

# **DMP204 (10 ECTS - 3rd & 4th Quarter)**

# **Scheduling, Timetabling and Routing**

## **Skedulering, Skemalægning og Ruteplanlægning**

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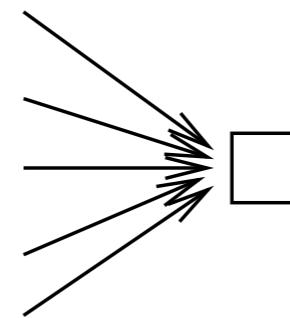
# Scheduling

Allocation of scarce **resources** to **tasks** over time with the goal of optimizing some objectives

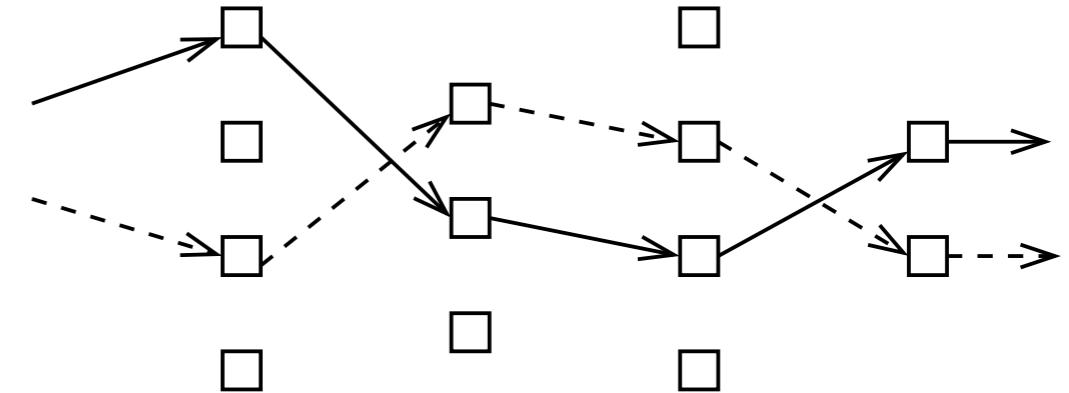
# Scheduling

Allocation of scarce **resources** to **tasks** over time with the goal of optimizing some objectives

