



DM503

Programming B

Peter Schneider-Kamp

petersk@imada.sdu.dk

<http://imada.sdu.dk/~petersk/DM503/>

ABSTRACT DATATYPE FOR LISTS

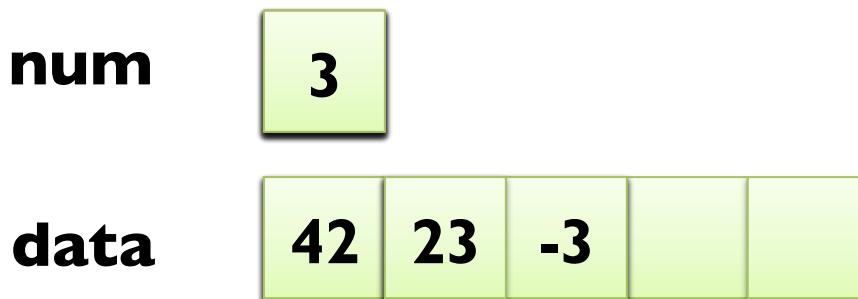
List ADT: Specification

- data are all integers, here represented as primitive int
- operations are defined by the following interface

```
public interface ListOfInt {  
    public int get(int i);                      // get i-th integer (0-based)  
    public void set(int i, int elem);            // set i-th element  
    public int size();                          // return length of list  
    public void add(int elem);                  // add element at end  
    public void add(int i, int elem);            // insert element at pos. i  
    public void remove(int i);                  // remove i-th element  
}
```

Partially Full Arrays

- arrays are fixed-length
- lists are variable-length
- **Idea:**
 - use an array of (fixed) length
 - track number of elements in variable
- **Example:** `add(23)` `add(42)` `add(-3)` `remove(0)` `add(1, 23)`



List ADT: Design & Implementation I

- Design I: partially full arrays of int
- Implementation I:

```
public class PartialArrayListOfInt implements ListOfInt {  
    private int limit;          // maximal number of elements  
    private int[] data;         // elements of the list  
    private int num = 0;         // current number of elements  
    public PartialArrayListOfInt(int limit) {  
        this.limit = limit;  
        this.data = new int[limit];  
    }  
    ...  
}
```

List ADT: Implementation I

- Implementation I (continued):

```
public class PartialArrayListOfInt implements ListOfInt { ...  
    private int[] data;  
    private int num = 0; ...  
    public int get(int i) {  
        if (i < 0 || i >= num) {  
            throw new IndexOutOfBoundsException();  
        }  
        return this.data[i];  
    }  
    ...  
}
```

List ADT: Implementation I

- Implementation I (continued):

```
public class PartialArrayListOfInt implements ListOfInt { ...  
    private int[] data;  
    private int num = 0; ...  
    public void set(int i, int elem) {  
        if (i < 0 || i >= num) {  
            throw new IndexOutOfBoundsException();  
        }  
        this.data[i] = elem;  
    }  
    ...  
}
```

List ADT: Implementation I

- Implementation I (continued):

```
public class PartialArrayListOfInt implements ListOfInt { ...  
    private int[] data;  
    private int num = 0; ...  
    public int size() {  
        return this.num;  
    }  
    public void add(int elem) {  
        this.add(this.num, elem); // insert at end  
    }  
    ...  
}
```

List ADT: Implementation I

- Implementation I (continued):

```
public class PartialArrayListOfInt implements ListOfInt { ...  
    public void add(int i, int elem) {  
        if (i < 0 || i > num) { throw new Index...Exception(); }  
        if (num >= limit) { throw new RuntimeException("full!"); }  
        for (int j = num-1; j >= i; j--) {  
            this.data[j+1] = this.data[j]; // move elements right  
        }  
        this.data[i] = elem;           // insert new element  
        num++;                      // one element more!  
    }  
    ...  }
```

List ADT: Implementation I

- Implementation I (continued):

```
public class PartialArrayListOfInt implements ListOfInt { ...  
    public void remove(int i) {  
        if (i < 0 || i >= num) { throw new Index...Exception(); }  
        for (int j = i; j+1 < num; j++) {  
            this.data[j] = this.data[j+1]; // move elements left  
        }  
        num--; // one element less!  
    }  
    // DONE!  
}
```

Dynamic Arrays

- arrays are fixed-length
- lists are variable-length
- **Idea:**
 - use an array of (fixed) length & track number of elements
 - extend array as needed by **add** method

add(23) **add(42)** **add(-3)** **add(17)** **add(31)**

- **Example:**

num

5

data

23 42 -3 17 31

List ADT: Design & Implementation 2

- Design 2: dynamic arrays of int
- Implementation 2:

```
public class DynamicArrayListOfInt extends PartialArrayListOfInt {  
    public DynamicArrayListOfInt(int limit) {  
        super(limit);  
    }  
    public void add(int i, int elem) {  
        if (i < 0 || i > num) { throw new Index...Exception(); }  
        ...  
    }  
}
```

