## DM545/DM871 - Linear and Integer Programming

## Exercise 1

Consider the matrices:

$$
\begin{gathered}
A=\left[\begin{array}{cc}
2 & 0 \\
-4 & 6
\end{array}\right] \quad B=\left[\begin{array}{ccc}
1 & -7 & 2 \\
5 & 3 & 0
\end{array}\right] \quad C=\left[\begin{array}{cc}
4 & 9 \\
-3 & 0 \\
2 & 1
\end{array}\right] \\
D=\left[\begin{array}{ccc}
-2 & 1 & 8 \\
3 & 0 & 2 \\
4 & -6 & 3
\end{array}\right] \quad E=\left[\begin{array}{ccc}
0 & 3 & 0 \\
-5 & 1 & 1 \\
7 & 6 & 2
\end{array}\right]
\end{gathered}
$$

In each part compute the given expression. Where the computation is not possible explain why.

1. $D+E$
2. $D-E$
3. $5 A$
4. $2 B-C$
5. $2(D+5 E)$
6. $\left(C^{T} B\right) A^{T}$
7. $2 \operatorname{tr}(A B)$
8. $\operatorname{det}(E)$

## Exercise 2

Consider the following system of linear equations in the variables $x, y, z \in \mathbb{R}$.

$$
\begin{aligned}
-2 y+3 z & =3 \\
3 x+6 y-3 z & =-2 \\
-3 x-8 y+6 z & =5
\end{aligned}
$$

1. Write the augmented matrix of this system.
2. Reduce this matrix to row echelon form by performing a sequence of elementary row operations.
3. Solve the system and write its general solution in parametric form.

## Exercise 3

Consider the following matrix

$$
M=\left[\begin{array}{ccc}
1 & 0 & 1 \\
-1 & 1 & 0 \\
2 & 2 & 2
\end{array}\right]
$$

1. Find $M^{-1}$ by performing row operations on the matrix $[M \mid I]$.
2. Is it possible to express $M$ as a product of elementary matrices? Explain why or why not.

## Exercise 4

1. Given the point $[3,2]$ and the vector $[-1,0]$ find the vector and parametric (Cartesian) equation of the line containing the point and parallel to the vector.
2. Find the vector and parametric (Cartesian) equations of the plane in $\mathbb{R}^{3}$ that passes through the origin and is orthogonal to $v=[3,-1,-6]$.