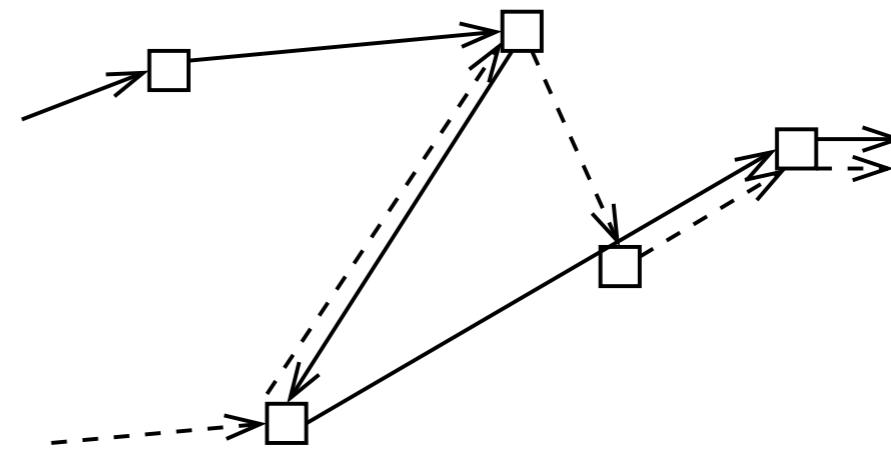
Single machine



Flow shop and  
flexible flow shop



Job shop,  
Open shop



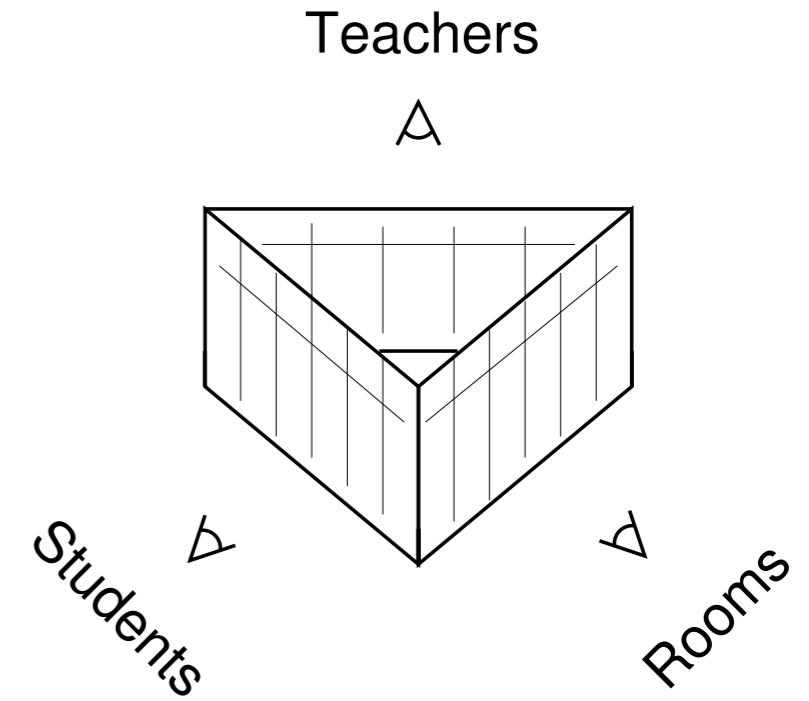
# Timetabling

## University course timetabling

Elective Courses at IMADA – First Quarter – Seminarrum					
	Monday	Tuesday	Wednesday	Thursday	Friday
8:00-10:00	DM818 <i>(Daniel Merkle)</i>	DM811 <i>(Marco Chiarandini)</i>	DM819 <i>(Kim Skak Larsen)</i>		
10:00-12:00	DM207 <i>(Rolf Fagerberg)</i>	DM819 <i>(Kim Skak Larsen)</i>	DM811 <i>(Marco Chiarandini)</i>	DM207 <i>(Rolf Fagerberg)</i>	
12:00-14:00	MM802 <i>(Niels Jørgen Nielsen)</i>		MM802 <i>(Niels Jørgen Nielsen)</i>		
14:00-16:00		COLLOQUIUM		COLLOQUIUM	MM804 <i>(Martin Svensson)</i>
16:00-18:00	MM804 <i>(Martin Svensson)</i>		MM804 <i>(Martin Svensson)</i>	DM818 <i>(Daniel Merkle)</i>	