List ADT: Implementation 2

- Implementation 2 (continued):

```
if (num >= limit) {      // array is full  
    int[] newData = new int[2*this.limit];  
    for (int j = 0; j < limit; j++) { newData[j] = data[j]; }  
    this.data = newData;  
    this.limit *= 2;  
}  
  
for (int j = num-1; j >= i; j--) {  
    this.data[j+1] = this.data[j]; // move elements right  
}  
this.data[i] = elem;      num++;  
} }
```

List ADT: Design 2 Revisited

- Design 2 (revisited): symmetric dynamic arrays of int
 - keep `startIndex` and `endIndex` of used indices
 - start with `startIndex = endIndex = limit / 2`
 - i.e., `limit / 2` free positions at the beginning
 - i.e., `limit / 2` free positions at the end
 - extend array at the beginning when `startIndex < 0` needed
 - extend array at the end when `endIndex > limit` needed
 - shrink array in remove, when
`(endIndex – startIndex) < limit / 4`

List ADT: Design 3

- goal is to use list for arbitrary data types
- Design 3: dynamic arrays of objects
- Implementation 3:

```
public class DynamicArrayList implements List {  
    private int limit;           // current maximum number  
    private Object[] data;       // elements of the list  
    private int num = 0;          // current number of elements  
  
    public DynamicArrayList(int limit) {  
        this.limit = limit;  
        this.data = new Object[limit];  
    } ...  
}
```

How to use with
int, double etc.?

Boxing and Unboxing

- primitive types like `int`, `double`, ... are not objects!
- Java provides wrapper classes `Integer`, `Double`, ...
- Example:
`Integer myInteger = new Integer(13);`
`int myInt = myInteger.intValue();`
- transparent due to *automatic boxing* and *unboxing*
- Example:
`Integer myInteger = 13;`
`int myInt = myInteger;`
- useful when e.g. storing `int` values in a `Object[]`

List ADT: ArrayList

- Java provides pre-defined symmetric dynamic array list implementation in class `java.util.ArrayList`
- Example:

```
ArrayList myList = new ArrayList(10);           // initial limit 10
for (int i = 0; i < 100; i++) {
    myList.add(i*i);                          // list of squares of 0 ... 99
}
System.out.println(myList);
for (int i = 99; i >= 0; i--) {
    int n = (Integer) myList.get(i);          // get returns Object
    myList.set(i, n*n);                      // now to the power of 4!
}
```

Generic Types

- type casts for accessing elements are unsafe!
- solution is to use *generic types*
- instead of using an array of objects, use array of some type E
- Example:

```
public class MyArrayList<E> implements List<E> {  
    ...  
    private E[] data;  
    ...  
    public E get(int i) {  
        return this.data[i];  
    }  
}
```

Finding in Lists

- finding typical example for another List ADT operation
- specified by the following method signature:

```
public int indexOf(E elem) {  
    for (int i = 0; i < this.size(); i++) {  
        E cand = this.get(i);  
        if (elem == null ? cand == null : elem.equals(cand)) {  
            return i;          // found an equal element  
        }  
    }  
    return -1;          // did not find any match  
}
```

Sorting Lists

- sorting is another important List ADT operation
- many different approaches to sorting exist
- more on this: **DM507 Algorithms and Data Structures**
- Example (Selection Sort for list of int):

```
private void swap(int i1, i2) {
```

```
    E temp = this.get(i1);
```

```
    this.set(i1, this.get(i2));
```

```
    this.set(i2, temp);
```

```
}
```

num

8 42

this.swap(1,3)

data

23 17 -3 42 31 97 71 59

Sorting Lists

- sorting is another important List ADT operation
- many different approaches to sorting exist
- more about this in DM507 Algorithms and Data Structures
- Example (Selection Sort):

```
public void selectionSort() {  
    for (int firstPos = 0; firstPos < this.size()-1; firstPos++) {  
        int minPos = this.size()-1; // assume last element is smallest  
        for (int i = firstPos; i < this.size()-1; i++) {  
            if (this.get(i) < this.get(minPos)) { minPos = i; }  
        }  
        this.swap(minPos, firstPos);  
    } }
```

Sorting Lists

```
public void selectionSort() {  
    for (int firstPos = 0; firstPos < this.size()-1; firstPos++) {  
        int minPos = this.size()-1; // assume last element is smallest  
        for (int i = firstPos; i < this.size()-1; i++) {  
            if (this.get(i) < this.get(minPos)) { minPos = i; }  
        }  
        this.swap(minPos, firstPos);  
    }  
}
```



RECURSION (REVISITED)

Recursion (Revisited)

- recursive function = a function that calls itself
- Example (meaningless):

```
public static void main(String[] args) {  
    if (args.length > 0) { main(new String[args.length-1]); }  
}
```

