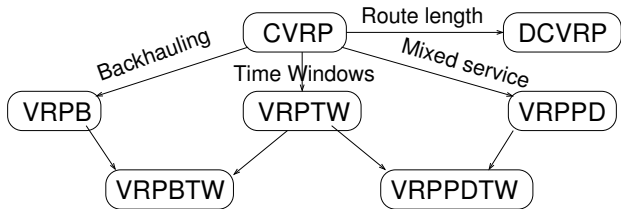
Vehicle Routing



Vehicle Routing



Vehicle Routing



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MIP Models

$$\min \sum_{k \in \mathcal{V}} \sum_{i \in \mathcal{N}} \sum_{j \in \mathcal{N}} c_{ij} x_{ijk} \text{ s.t.}, \quad (3.1)$$

$$\sum_{k \in \mathcal{V}} \sum_{j \in \mathcal{N}} x_{ijk} = 1 \quad \forall i \in \mathcal{C}, \quad (3.2)$$

$$\sum_{i \in \mathcal{C}} d_i \sum_{j \in \mathcal{N}} x_{ijk} \leq q \quad \forall k \in \mathcal{V}, \quad (3.3)$$

$$\sum_{j \in \mathcal{N}} x_{0jk} = 1 \quad \forall k \in \mathcal{V}, \quad (3.4)$$

$$\sum_{i \in \mathcal{N}} x_{ihk} - \sum_{j \in \mathcal{N}} x_{hjk} = 0 \quad \forall h \in \mathcal{C}, \forall k \in \mathcal{V}, \quad (3.5)$$

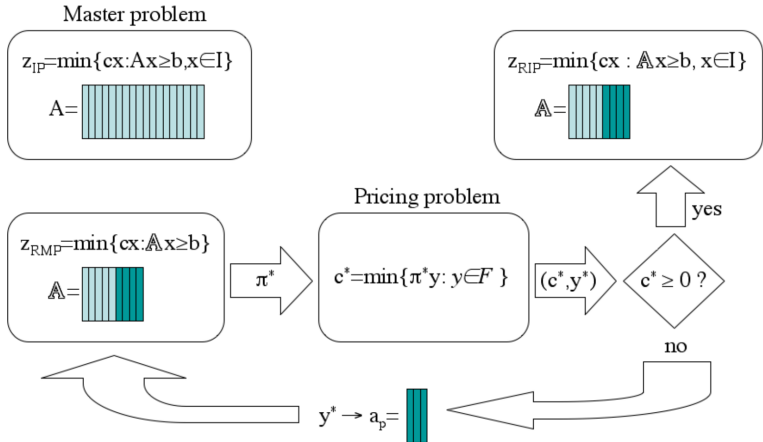
$$\sum_{i \in \mathcal{N}} x_{i,n+1,k} = 1 \quad \forall k \in \mathcal{V}, \quad (3.6)$$

$$x_{ijk}(s_{ik} + t_{ij} - s_{jk}) \leq 0 \quad \forall i, j \in \mathcal{N}, \forall k \in \mathcal{V}, \quad (3.7)$$

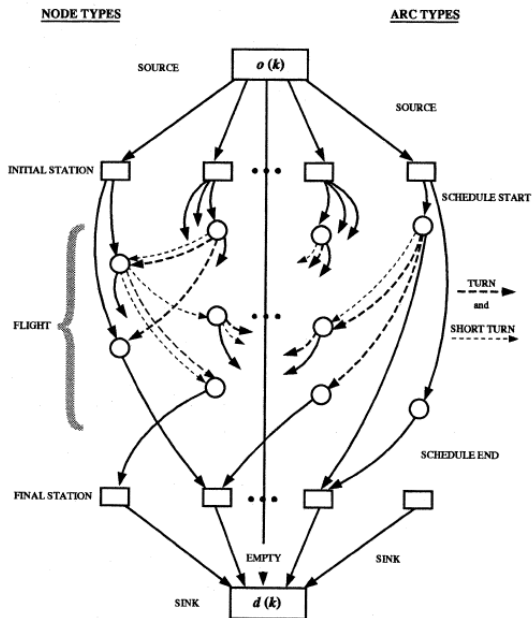
$$a_i \leq s_{ik} \leq b_i \quad \forall i \in \mathcal{N}, \forall k \in \mathcal{V}, \quad (3.8)$$

$$x_{ijk} \in \{0, 1\} \quad \forall i, j \in \mathcal{N}, \forall k \in \mathcal{V}. \quad (3.9)$$

Branch and Price



Resource Constrained Shortest Path



Bus Driver Scheduling

Outline

1. Problem Classification
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Course Formalities

Prerequisites:

- ✓ A bachelor in CS, App. Math or Mat-Øk
- ✓ DM545 - Linear and Integer Programming
 - ▶ DM811 - Heuristics and Local Search for Combinatorial Optimization

Credits: 5 ECTS

Language: English

Classes: $2h \times 8$ intro phase + $2h \times 6$ training phase
+ $10h$ study phase

Material: slides + pointers to literature + source code & data sets

Assessment

- ▶ Practical part
- ▶ Oral exam with external censor on the practical part

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“Hiring” Announcement

Master and Individual Study Activities

- ▶ Course/Exam timetabling at NAT-SDU
- ▶ Graph coloring problems
- ▶ Crew scheduling (AirSupport)
- ▶ Aircraft routing (AirSupport)
- ▶ Vehicle routing (CargoMatch)
- ▶ Distribution of virtualization clusters on the physical infrastructure (APC Schneider Electric)
- ▶ ROADEF 2014 competition (FNRS train management)
- ▶ Local search framework