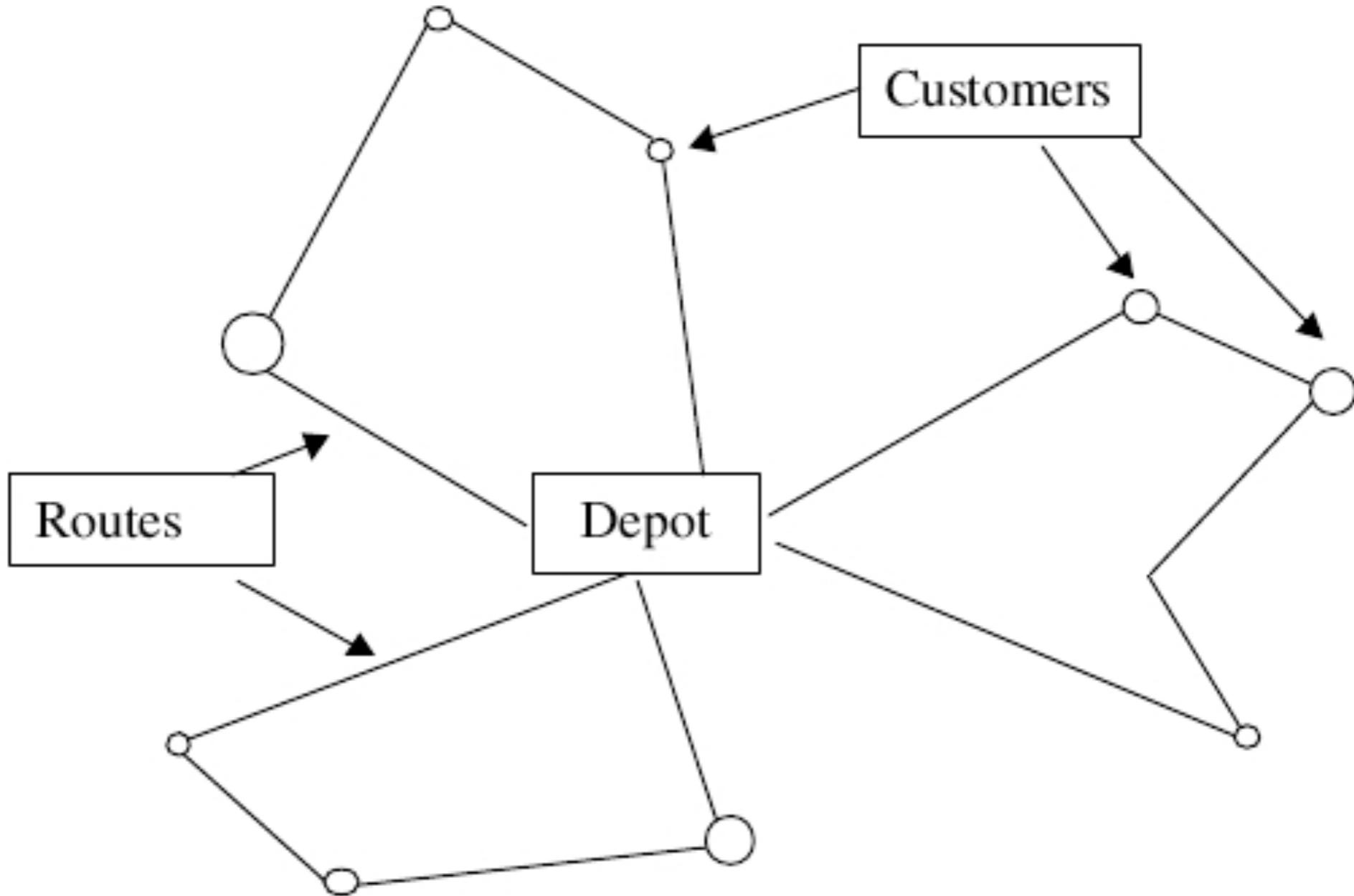
# Timetabling

## University course timetabling



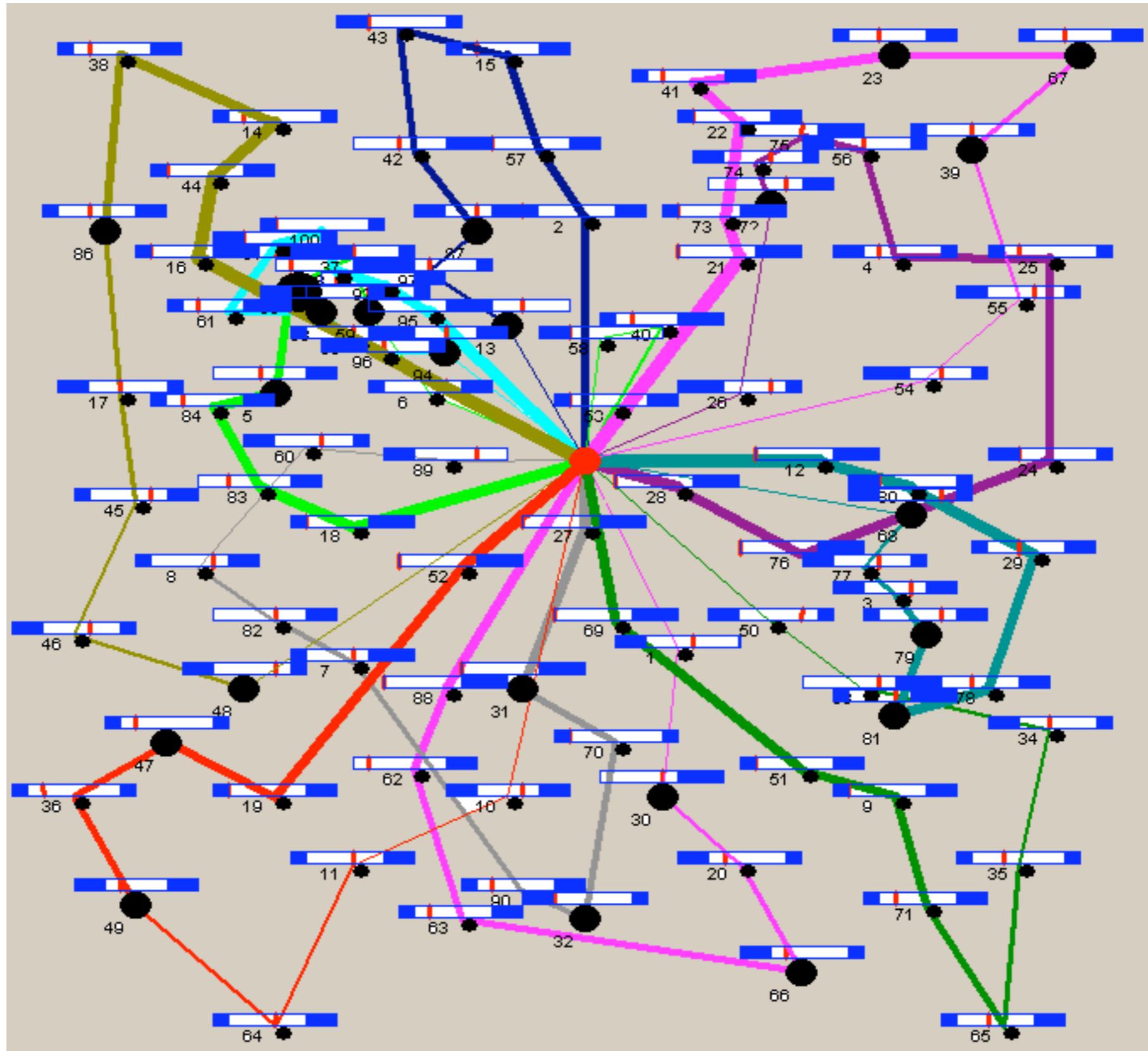
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# Vehicle Routing



# DM204 Scheduling, Timetabling and Routing - L0

# Vehicle Routing



# Methodology

- ▶ Mathematical Programming
- ▶ Constraint Programming
- ▶ Graph Models and Algorithms
- ▶ Heuristics

# Mixed Integer Programming for Routing

$$\min \sum_{k \in \mathcal{V}} \sum_{i \in \mathcal{N}} \sum_{j \in \mathcal{N}} c_{ij} x_{ijk} \text{ s.t.,} \quad (3.1)$$

$$\sum_{k \in \mathcal{V}} \sum_{j \in \mathcal{N}} x_{ijk} = 1 \quad \forall i \in \mathcal{C}, \quad (3.2)$$

$$\sum_{i \in \mathcal{C}} d_i \sum_{j \in \mathcal{N}} x_{ijk} \leq q \quad \forall k \in \mathcal{V}, \quad (3.3)$$

$$\sum_{j \in \mathcal{N}} x_{0jk} = 1 \quad \forall k \in \mathcal{V}, \quad (3.4)$$

$$\sum_{i \in \mathcal{N}} x_{ihk} - \sum_{j \in \mathcal{N}} x_{hjk} = 0 \quad \forall h \in \mathcal{C}, \forall k \in \mathcal{V}, \quad (3.5)$$