- base case = no recursive function call reached
- we say the function call *terminates*
- infinite recursion = no base case is reached
- also called *non-termination*
- Java recursion depth only limited by Java stack size

Comparable Interface

- imposes *total order* on elements, i.e., all elements comparable
- works similar to `__cmp__(self, other)` method in Python
- classes need to implement interface Comparable:

```
public interface Comparable<T> {  
    public int compareTo(T other);  
}
```

- has to return 0, if `this` and `other` are equal according to `equals`
- has to return 1, if `this` is greater than `other`
- has to return -1, if `this` is smaller than `other`

Binary Search

- assume ordered list of elements implementing Comparable
- “Divide et Impera” gives us *binary search* by halving the list
- Example:

```
public int find(Comparable elem) {  
    return this.binarySearch(elem, 0, this.getSize()-1);  
}  
  
public int binarySearch(Comparable elem, int low, int high) {  
    if (low > high) { return -1; }      // range is empty; not found  
    int middle = (low + high) / 2;  
    switch (elem.compareTo(this.get(middle))) { ... }  
}
```

Binary Search

- Example (continued):

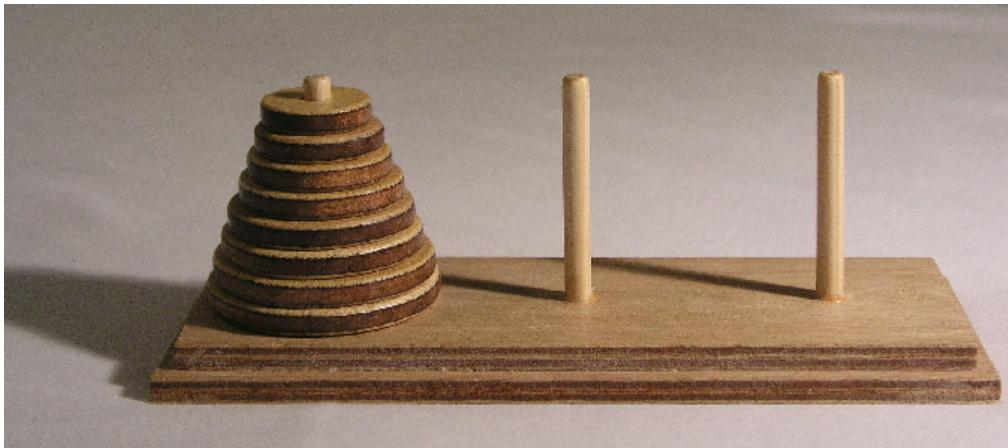
```
public int binarySearch(Comparable elem, int low, int high) {  
    if (low > high) { return -1; }      // range is empty; not found  
    int middle = (low + high) / 2;  
    switch (elem.compareTo(this.get(middle))) {  
        case 0:  return middle;  
        case 1:  return binarySearch(elem, middle+1, high);  
        case -1: return binarySearch(elem, low, middle-1);  
    }  
    throw new RuntimeException("compareTo error");  
}
```



binarySearch(42, 4, 4)

Towers of Hanoi

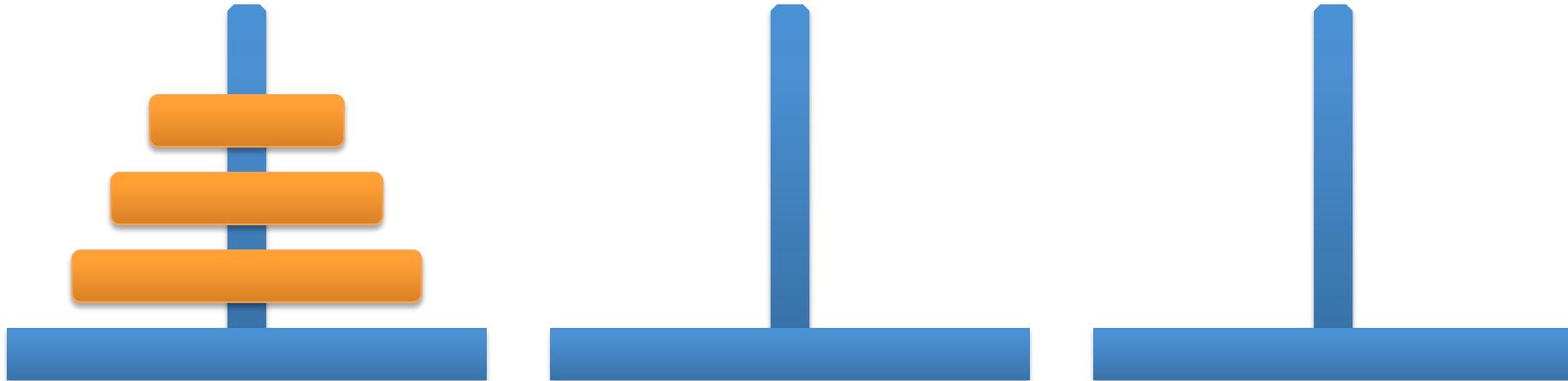
- game invented by Edouard Lucas in 1883
- three pins with discs of varying diameter



