DM545/DM871 – Linear and Integer Programming

Exercise 1

Consider the matrices:

$$A = \begin{bmatrix} 2 & 0 \\ -4 & 6 \end{bmatrix} \quad B = \begin{bmatrix} 1 & -7 & 2 \\ 5 & 3 & 0 \end{bmatrix} \quad C = \begin{bmatrix} 4 & 9 \\ -3 & 0 \\ 2 & 1 \end{bmatrix}$$
$$D = \begin{bmatrix} -2 & 1 & 8 \\ 3 & 0 & 2 \\ 4 & -6 & 3 \end{bmatrix} \quad E = \begin{bmatrix} 0 & 3 & 0 \\ -5 & 1 & 1 \\ 7 & 6 & 2 \end{bmatrix}$$

In each part compute the given expression. Where the computation is not possible explain why.

- 1. D + E
- 2. *D* − *E*
- 3. 5A
- 4. 2B C
- 5. 2(D + 5E)
- 6. $(C^T B) A^T$
- 7. 2tr(AB)
- 8. det(*E*)

Exercise 2

Consider the following system of linear equations in the variables $x, y, z \in \mathbb{R}$.

$$-2y + 3z = 3$$
$$3x + 6y - 3z = -2$$
$$-3x - 8y + 6z = 5$$

- 1. Write the augmented matrix of this system.
- 2. Reduce this matrix to row echelon form by performing a sequence of elementary row operations.
- 3. Solve the system and write its general solution in parametric form.

Exercise 3

Consider the following matrix

	1	0	1]
M =	-1	1	0	.
	2	2	2	

- 1. Find M^{-1} by performing row operations on the matrix $[M \mid I]$.
- 2. Is it possible to express *M* as a product of elementary matrices? Explain why or why not.

Exercise 4

- 1. Given the point [3, 2] and the vector [-1, 0] find the vector and parametric (Cartesian) equation of the line containing the point and parallel to the vector.
- 2. Find the vector and parametric (Cartesian) equations of the plane in \mathbb{R}^3 that passes through the origin and is orthogonal to $\mathbf{v} = [3, -1, -6]$.