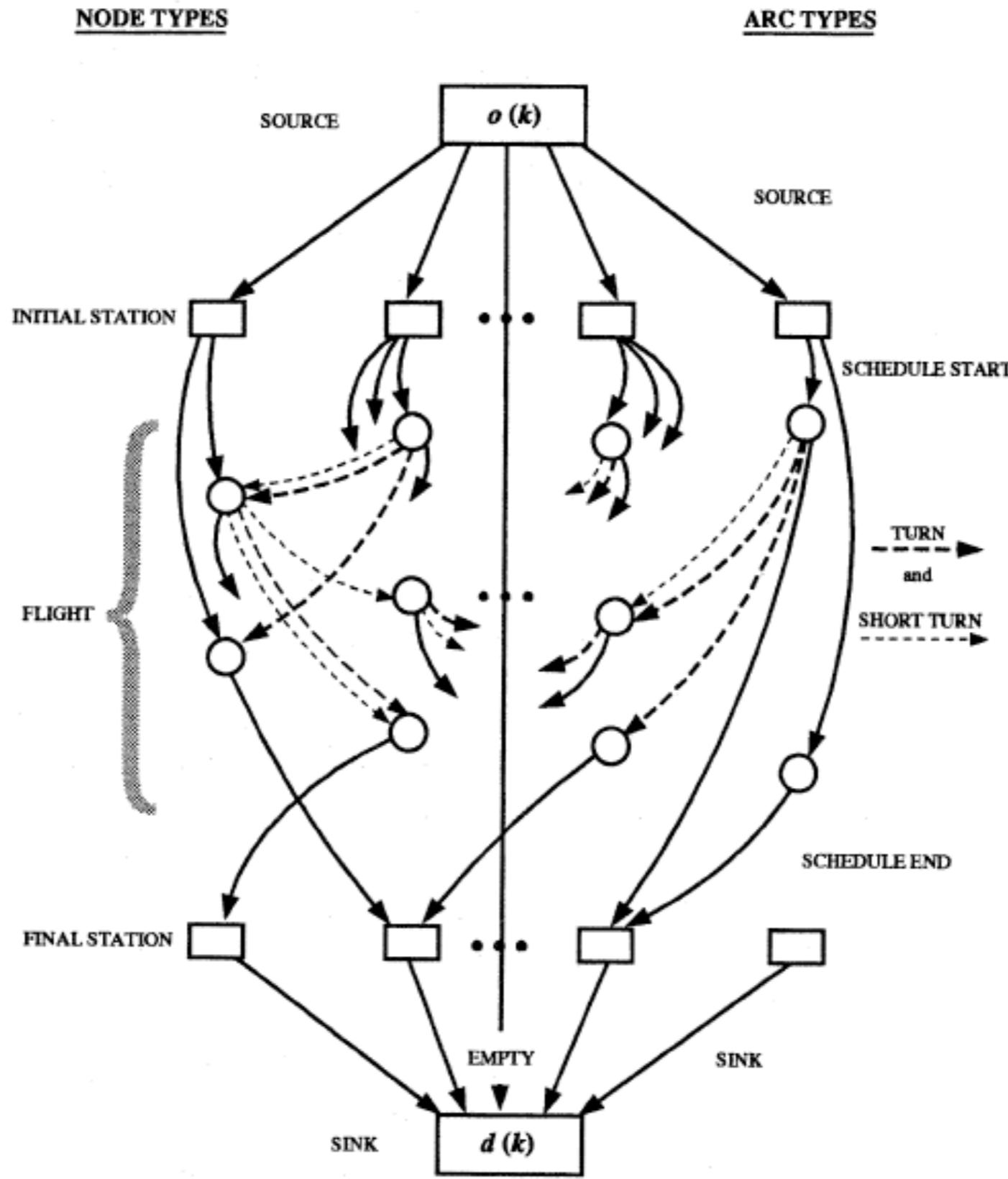
$$\sum_{i \in \mathcal{N}} x_{i,n+1,k} = 1 \quad \forall k \in \mathcal{V}, \quad (3.6)$$