- **Goal:** move all discs from the left to the right pin
- **Rule 1:** only one disc may be moved at a time
- **Rule 2:** a bigger disc may not lie on top of a smaller one
- **Rule 3:** all discs except the one moved are on some pin

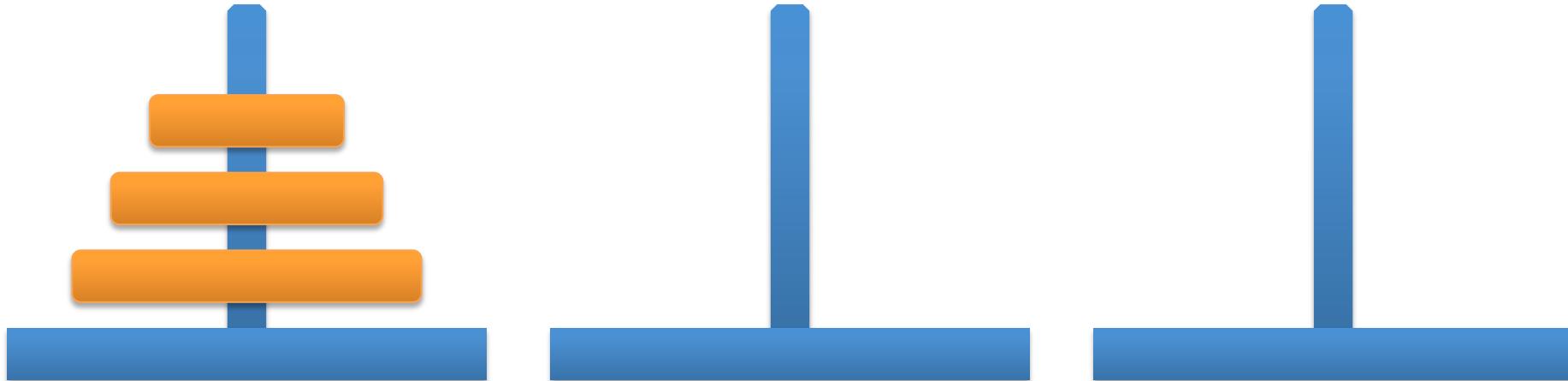
Towers of Hanoi

- **Solution:** move discs from left to right using the middle pin
 - move all discs (except the largest) from left pin to the middle pin using the right pin
 - move the largest disc from left to right pin
 - move all discs (except the largest) from middle pin to the right pin using the left pin



