



DM502

Programming A

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<http://imada.sdu.dk/~petersk/DM502/>

TURTLE WORLD & INTERFACE DESIGN

Turtle World

- available from
 - <http://imada.sdu.dk/~petersk/DM502/lit/swampy-2.0.zip>
- check for Tkinter (install if not available)
 - `python -c "import Tkinter"`
- unpack using `unzip swampy-2.0.zip`
- go to subdirectory `swampy-2.0/python2`
- basic elements of the library
 - can be imported using `from TurtleWorld import *`
 - `w = TurtleWorld()` creates new world `w`
 - `t = Turtle()` creates new turtle `t`
 - `wait_for_user()` can be used at the end of the program

Simple Repetition

- two basic commands to the turtle
 - `fd(t, 100)` advances turtle `t` by 100
 - `lt(t)` turns turtle `t` 90 degrees to the left
- drawing a square requires 4x drawing a line and turning left
 - `fd(t, 100); lt(t); fd(t, 100); lt(t); fd(t, 100); lt(t); fd(t, 100); lt(t)`
- simple repetition using for-loop `for <var> in range(<expr>):`
`<instr1>; <instr2>`
- Example:
`for i in range(4):`
`fd(t, 100)`
`lt(t)`

Encapsulation

- **Idea:** wrap up a block of code in a function
 - documents use of this block of code
 - allows reuse of code by using parameters

- Example:

```
def square(t):  
    for i in range(4):  
        fd(t, 100)  
        lt(t)  
square(t)  
u = Turtle(); rt(u); fd(u, 10); lt(u);  
square(u)
```

Generalization

- `square(t)` can be reused, but size of square is fixed
- **Idea:** generalize function by adding parameters
 - more flexible functionality
 - more possibilities for reuse

- Example 1:

```
def square(t, length):  
    for i in range(4):  
        fd(t, length)  
        lt(t)  
square(t, 100)  
square(t, 50)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def square(t, length):  
    for i in range(4):  
        fd(t, length)  
        lt(t)
```


Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, length):  
    for i in range(4):  
        fd(t, length)  
        lt(t)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):
```

```
    for i in range(n):
```

```
        fd(t, length)
```

```
        lt(t)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):
```

```
    for i in range(n):
```

```
        fd(t, length)
```

```
        lt(t, 360/n)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):
```

```
    angle = 360/n
```

```
    for i in range(n):
```

```
        fd(t, length)
```

```
        lt(t, angle)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):
```

```
    angle = 360/n
```

```
    for i in range(n):
```

```
        fd(t, length)
```

```
        lt(t, angle)
```

```
polygon(t, 4, 100)
```

```
polygon(t, 6, 50)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):  
    angle = 360/n  
    for i in range(n):  
        fd(t, length)  
        lt(t, angle)  
polygon(t, n=4, length=100)  
polygon(t, n=6, length=50)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):
```

```
    angle = 360/n
```

```
    for i in range(n):
```

```
        fd(t, length)
```

```
        lt(t, angle)
```

```
square(t, 100)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):
```

```
    angle = 360/n
```

```
    for i in range(n):
```

```
        fd(t, length)
```

```
        lt(t, angle)
```

```
def square(t, length):
```

```
    polygon(t, 4, length)
```

```
square(t, 100)
```


Interface Design

- **Idea:** interface = parameters + semantics + return value
- should be general (= easy to reuse)
- but as simple as possible (= easy to read and debug)
- Example:

```
def circle(t, r):
```

```
    circumference = 2*math.pi*r
```

```
    n = 10
```

```
    length = circumference / n
```

```
    polygon(t, n, length)
```

```
circle(t, 10)
```

```
circle(t, 100)
```

Interface Design

- **Idea:** interface = parameters + semantics + return value
- should be general (= easy to reuse)
- but as simple as possible (= easy to read and debug)

- Example:

```
def circle(t, r, n):  
    circumference = 2*math.pi*r  
#    n = 10  
    length = circumference / n  
    polygon(t, n, length)  
circle(t, 10, 10)  
circle(t, 100, 40)
```

Interface Design

- **Idea:** interface = parameters + semantics + return value
- should be general (= easy to reuse)
- but as simple as possible (= easy to read and debug)
- Example:

```
def circle(t, r):
```

```
    circumference = 2*math.pi*r
```

```
    n = int(circumference / 3) + 1
```

```
    length = circumference / n
```

```
    polygon(t, n, length)
```

```
circle(t, 10)
```

```
circle(t, 100)
```

Refactoring

- we want to be able to draw arcs
- Example:

```
def arc(t, r, angle):  
    arc_length = 2*math.pi*r*angle/360  
    n = int(arc_length / 3) + 1  
    step_length = arc_length / n  
    step_angle = float(angle) / n
```

```
for i in range(n):  
    fd(t, step_length)  
    lt(t, step_angle)
```

Refactoring

- we want to be able to draw arcs
- Example:

```
def arc(t, r, angle):  
    arc_length = 2*math.pi*r*angle/360  
    n = int(arc_length / 3) + 1  
    step_length = arc_length / n  
    step_angle = float(angle) / n
```

```
def polyline(t, n, length, angle):  
    for i in range(n):  
        fd(t, length)  
        lt(t, angle)
```

Refactoring

- we want to be able to draw arcs
- Example:

```
def arc(t, r, angle):  
    arc_length = 2*math.pi*r*angle/360  
    n = int(arc_length / 3) + 1  
    step_length = arc_length / n  
    step_angle = float(angle) / n  
    polyline(t, n, step_length, step_angle)  
def polyline(t, n, length, angle):  
    for i in range(n):  
        fd(t, length)  
        lt(t, angle)
```

Refactoring

- we want to be able to draw arcs
- Example:

```
def polyline(t, n, length, angle):  
    for i in range(n):  
        fd(t, length)  
        lt(t, angle)
```

Refactoring

- we want to be able to draw arcs
- Example:

```
def polyline(t, n, length, angle):
```

```
    for i in range(n):
```

```
        fd(t, length)
```

```
        lt(t, angle)
```

```
def polygon(t, n, length):
```

```
    angle = 360/n
```

```
    polyline(t, n, length, angle):
```


Refactoring

- we want to be able to draw arcs
- Example:

```
def arc(t, r, angle):  
    arc_length = 2*math.pi*r*angle/360  
    n = int(arc_length / 3) + 1  
    step_length = arc_length / n  
    step_angle = float(angle) / n  
    polyline(t, n, step_length, step_angle)
```

Refactoring

- we want to be able to draw arcs
- Example:

```
def arc(t, r, angle):  
    arc_length = 2*math.pi*r*angle/360  
    n = int(arc_length / 3) + 1  
    step_length = arc_length / n  
    step_angle = float(angle) / n  
    polyline(t, n, step_length, step_angle)  
def circle(t, r):  
    arc(t, r, 360)
```

Simple Iterative Development

- first structured approach to develop programs:
 1. write small program without functions
 2. encapsulate code in functions
 3. generalize functions (by adding parameters)
 4. repeat steps 1–3 until functions work
 5. refactor program (e.g. by finding similar code)
- copy & paste helpful
 - reduces amount of typing
 - no need to debug same code twice

Debugging Interfaces

- interfaces simplify testing and debugging
- 1. test if pre-conditions are given:
 - do the arguments have the right type?
 - are the values of the arguments ok?
- 2. test if the post-conditions are given:
 - does the return value have the right type?
 - is the return value computed correctly?
- 3. debug function, if pre- or post-conditions violated

CONDITIONAL EXECUTION

Boolean Expressions

- expressions whose value is either **True** or **False**
- logic operators for computing with Boolean values:
 - **x and y** **True** if, and only if, **x** is **True** and **y** is **True**
 - **x or y** **True** if (**x** is **True** or **y** is **True**)
 - **not x** **True** if, and only if, **x** is **False**
- Python also treats numbers as Boolean expressions:
 - **0** **False**
 - any other number **True**
 - Please, do **NOT** use this feature!

Relational Operators

- relational operators are operators, whose value is Boolean

- important relational operators are:

	Example True	Example False
▪ $x < y$	$23 < 42$	<code>"World" < "Hej!"</code>
▪ $x \leq y$	$42 \leq 42.0$	<code>int(math.pi) <= 2</code>
▪ $x == y$	$42 == 42.0$	<code>type(2) == type(2.0)</code>
▪ $x \geq y$	$42 \geq 42$	<code>"Hej!" >= "Hello"</code>
▪ $x > y$	<code>"World" > "Hej!"</code>	$42 > 42$

- remember to use “==” instead of “=” (assignment)!

Conditional Execution

- the if-then statement executes code only if a condition holds
- grammar rule:

`<if-then>` \Rightarrow `if <cond>:`
 `<instr1>; ...; <instrk>`

- Example:

```
if x <= 42:
    print "not more than the answer"
if x > 42:
    print "sorry - too much!"
```


Control Flow Graph

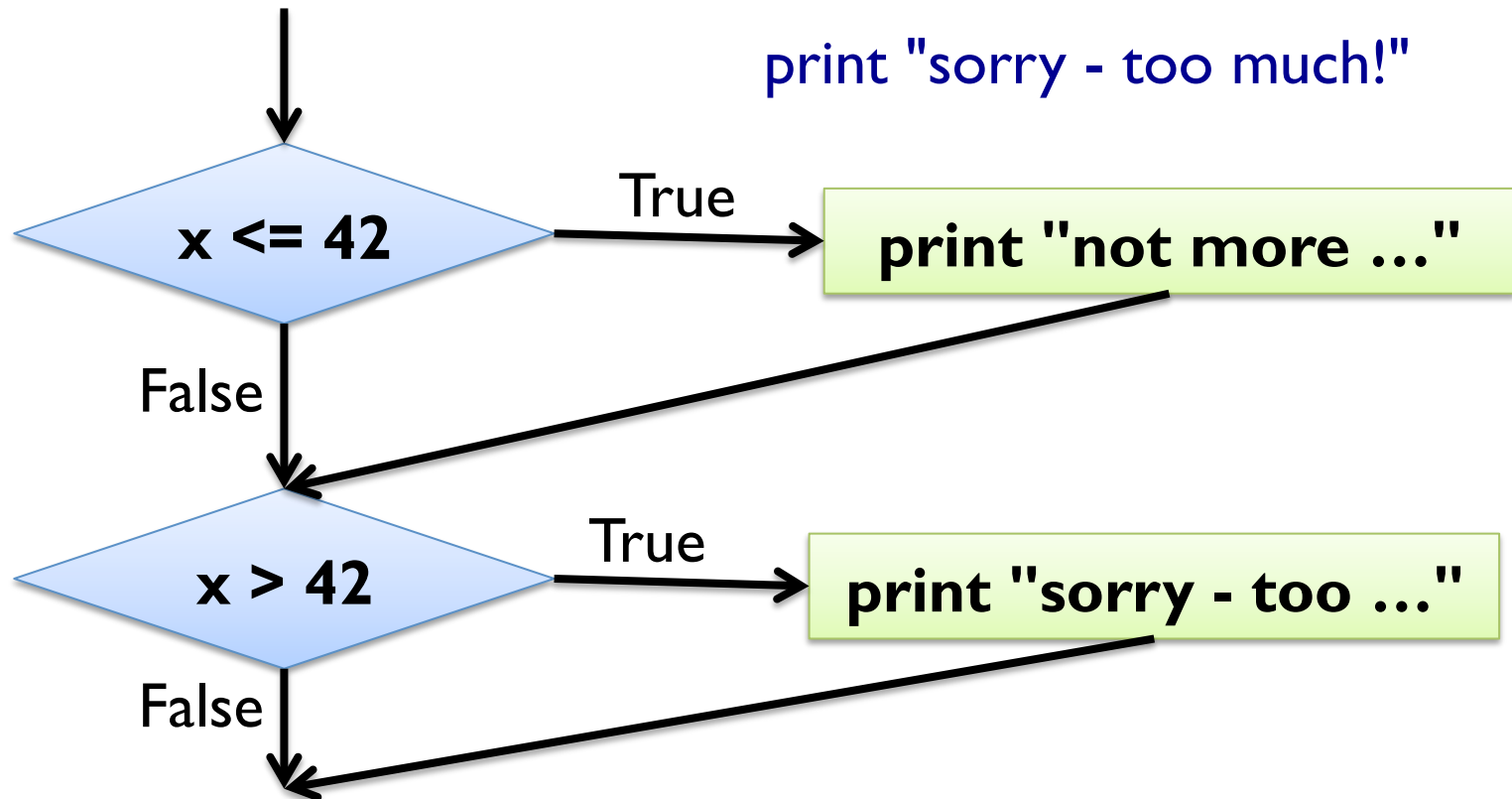
- Example:

if $x \leq 42$:

print "not more than the answer"

if $x > 42$:

print "sorry - too much!"



Alternative Execution

- the if-then-else statement executes one of two code blocks
- grammar rule:

```
<if-then-else> => if <cond>:  
    <instr1>; ...; <instrk>  
else:  
    <instr'1>; ...; <instr'k>
```

- Example:
if $x \leq 42$:
 print "not more than the answer"
else:
 print "sorry - too much!"

Control Flow Graph

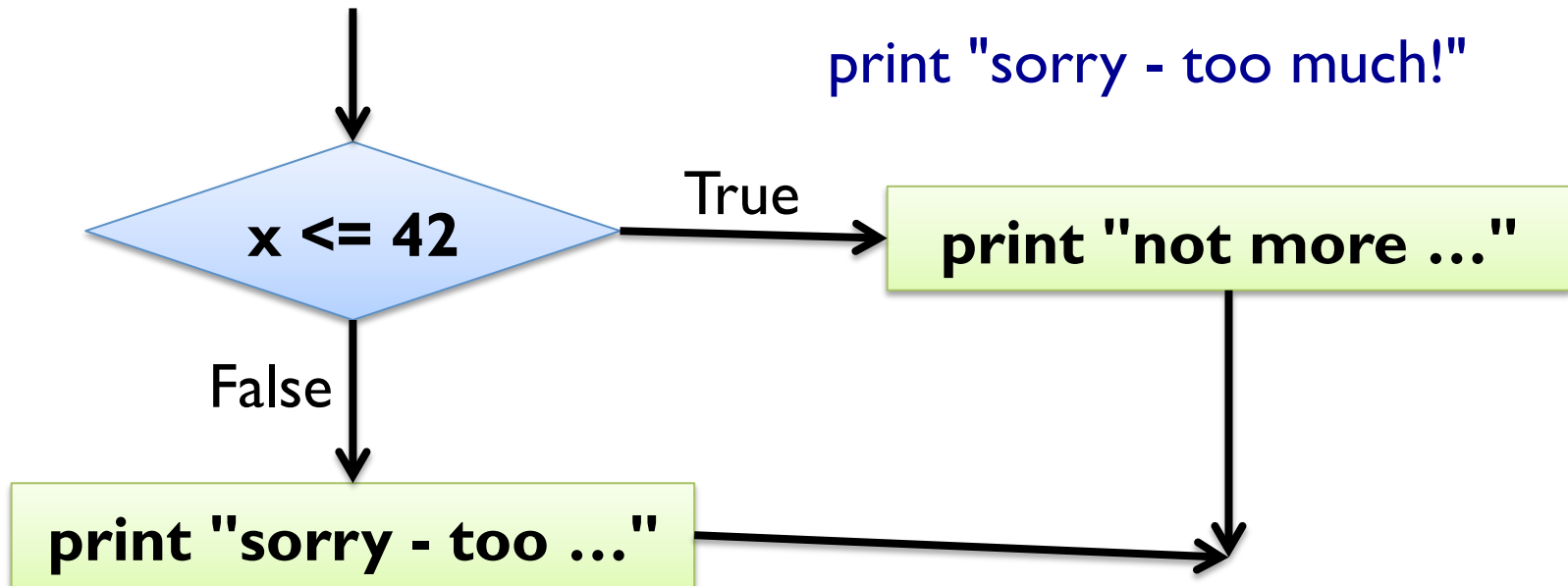
- Example:

if $x \leq 42$:

print "not more than the answer"

else:

print "sorry - too much!"



Chained Conditionals

- alternative execution a special case of chained conditionals
- grammar rules:

```
<if-chained>    =>  if <cond1>:  
                   <instr1,1>; ...; <instrk1,1>  
                   elif <cond2>:  
                   ...  
                   else:  
                   <instr1,m>; ...; <instrkm,m>
```

- Example: if x > 0: print "positive"
 elif x < 0: print "negative"
 else: print "zero"

Control Flow Diagram

- Example:

if $x > 0$:

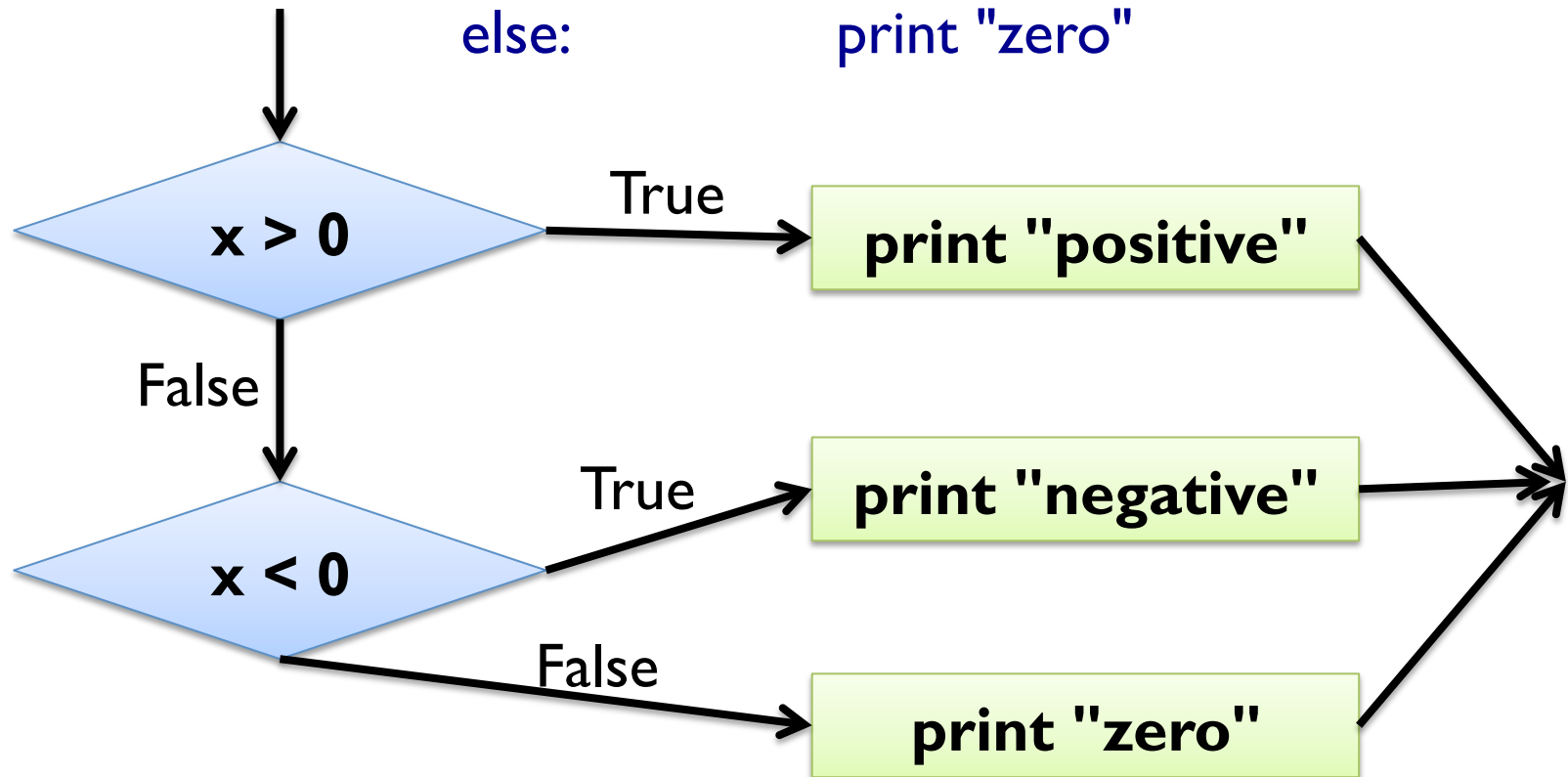
print "positive"

elif $x < 0$:

print "negative"

else:

print "zero"



Nested Conditionals

- conditionals can be nested below conditionals:

```
x = input()
```

```
y = input()
```

```
if x > 0:
```

```
    if y > 0:        print "Quadrant 1"
```

```
    elif y < 0:     print "Quadrant 4"
```

```
    else:           print "positive x-Axis"
```

```
elif x < 0:
```

```
    if y > 0:        print "Quadrant 2"
```

```
    elif y < 0:     print "Quadrant 3"
```

```
    else:           print "negative x-Axis"
```

```
else: print "y-Axis"
```

RECURSION

Recursion

- a function can call other functions
- a function can call **itself**
- such a function is called a *recursive* function
- Example 1:

```
def countdown(n):  
    if n <= 0:  
        print "Ka-Boooom!"  
    else:  
        print n, "seconds left!"  
        countdown(n-1)  
countdown(3)
```


Stack Diagrams for Recursion



Recursion

- a function can call other functions
- a function can call **itself**
- such a function is called a *recursive* function
- Example 2:

```
def polyline(t, n, length, angle):  
    for i in range(n):  
        fd(t, length)  
        lt(t, angle)
```

Recursion

- a function can call other functions
- a function can call **itself**
- such a function is called a *recursive* function
- Example 2:

```
def polyline(t, n, length, angle):
```

```
    if n > 0:
```

```
        fd(t, length)
```

```
        lt(t, angle)
```

```
        polyline(t, n-1, length, angle)
```

Infinite Recursion

- base case = no recursive function call reached
- we say the function call *terminates*
 - Example 1: `n == 0` in countdown / polyline
- infinite recursion = no base case is reached
- also called *non-termination*
- Example:

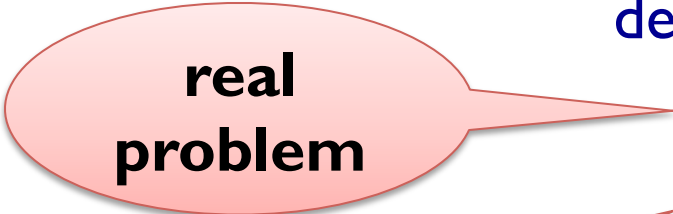
```
def infinitely_often():  
    infinitely_often()
```
- Python has *recursion limit* 1000 – ask `sys.getrecursionlimit()`

Keyboard Input

- so far we only know `input()`
 - what happens when we enter `Hello`?
 - `input()` treats all input as Python expression `<expr>`
- for string input, use `raw_input()`
 - what happens when we enter `42`?
 - `raw_input()` treats all input as string
- both functions can take one argument `prompt`
 - Example 1: `a = input("first side: ")`
 - Example 2: `name = raw_input("Your name:\n")`
 - “`\n`” denotes a new line: `print "Hello\nWorld\n!"`

Debugging using Tracebacks

- error messages in Python give important information:
 - where did the error occur?
 - what kind of error occurred?
- unfortunately often hard to localize real problem
- Example:



**real
problem**



**error
reported**

```
def determine_vat(base_price, vat_price):  
    factor = base_price / vat_price  
    reverse_factor = 1 / factor  
    return reverse_factor - 1  
print determine_vat(400, 500)
```

Debugging using Tracebacks

- error messages in Python give important information:
 - where did the error occur?
 - what kind of error occurred?
- unfortunately often hard to localize real problem
- Example:

```
def determine_vat(base_price, vat_price):  
    factor = float(base_price) / vat_price  
    reverse_factor = 1 / factor  
    return reverse_factor - 1  
print determine_vat(400, 500)
```

FRUITFUL FUNCTIONS

Return Values

- so far we have seen only functions with one or no `return`
- sometimes more than one `return` makes sense
- Example 1:

```
def sign(x):  
    if x < 0:  
        return -1  
    elif x == 0:  
        return 0  
    else:  
        return 1
```

Return Values

- so far we have seen only functions with one or no **return**
- sometimes more than one **return** makes sense

- Example 1:

```
def sign(x):  
    if x < 0:  
        return -1  
    elif x == 0:  
        return 0  
    return 1
```

- important that all paths reach one **return**

Incremental Development

- Idea: test code while writing it
- Example: computing the distance between (x_1, y_1) and (x_2, y_2)

```
def distance(x1, y1, x2, y2):  
    print "x1 y1 x2 y2:", x1, y1, x2, y2
```

Incremental Development

- Idea: test code while writing it
- Example: computing the distance between (x_1, y_1) and (x_2, y_2)

```
def distance(x1, y1, x2, y2):  
    print "x1 y1 x2 y2:", x1, y1, x2, y2  
    dx = x2 - x1          # horizontal distance  
    print "dx:", dx
```

Incremental Development

- Idea: test code while writing it
- Example: computing the distance between (x_1, y_1) and (x_2, y_2)

```
def distance(x1, y1, x2, y2):  
    print "x1 y1 x2 y2:", x1, y1, x2, y2  
    dx = x2 - x1          # horizontal distance  
    print "dx:", dx  
    dy = y2 - y1          # vertical distance  
    print "dy:", dy
```

Incremental Development

- Idea: test code while writing it
- Example: computing the distance between (x_1, y_1) and (x_2, y_2)

```
def distance(x1, y1, x2, y2):  
    print "x1 y1 x2 y2:", x1, y1, x2, y2  
    dx = x2 - x1          # horizontal distance  
    print "dx:", dx  
    dy = y2 - y1          # vertical distance  
    print "dy:", dy  
    dxs = dx**2; dys = dy**2  
    print "dxs dys:", dxs, dys
```

Incremental Development

- Idea: test code while writing it
- Example: computing the distance between (x_1, y_1) and (x_2, y_2)

```
def distance(x1, y1, x2, y2):  
    print "x1 y1 x2 y2:", x1, y1, x2, y2  
    dx = x2 - x1          # horizontal distance  
    dy = y2 - y1          # vertical distance  
    dxs = dx**2; dys = dy**2  
    print "dxs dys:", dxs, dys
```

Incremental Development

- Idea: test code while writing it
- Example: computing the distance between (x_1, y_1) and (x_2, y_2)

```
def distance(x1, y1, x2, y2):  
    print "x1 y1 x2 y2:", x1, y1, x2, y2  
    dx = x2 - x1          # horizontal distance  
    dy = y2 - y1          # vertical distance  
    dxs = dx**2; dys = dy**2  
    print "dxs dys:", dxs, dys  
    ds = dxs + dys        # square of distance  
    print "ds:", ds
```


Incremental Development

- Idea: test code while writing it
- Example: computing the distance between (x_1, y_1) and (x_2, y_2)

```
def distance(x1, y1, x2, y2):  
    print "x1 y1 x2 y2:", x1, y1, x2, y2  
    dx = x2 - x1          # horizontal distance  
    dy = y2 - y1          # vertical distance  
    dxs = dx**2; dys = dy**2  
    ds = dxs + dys        # square of distance  
    print "ds:", ds
```

Incremental Development

- Idea: test code while writing it
- Example: computing the distance between (x_1, y_1) and (x_2, y_2)

```
def distance(x1, y1, x2, y2):  
    print "x1 y1 x2 y2:", x1, y1, x2, y2  
    dx = x2 - x1      # horizontal distance  
    dy = y2 - y1      # vertical distance  
    dxs = dx**2; dys = dy**2  
    ds = dxs + dys    # square of distance  
    print "ds:", ds  
    d = math.sqrt(ds) # distance  
    print d
```

Incremental Development

- Idea: test code while writing it
- Example: computing the distance between (x_1, y_1) and (x_2, y_2)

```
def distance(x1, y1, x2, y2):  
    print "x1 y1 x2 y2:", x1, y1, x2, y2  
    dx = x2 - x1      # horizontal distance  
    dy = y2 - y1      # vertical distance  
    dxs = dx**2; dys = dy**2  
    ds = dxs + dys    # square of distance  
    d = math.sqrt(ds) # distance  
    print d
```

Incremental Development

- Idea: test code while writing it
- Example: computing the distance between (x_1, y_1) and (x_2, y_2)

```
def distance(x1, y1, x2, y2):  
    print "x1 y1 x2 y2:", x1, y1, x2, y2  
    dx = x2 - x1      # horizontal distance  
    dy = y2 - y1      # vertical distance  
    dxs = dx**2; dys = dy**2  
    ds = dxs + dys    # square of distance  
    d = math.sqrt(ds) # distance  
    print d  
    return d
```

Incremental Development

- Idea: test code while writing it
- Example: computing the distance between (x_1, y_1) and (x_2, y_2)

```
def distance(x1, y1, x2, y2):  
    dx = x2 - x1      # horizontal distance  
    dy = y2 - y1      # vertical distance  
    dxs = dx**2; dys = dy**2  
    ds = dxs + dys    # square of distance  
    d = math.sqrt(ds) # distance  
    return d
```

Incremental Development

- Idea: test code while writing it
- Example: computing the distance between (x_1, y_1) and (x_2, y_2)

```
def distance(x1, y1, x2, y2):  
    dx = x2 - x1          # horizontal distance  
    dy = y2 - y1          # vertical distance  
    return math.sqrt(dx**2 + dy**2)
```

Incremental Development

- Idea: test code while writing it
 1. start with minimal function
 2. add functionality piece by piece
 3. use variables for intermediate values
 4. print those variables to follow your progress
 5. remove unnecessary output when function is finished

Composition

- function calls can be arguments to functions
- direct consequence of arguments being expressions
- Example: area of a circle from center and peripheral point

```
def area(radius):  
    return math.pi * radius**2
```

```
def area_from_points(xc, yc, xp, yp):  
    return area(distance(xc, yc, xp, yp))
```


Boolean Functions

- boolean functions = functions that return **True** or **False**
- useful e.g. as **<cond>** in a conditional execution
- Example:

```
def divides(x, y):
```

```
    if y / x * x == y:    # remainder of integer division is 0
```

```
        return True
```

```
    return False
```

Boolean Functions

- boolean functions = functions that return **True** or **False**
- useful e.g. as **<cond>** in a conditional execution
- Example:

```
def divides(x, y):
```

```
    if y % x == 0:           # remainder of integer division is 0
```

```
        return True
```

```
    return False
```

Boolean Functions

- boolean functions = functions that return **True** or **False**
- useful e.g. as **<cond>** in a conditional execution
- Example:

```
def divides(x, y):  
    return y % x == 0
```

Boolean Functions

- boolean functions = functions that return **True** or **False**
- useful e.g. as **<cond>** in a conditional execution
- Example:

```
def divides(x, y):  
    return y % x == 0
```

```
def even(x):  
    return divides(2, x)
```

Boolean Functions

- boolean functions = functions that return **True** or **False**
- useful e.g. as **<cond>** in a conditional execution
- Example:

```
def divides(x, y):  
    return y % x == 0
```

```
def even(x):  
    return divides(2, x)
```

```
def odd(x):  
    return not divides(2, x)
```

Boolean Functions

- boolean functions = functions that return **True** or **False**
- useful e.g. as **<cond>** in a conditional execution
- Example:

```
def divides(x, y):  
    return y % x == 0
```

```
def even(x):  
    return divides(2, x)
```

```
def odd(x):  
    return not even(x)
```

**RECURSION:
SEE RECURSION**

Recursion is “Complete”

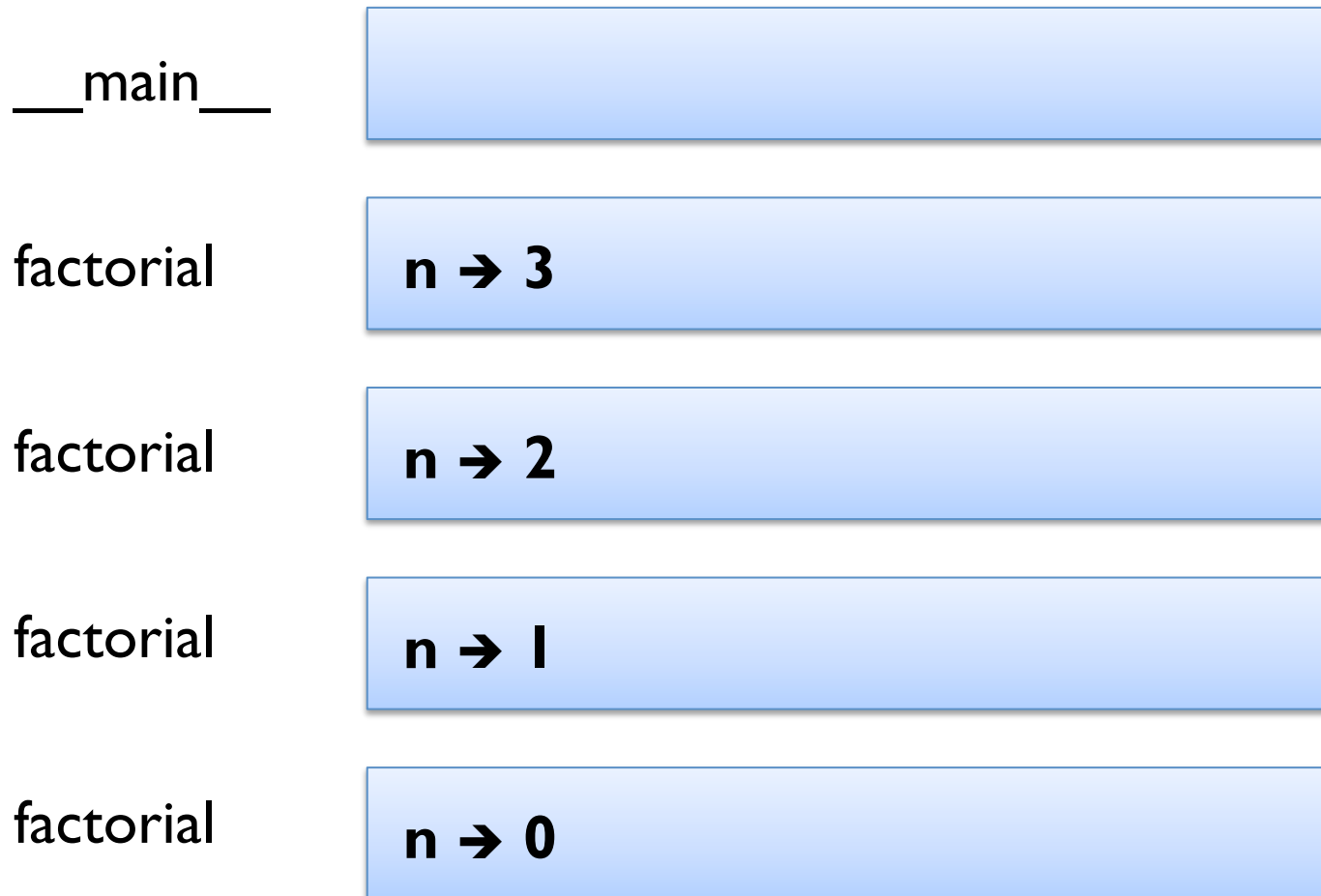
- so far we know:
 - values of type integer, float, string
 - arithmetic expressions
 - (recursive) function definitions
 - (recursive) function calls
 - conditional execution
 - input/output
- **ALL** possible programs can be written using these elements!
- we say that we have a “Turing complete” language

Factorial

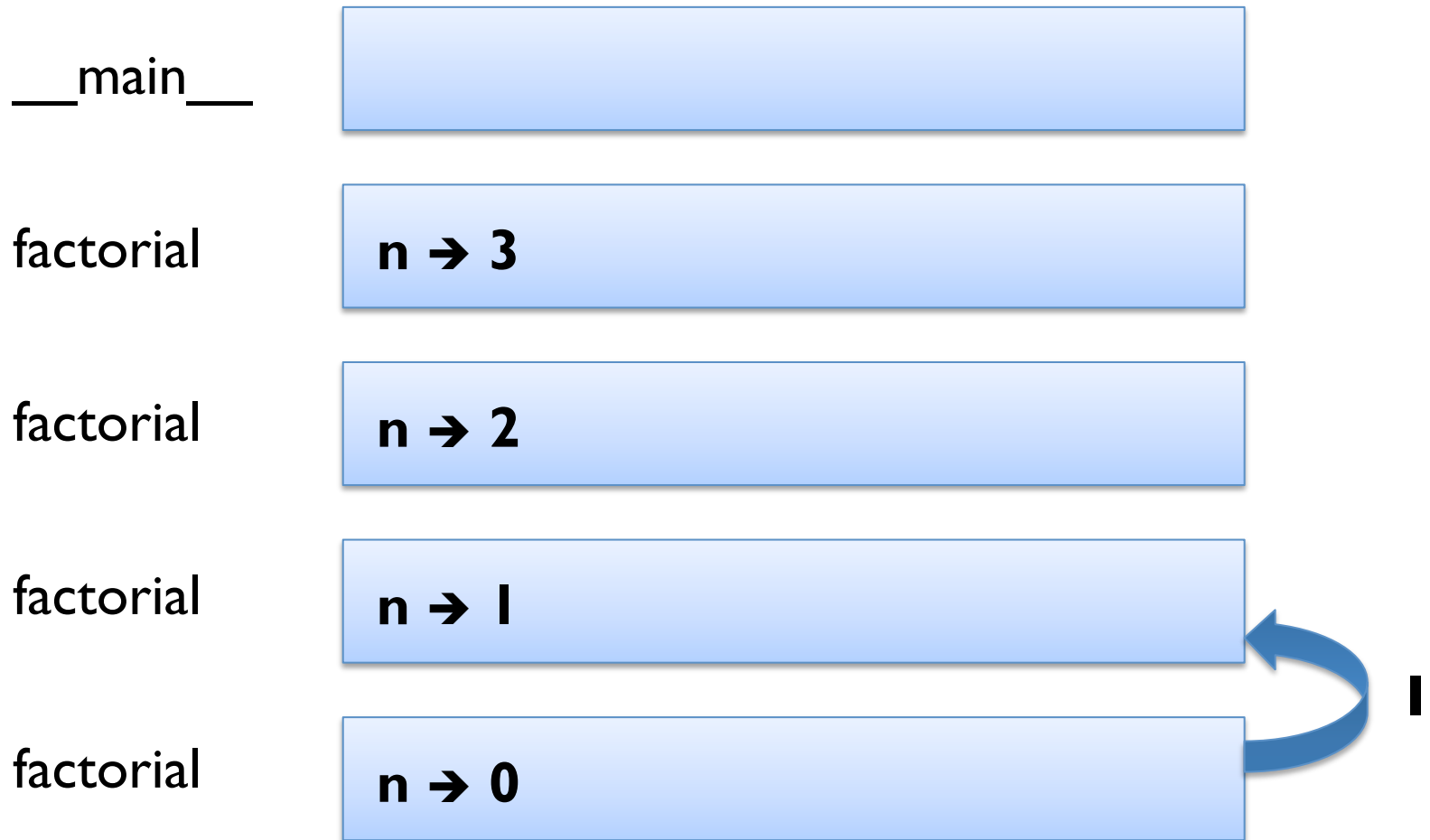
- in mathematics, the factorial function is defined by
 - $0! = 1$
 - $n! = n * (n-1)!$
- such *recursive* definitions can trivially be expressed in Python
- Example:

```
def factorial(n):  
    if n == 0:  
        return 1  
    recurse = factorial(n-1)  
    result = n * recurse  
    return result  
x = factorial(3)
```

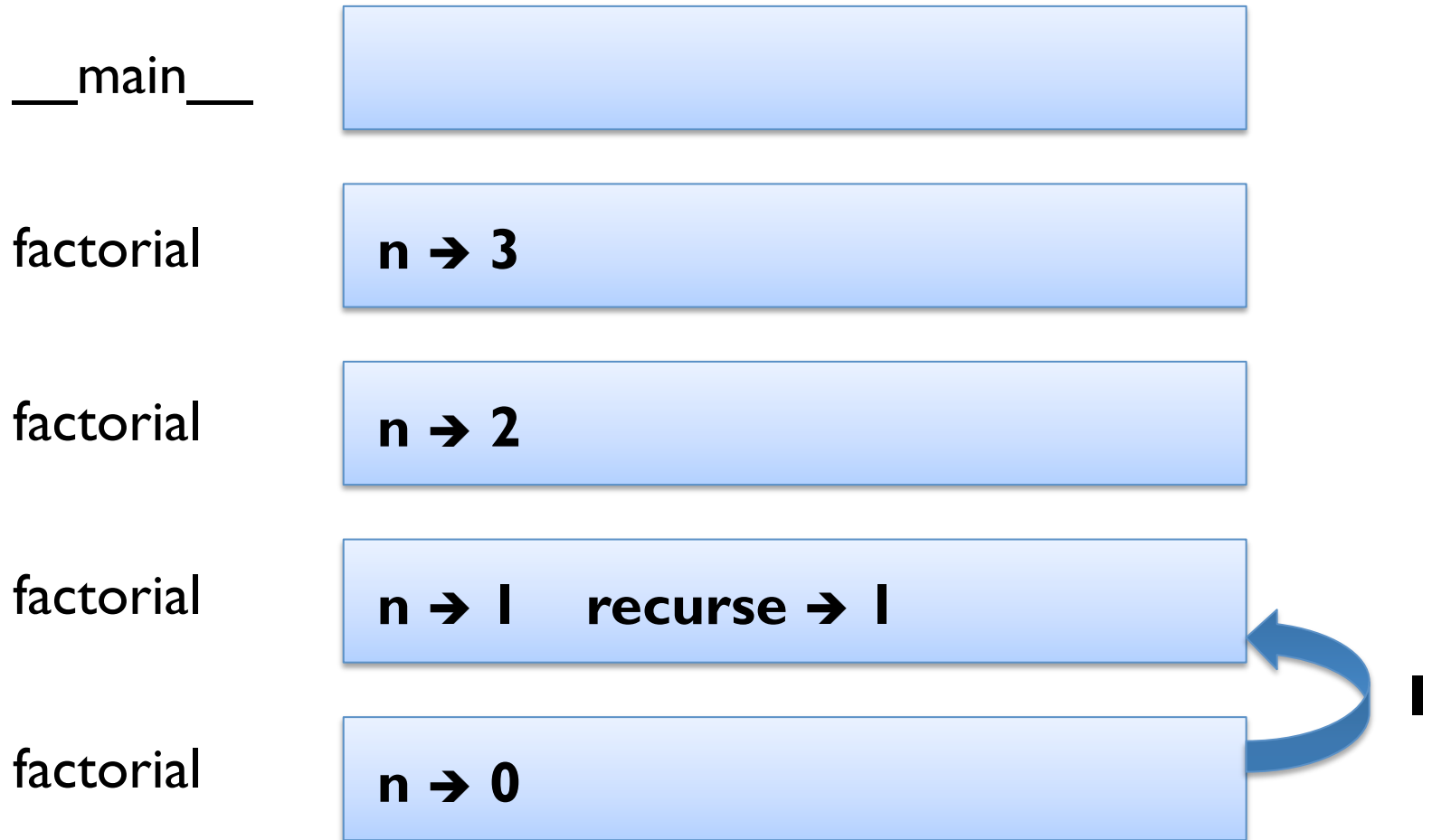
Stack Diagram for Factorial



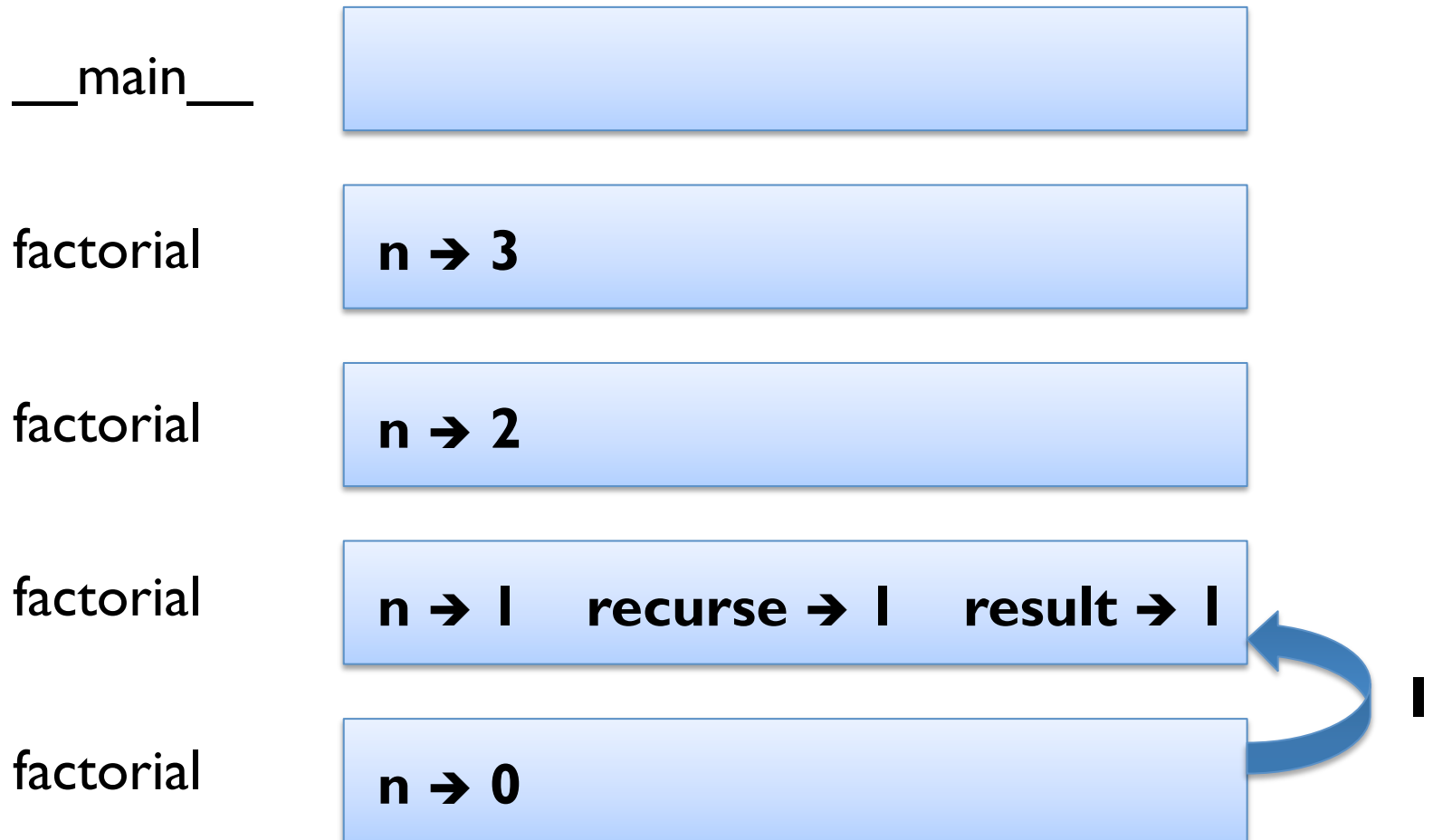
Stack Diagram for Factorial



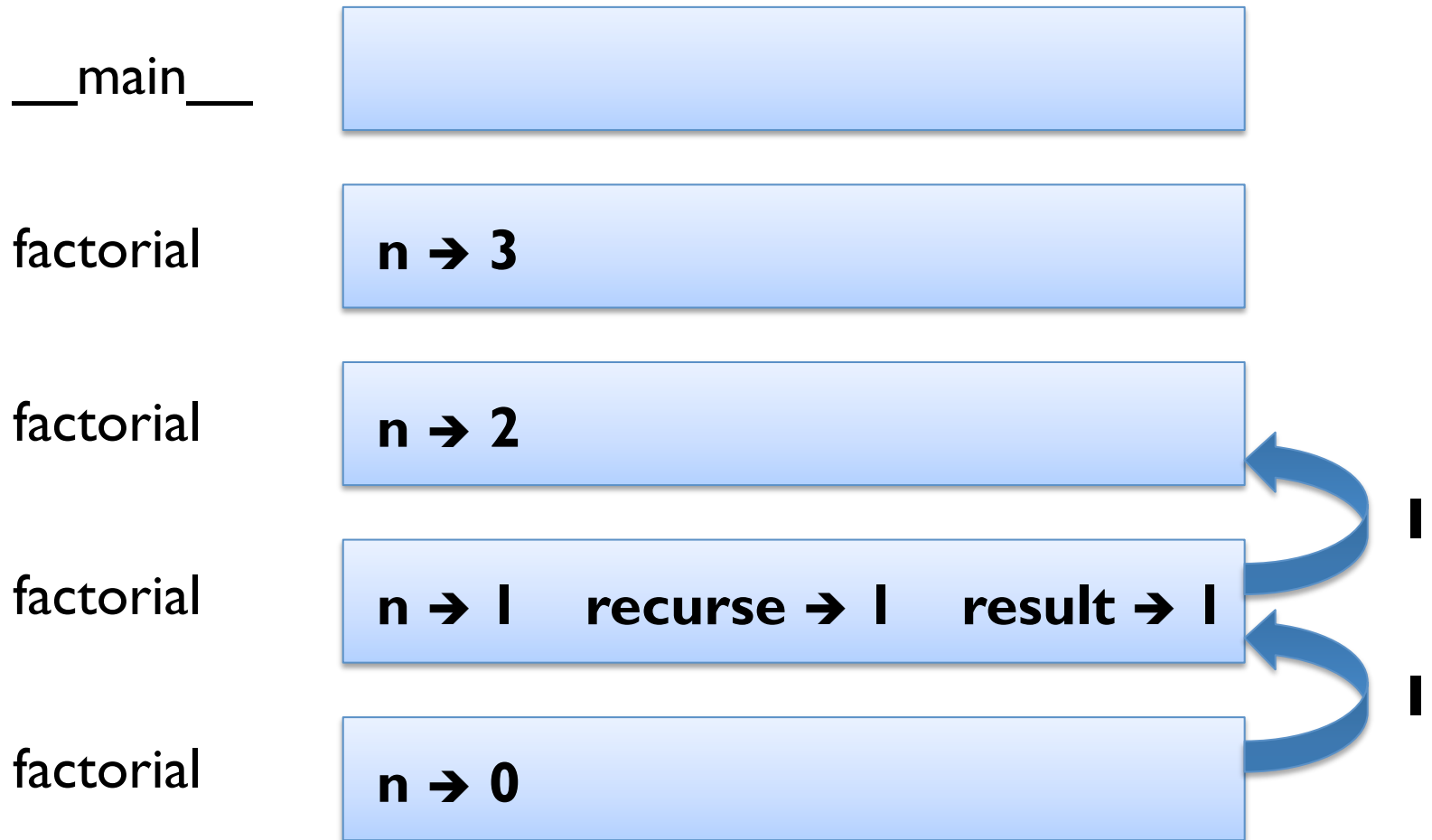
Stack Diagram for Factorial