$$x_{ijk}(s_{ik} + t_{ij} - s_{jk}) \leq 0 \quad \forall i, j \in \mathcal{N}, \forall k \in \mathcal{V}, \quad (3.7)$$

$$a_i \leq s_{ik} \leq b_i \quad \forall i \in \mathcal{N}, \forall k \in \mathcal{V}, \quad (3.8)$$

$$x_{ijk} \in \{0, 1\} \quad \forall i, j \in \mathcal{N}, \forall k \in \mathcal{V}. \quad (3.9)$$

# Graph Algorithms



# Constraint Programming for Scheduling

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```
range Cars = 1..100;
range Configs = 1..18;
range Options = 1..5;
int lb[Options] = [1,2,1,2,1];
int ub[Options] = [2,3,3,5,5];
int demand[Configs] = [5,3,7,1,10,2,11,5,4,6,12,1,1,5,9,5,12,1];
int requires[Configs,Options] = [[1,1,0,0,1],[1,1,0,1,0],..., [0,0,1,0,0]];
set{int} options[o in Options] = filter(c in Configs)(requires[c,o]==1);

import cotfd;
Solver<CP> cp();
var<CP>{int} line[Cars](cp,Configs);
solve<cp> {
    forall(o in Options)
        cp.post(sequence(line,demand,lb[o],ub[o],options[o]));
} using {
    labelFF(line);
}
cout << "#choices = " << cp.getNChoice() << endl;
cout << "#fail  = " << cp.getNFail() << endl;
```

**Statement 11.4:** COMET model for the car sequencing problem (implemented in `carsequencing-cp.co`)

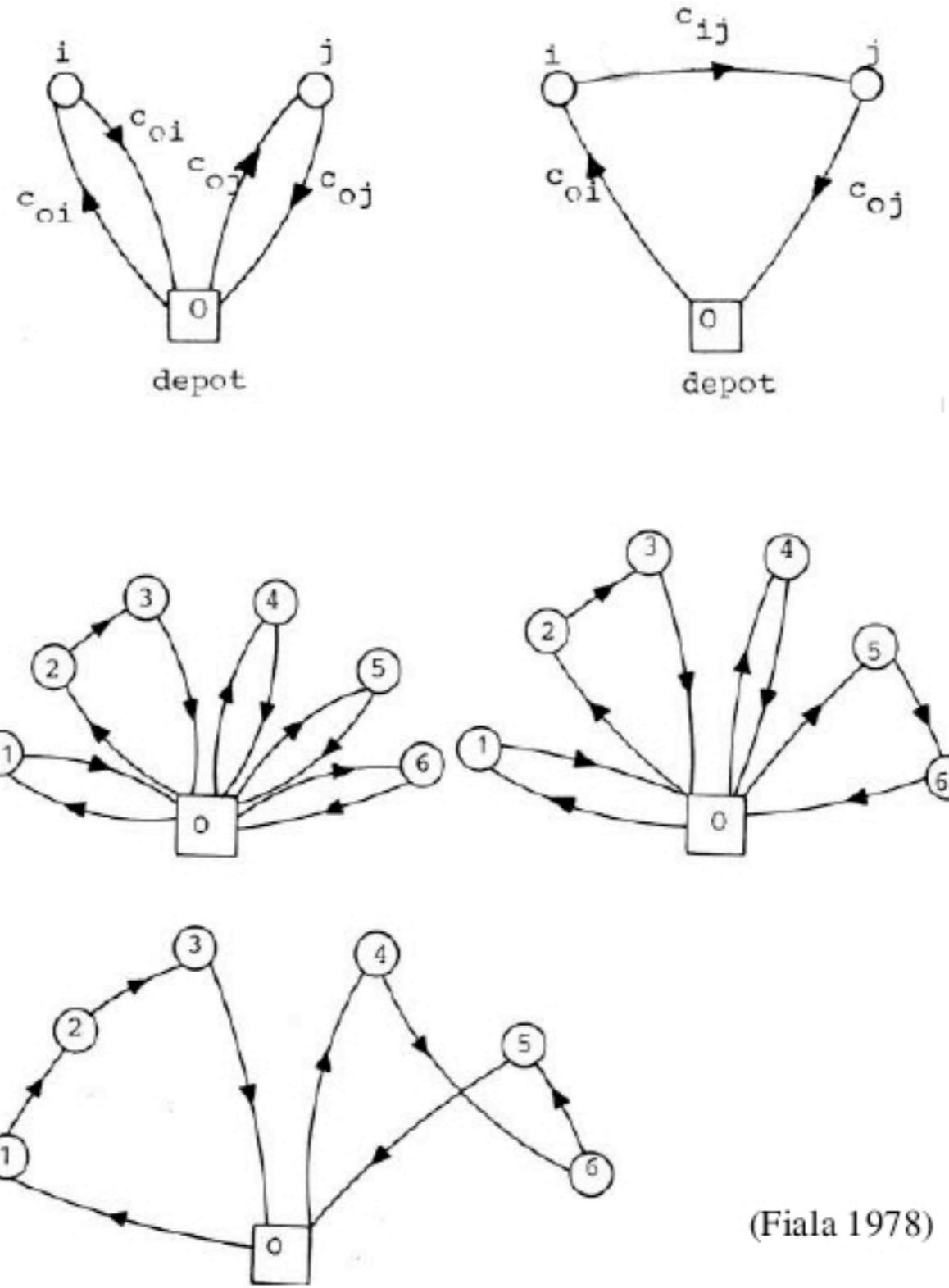
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# Heuristics for Routing

## Sweeping heuristic



# Heuristics for Routing



# Aims of the course

You will learn to:

- ▶ recognize abstract models from real-life applications
- ▶ assess which solution method is most appropriate
- ▶ implement the solution methods
- ▶ analyze empirically the results produced
- ▶ describe with appropriate language

# Prerequisites

- ▶ A bachelor in CS, Math or Mat-Øk (possibly)
- ▶ DM515: Introduction to Linear and Integer Programming  
(would be nice having)
- ▶ DM811 Heuristics for Optimization  
(content should be known)

# Course Work Load

- ▶ 28 lectures, 4 hours per week
- ▶ Read articles
- ▶ Learn to program in COMET 
- ▶ Weekly assignments
- ▶ In the 4th quarter project assignment

# Final Assessment (10 ECTS)

- ▶ Project assignment.  
Grade in 7 mark scale system.  
40% of final grade.
  
- ▶ Oral exam with external examiner.  
Duration: 30 min.  
Grade in 7 mark scale.  
60% of final grade.

Single combined grade.

# Course Material

- ▶ Text books
  - Pinedo, M. *Planning and Scheduling in Manufacturing and Services* Springer Verlag, 2005
  - Pinedo, M. *Scheduling: Theory, Algorithms, and Systems* Springer New York, 2008
  - Toth, P. & Vigo, D. (ed.) *The Vehicle Routing Problem* SIAM Monographs on Discrete Mathematics and Applications, 2002
- ▶ Literature (articles, photocopies)
- ▶ Slides
- ▶ Source code and data sets
- ▶ [www.imada.sdu.dk/~marco/DM204](http://www.imada.sdu.dk/~marco/DM204)

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