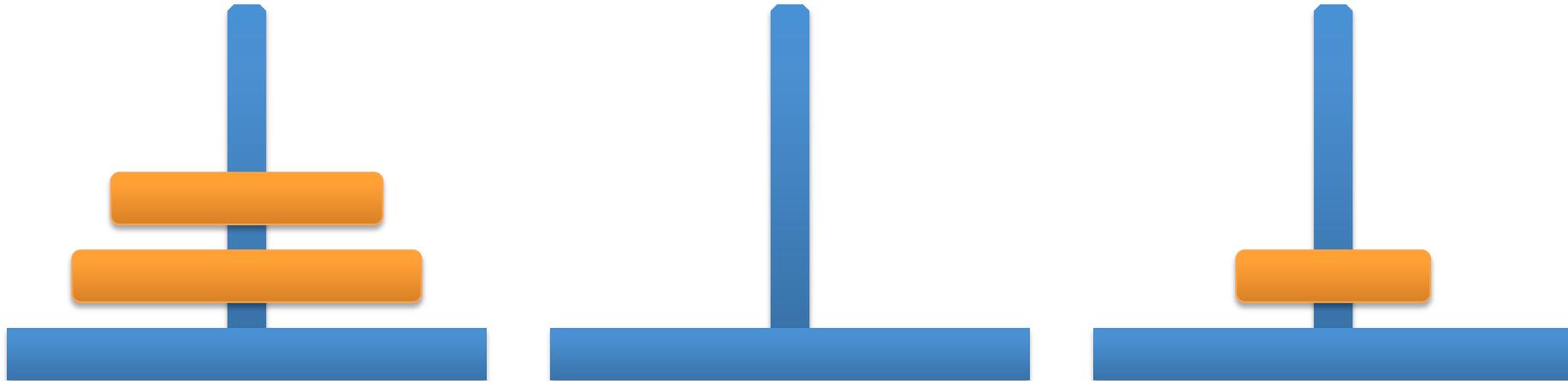
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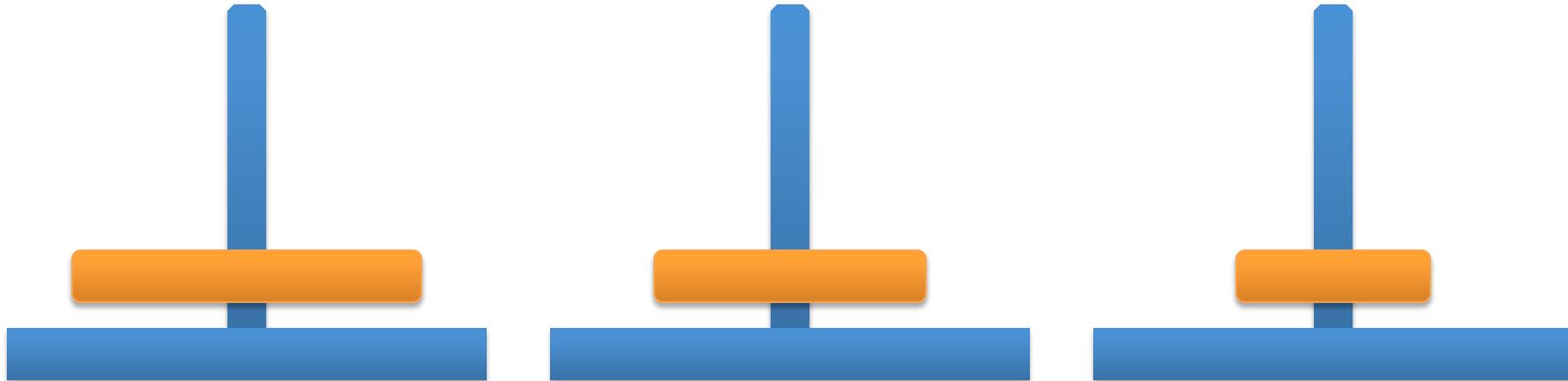
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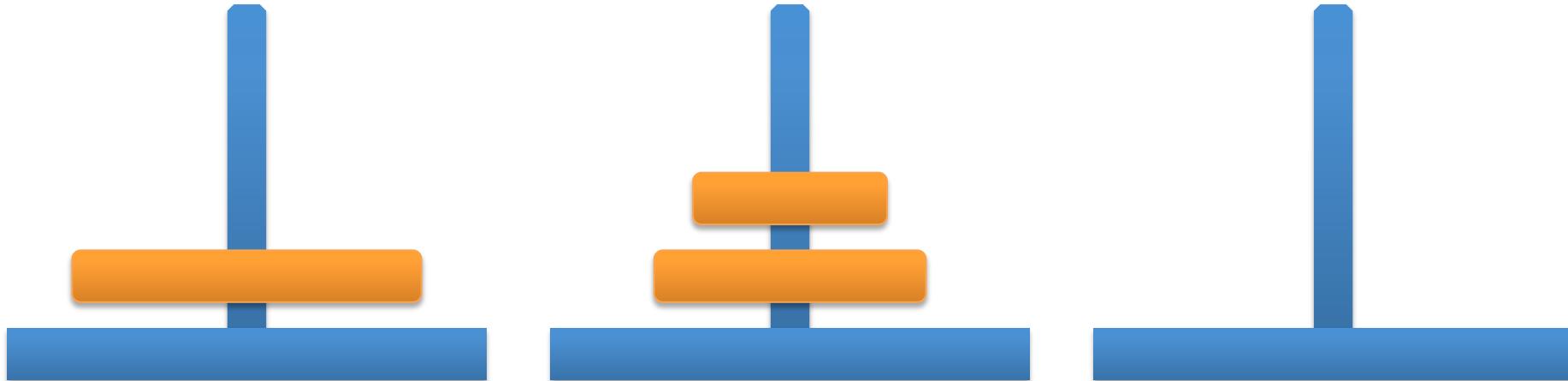
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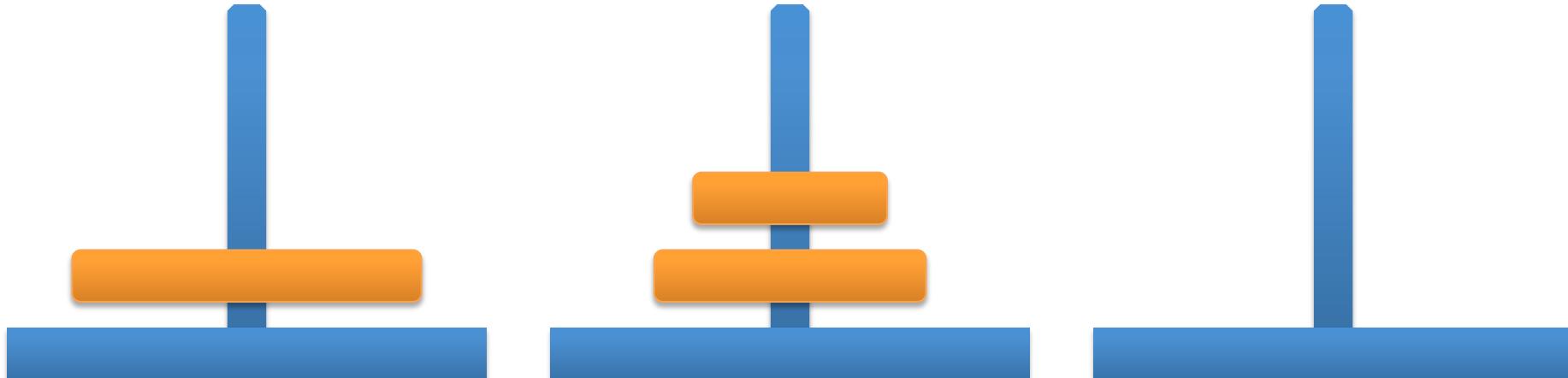
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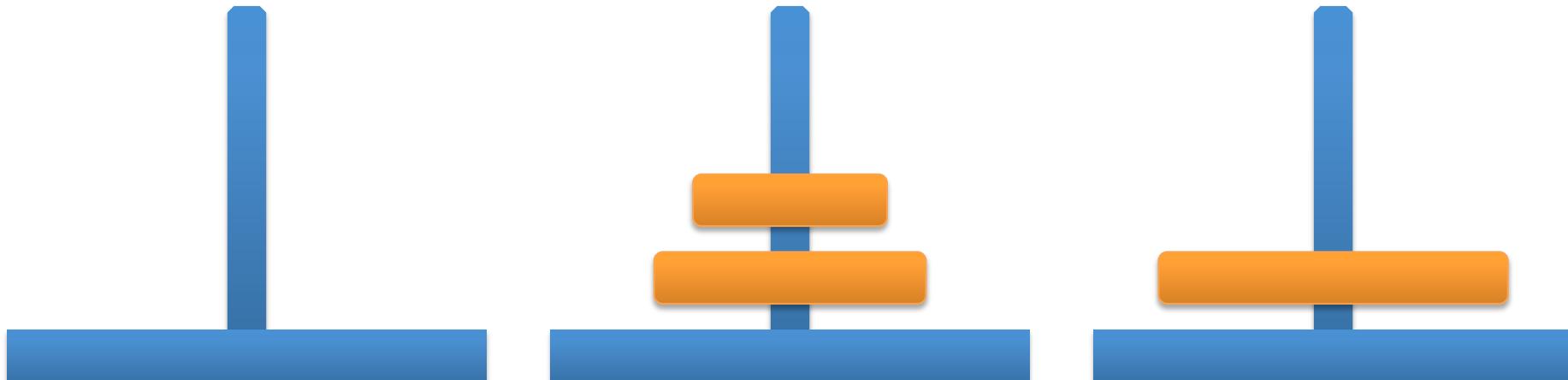
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Towers of Hanoi