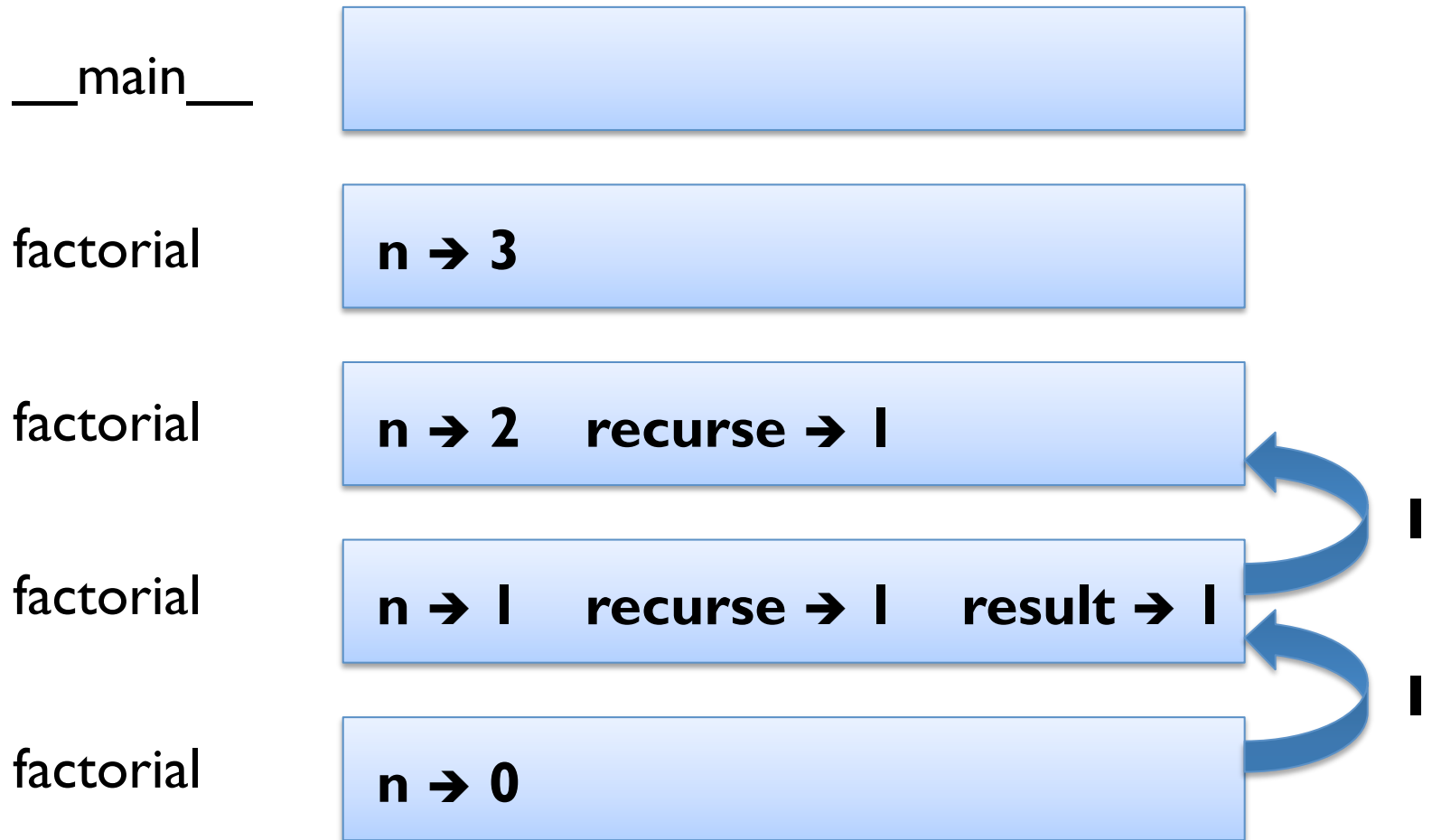
Stack Diagram for Factorial



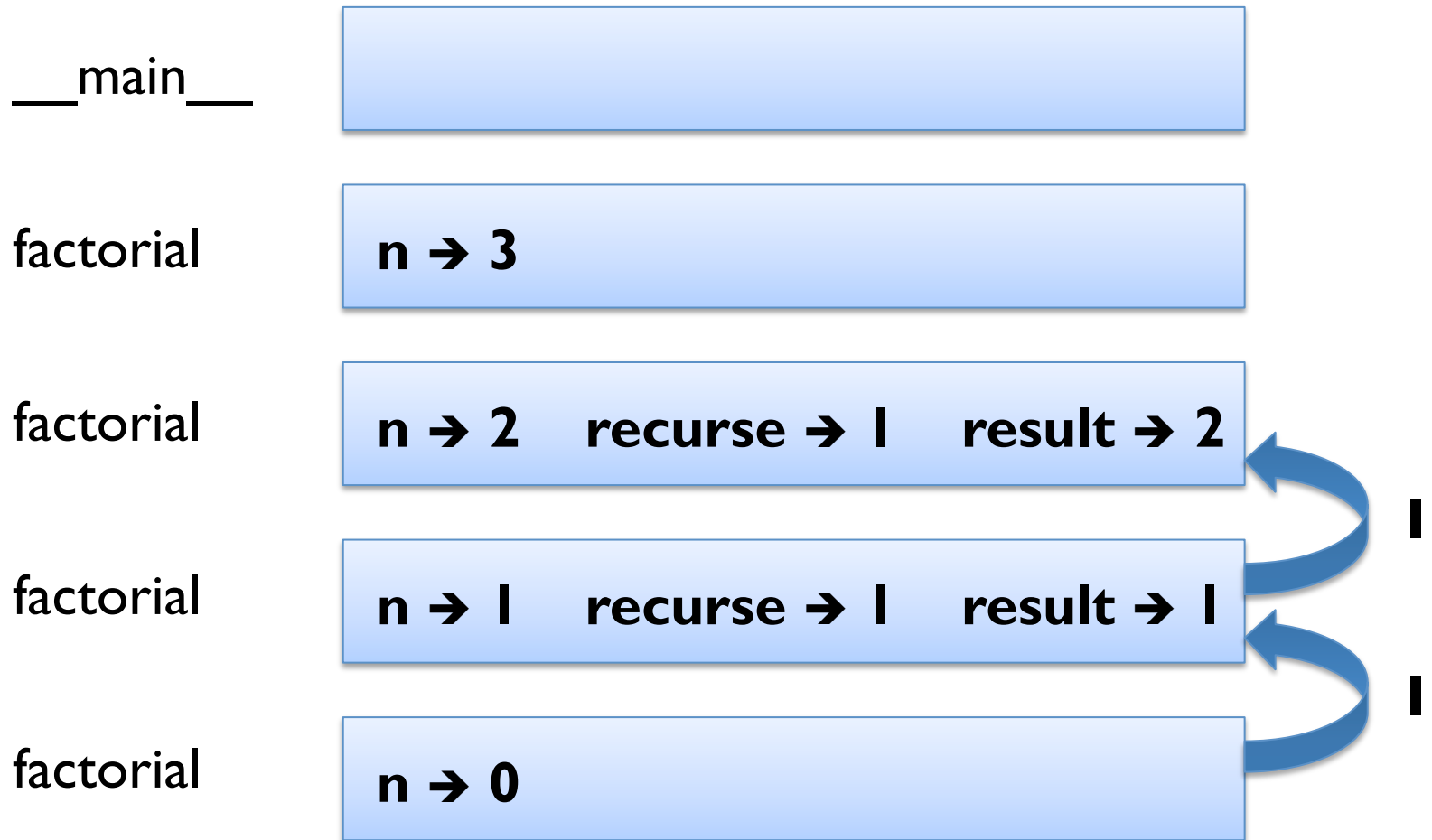
Stack Diagram for Factorial



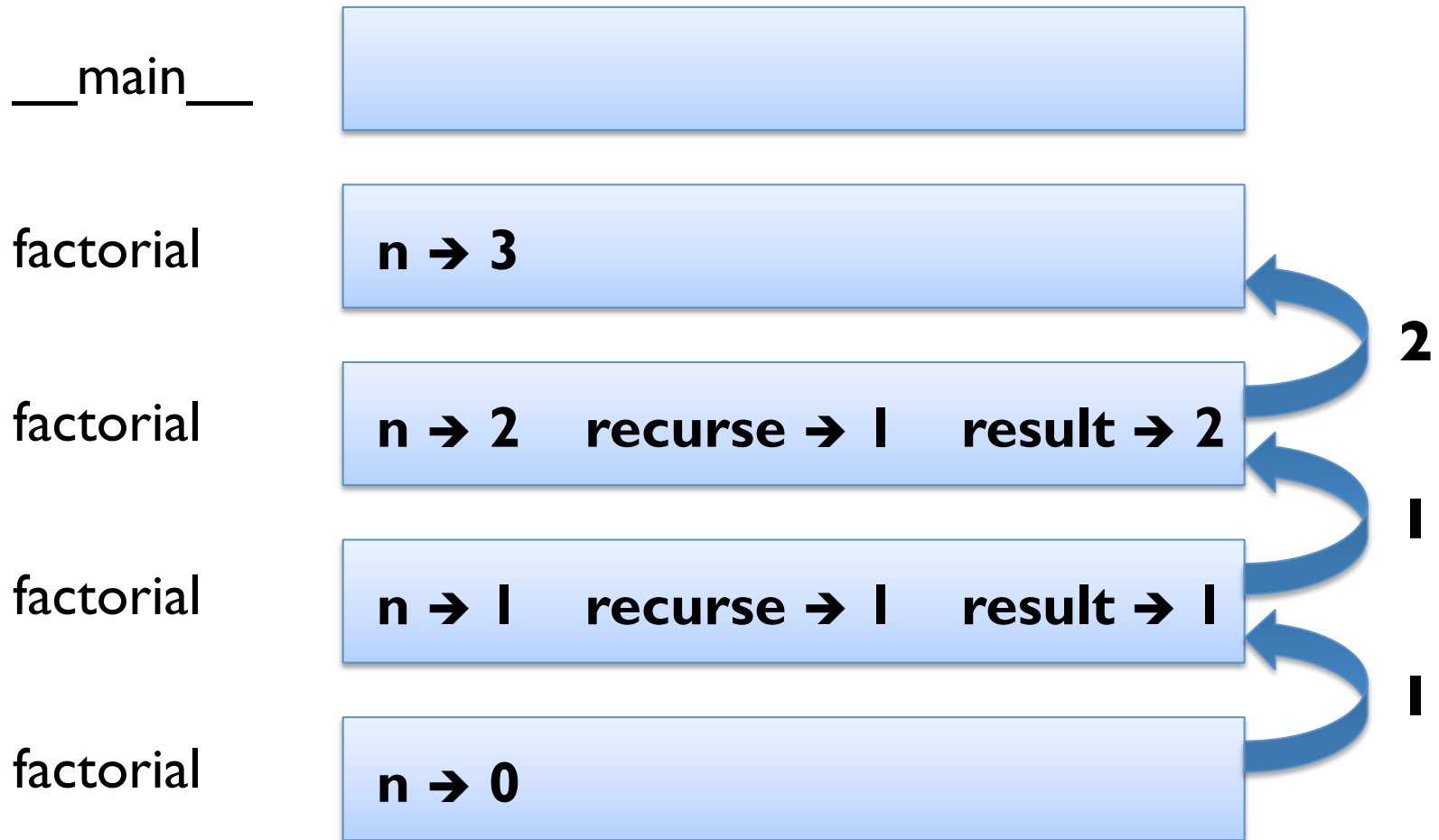
Stack Diagram for Factorial



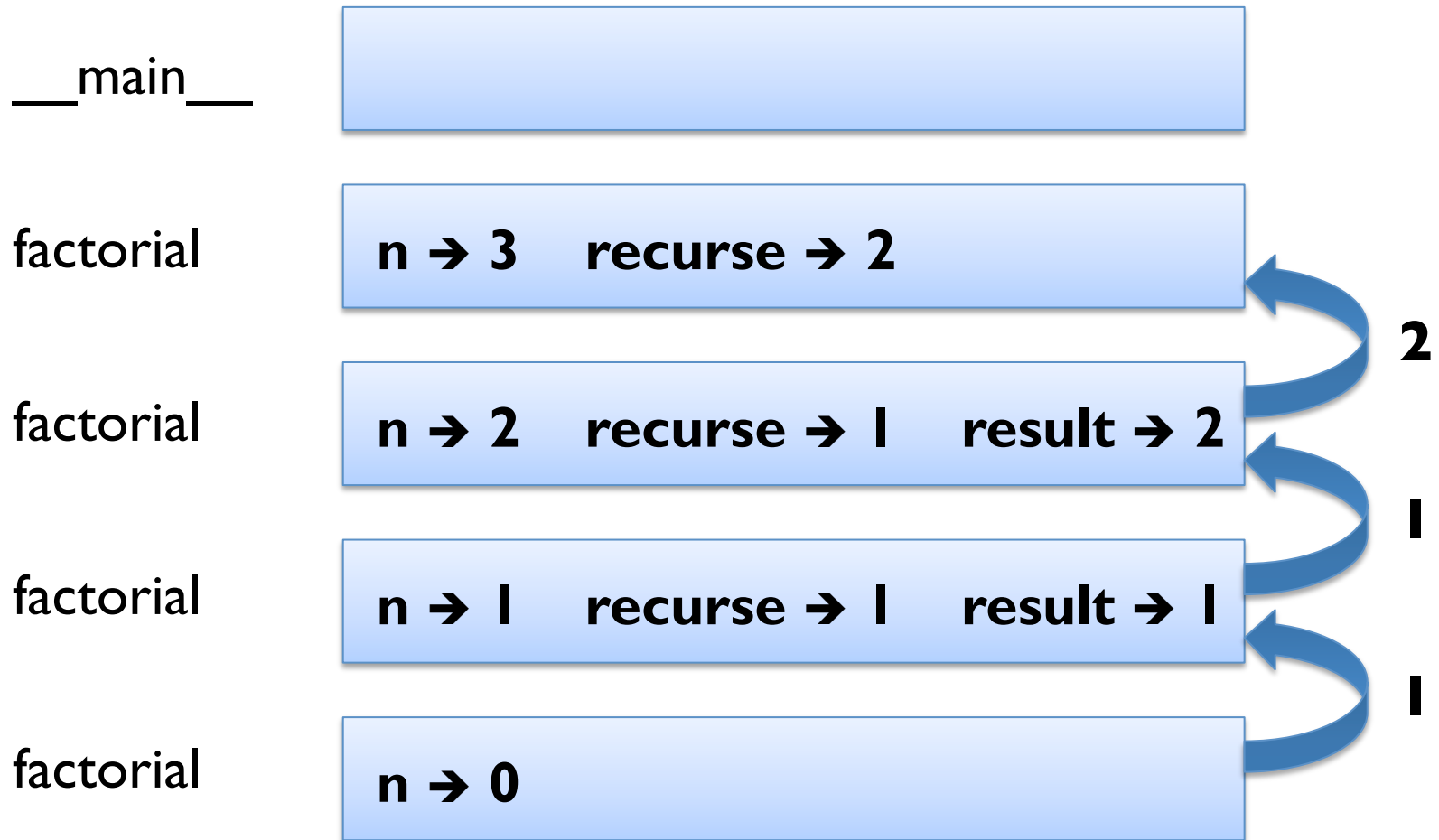
Stack Diagram for Factorial



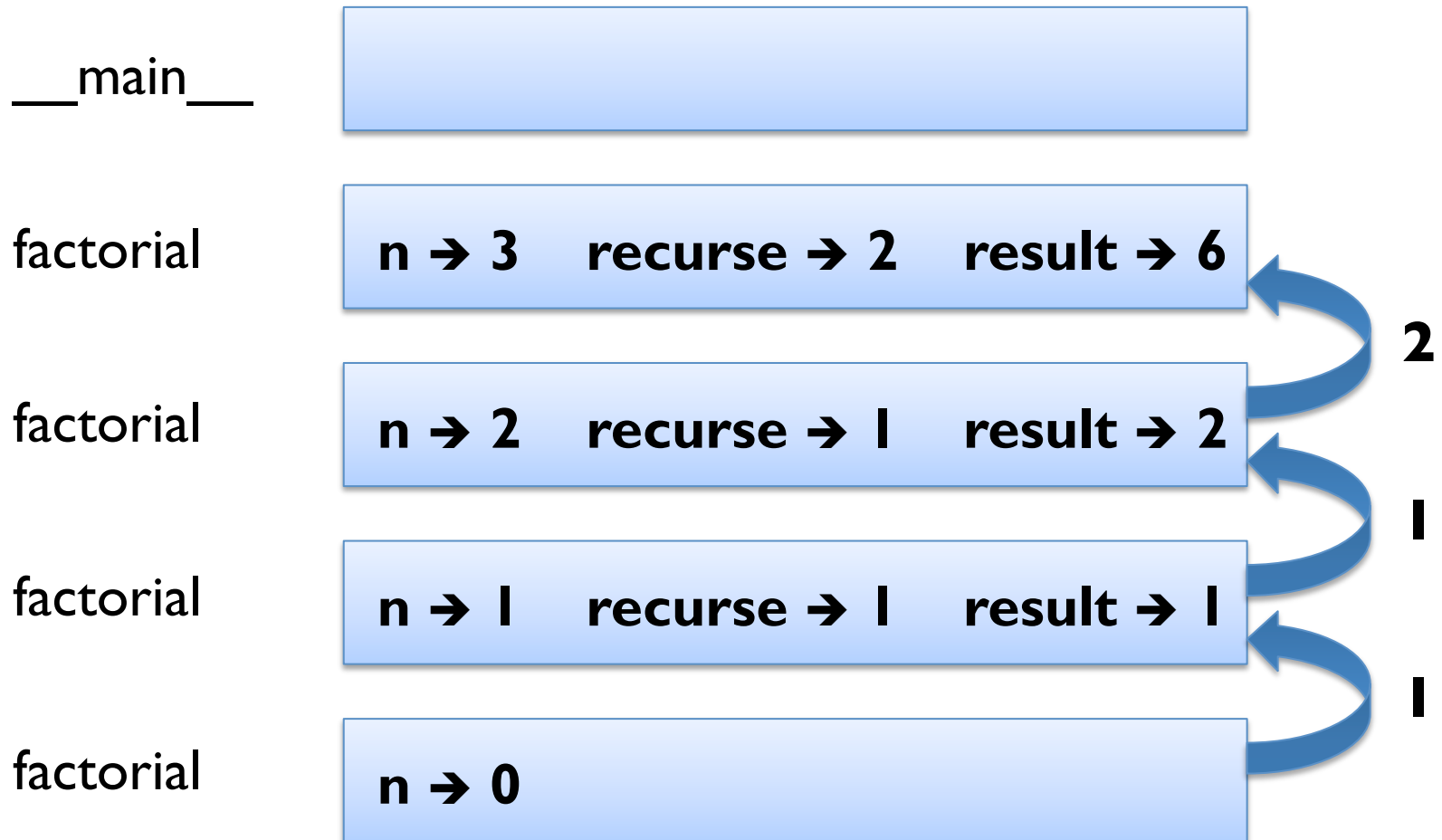
Stack Diagram for Factorial