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Towers of Hanoi

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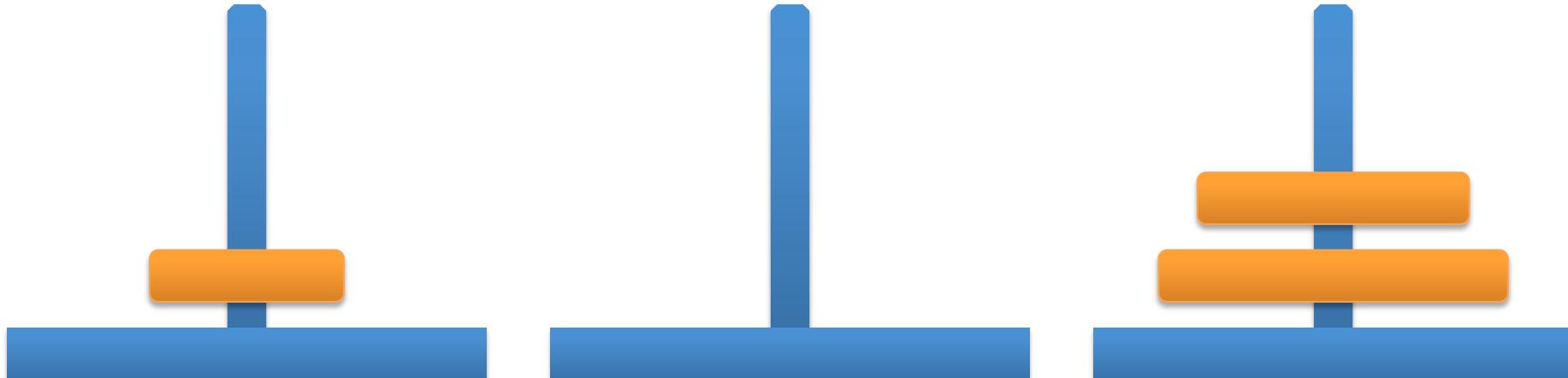
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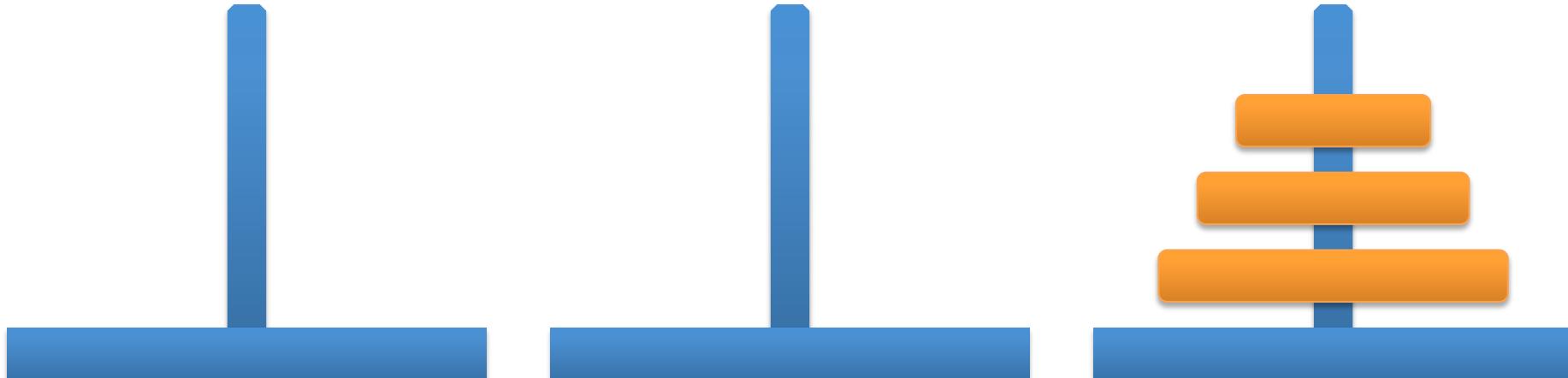
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Towers of Hanoi