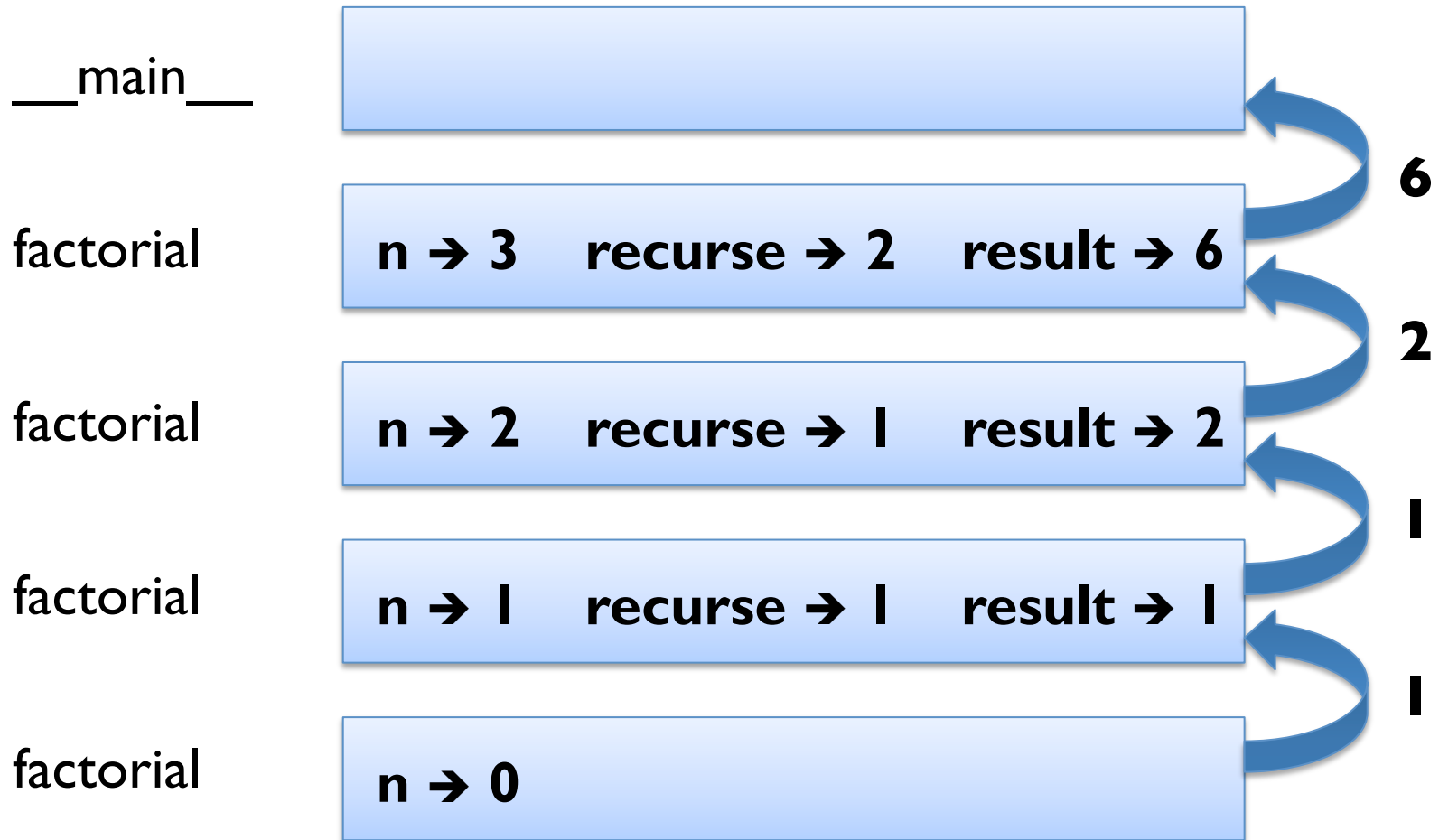
Stack Diagram for Factorial



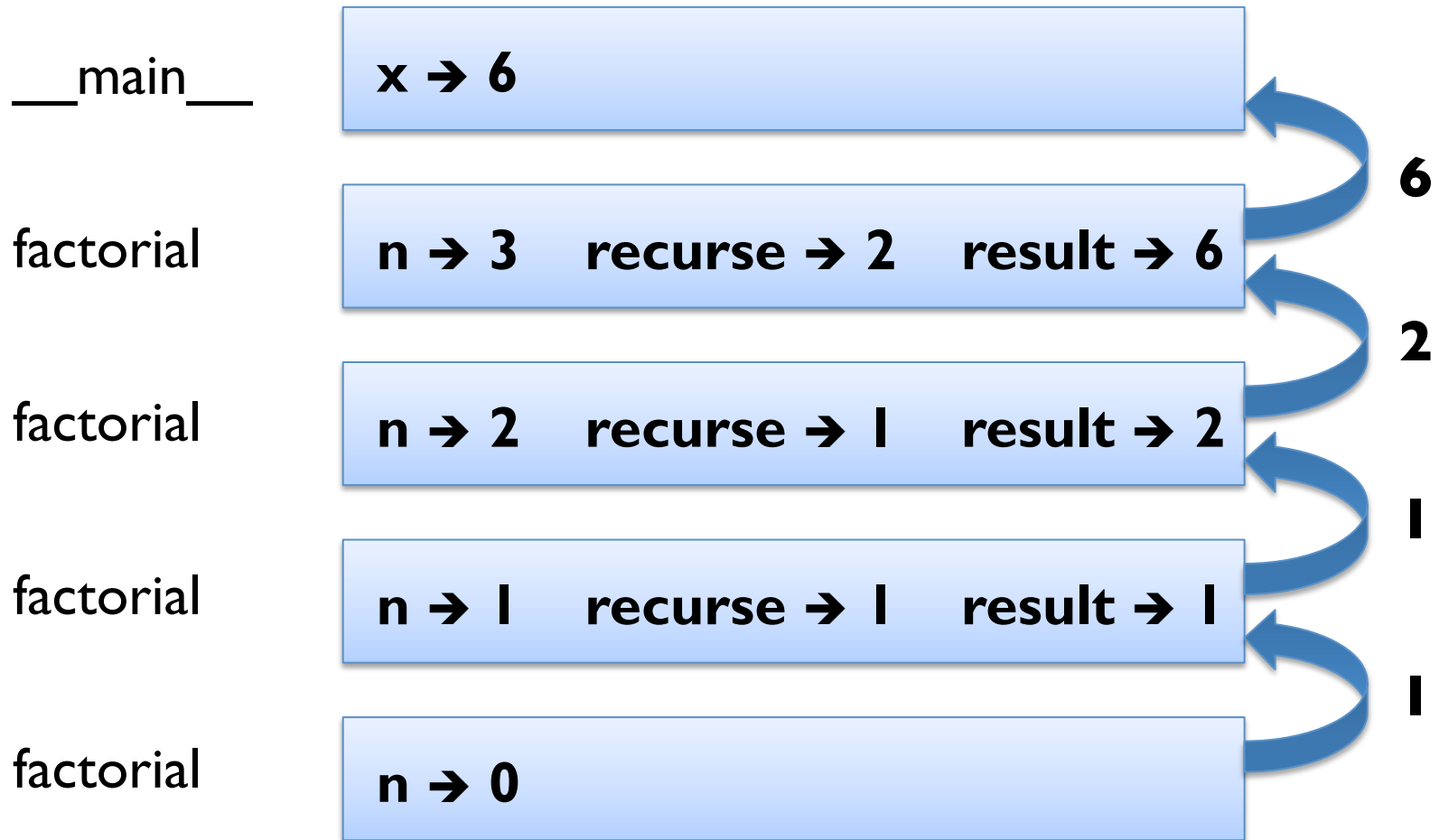
Stack Diagram for Factorial



Stack Diagram for Factorial



Stack Diagram for Factorial



Leap of Faith

- following the flow of execution difficult with recursion
- alternatively take the “leap of faith” (*induction*)
- Example:

```
def factorial(n):
```

```
    if n == 0:
```

```
        return 1
```

```
    recurse = factorial(n - 1)
```

```
    result = n * recurse
```

```
    return result
```

```
x = factorial(3)
```

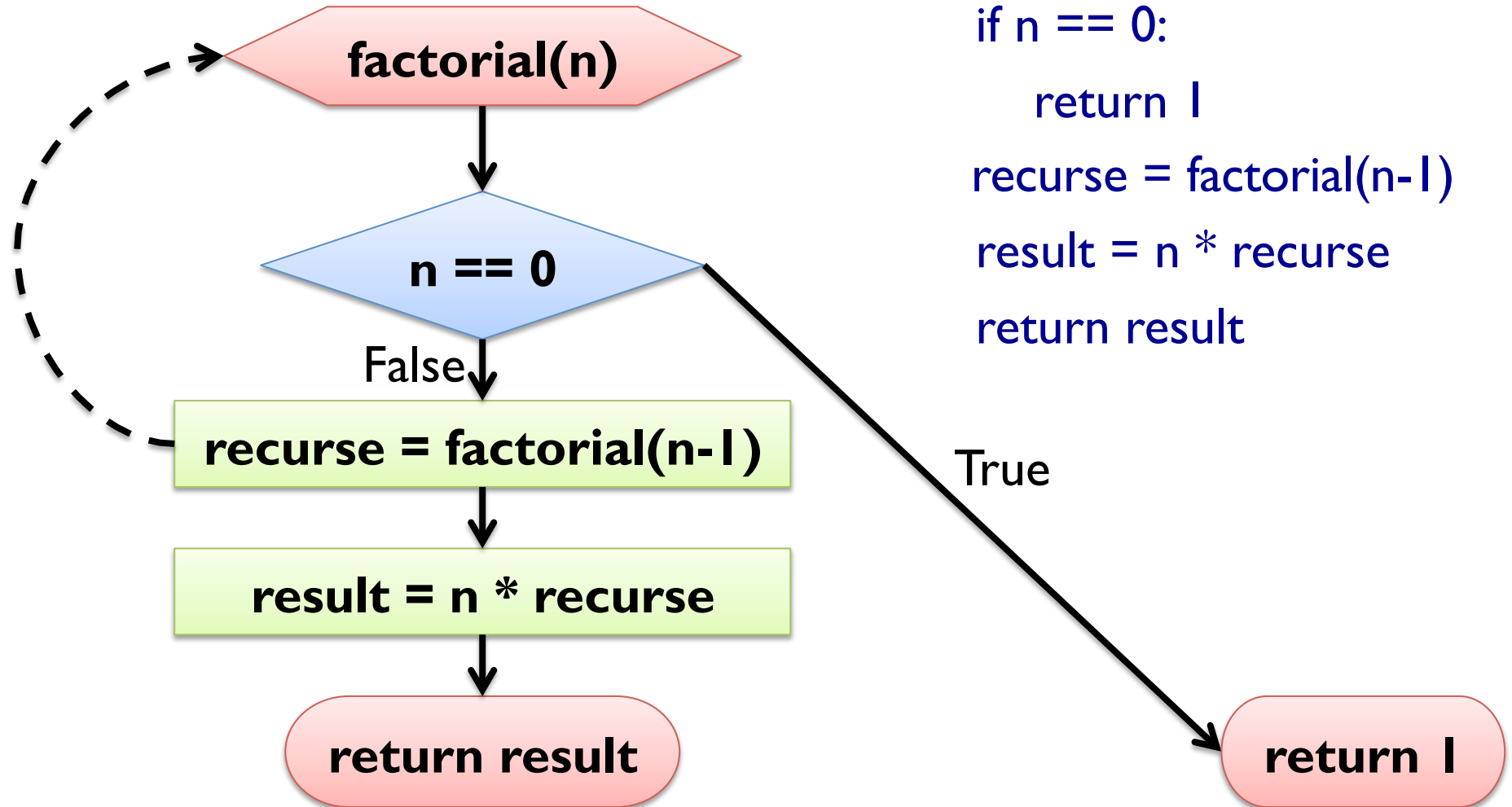
**check the
base case**

**assume recursive
call is correct**

**check the
step case**

Control Flow Diagram

- Example:



```
def factorial(n):  
    if n == 0:  
        return 1  
    recurse = factorial(n-1)  
    result = n * recurse  
    return result
```