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Towers of Hanoi

- **Solution:** move discs from left to right using the middle pin
 - move all discs (except the largest) from left pin to the middle pin using the right pin
 - move the largest disc from left to right pin
 - move all discs (except the largest) from middle pin to the right pin using the left pin
- this solution is inherently recursive
- can be formulated very simple by specifying individual moves
- to move n discs from pin 1 to pin 3 using pin 2, do:
 - move $n-1$ discs from pin 1 to pin 2 using pin 3
 - move disc from pin 1 to pin 3
 - move $n-1$ discs from pin 2 to pin 3 using pin 1

Towers of Hanoi

```
public class Move { public int from, to; // simply a pair of ints
    Move(int from, int to) { this.to = to; this.from = from; }
    public String toString() { return this.from+" -> "+this.to; }
}
public static List<Move> hanoi(int n, int from, int to, int using) {
    List<Move> moves = new ArrayList<Move>();
    if (n > 1) { moves.addAll(hanoi(n-1, from, using, to)); }
    moves.add(new Move(from, to));
    if (n > 1) { moves.addAll(hanoi(n-1, using, to, from)); }
}
...
System.out.println(hanoi(3, 1, 3 2));
```

RECURSIVE DATA STRUCTURES

Recursive Data Structures

- like functions, data structures can be recursive, too
- recursive class = contains a member variable of same class
- Example:

```
public class Student {  
    String name;  
    Student tutor;  
    public String toString() {  
        return name + tutor == null ? "" : "(" + tutor.name + ")";  
    }  
}
```

- useful to implement linked lists, trees, ...

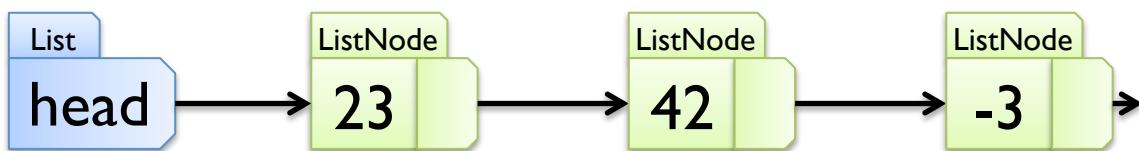
List ADT: Specification (revisited)

- data are arbitrary objects of class E
- operations are defined by the following interface

```
public interface List<E> {  
    public E get(int i);                      // get i-th integer (0-based)  
    public void set(int i, E elem);            // set i-th element  
    public int size();                         // return length of list  
    public void add(E elem);                   // add element at end  
    public void add(int i, E elem);            // insert element at pos. i  
    public void remove(int i);                 // remove i-th element  
}
```

Linked Lists

- arrays require copying when inserting in the middle
- avoid copying by using links from one element to the next
- **Idea:**
 - use a recursive data structure `ListNode`
 - one instance of this class per element
 - every node (except the last) refers to next element



List ADT: Design & Implementation 4

- Design 4: linked lists
- Implementation 4:

```
public class ListNode<E> {  
    private E elem;                      // one list element  
    private ListNode<E> next;             // next element  
    public ListNode(E elem, ListNode<E> next) {  
        this.elem = elem;  
        this.next = next;  
    }  
    ...  
}
```

List ADT: Implementation 4

- Implementation 4 (continued)

```
public class ListNode<E> {  
    private E elem;                      // one list element  
    private ListNode<E> next;             // next element  
    ...  
    public E get(int i) {  
        if (i == 0) { return this.elem; }  
        if (this.next == null) { throw new Index...Exception(); }  
        return this.next.get(i-1);  
    }  
    ...  
}
```

List ADT: Implementation 4

- Implementation 4 (continued)

```
public class ListNode<E> {  
    private E elem;                      // one list element  
    private ListNode<E> next;             // next element  
    ...  
    public void set(int i, E elem) {  
        if (i == 0) { this.elem = elem; } else {  
            if (this.next == null) { throw new Index...Exception(); }  
            this.next.set(i-1, elem);  
        }  
    }  
    ... }
```

List ADT: Implementation 4

- Implementation 4 (continued)

```
public class ListNode<E> {  
    private E elem;                      // one list element  
    private ListNode<E> next;             // next element  
    ...  
    public int size() {  
        int result = 1;  
        if (this.next != null) { result += this.next.size(); }  
        return result;  
    }  
    ...  
}
```

List ADT: Implementation 4

- Implementation 4 (continued)

```
public class ListNode<E> {  
    private E elem;                      // one list element  
    private ListNode<E> next;             // next element  
    ...  
    public void add(E elem) {  
        if (this.next != null) {  
            this.next.add(elem);  
        } else {  
            this.next = new ListNode<E>(elem, null);  
        }  
    } ... }
```

List ADT: Implementation 4

- Implementation 4 (continued)

```
public void add(E elem) {  
    if (this.next != null) {  
        this.next.add(elem);  
    } else {  
        this.next = new ListNode<E>(elem, null);  
    }  
}  
  
add(17)
```



List ADT: Implementation 4

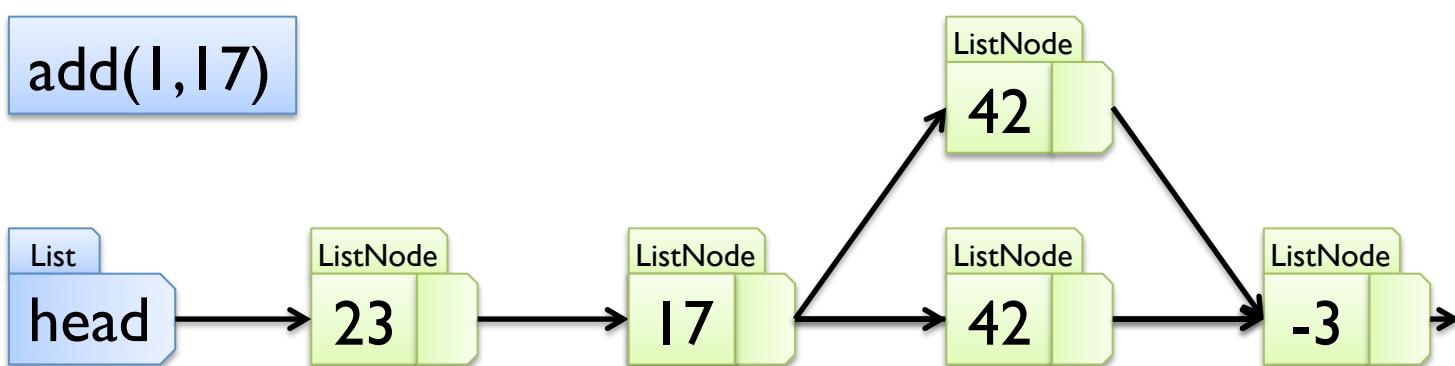
- Implementation 4 (continued)

```
public void add(int i, E elem) {  
    if (i == 0) {  
        this.next = new ListNode<E>(this.elem, this.next);  
        this.elem = elem;  
    } else {  
        if (this.next == null) {  
            if (i == 1) { this.add(elem); }      // end of list  
            else { throw new Index...Exception(); }  
        } else { this.next.add(i-1, elem); }  
    }  
}
```

List ADT: Implementation 4

- Implementation 4 (continued)

```
public void add(int i, E elem) {  
    if (i == 0) {  
        this.next = new ListNode<E>(this.elem, this.next);  
        this.elem = elem;  
    } else {  
        ...  
    }  
}
```



List ADT: Implementation 4

- Implementation 4 (continued)

```
public void remove(int i) {  
    if (i == 0) {  
        if (this.next == null) { throw new RuntimeException(); }  
        this.elem = this.next.elem;  
        this.next = this.next.next;  
    } else {  
        if (this.next == null) { throw new Index...Exception(); }  
        this.next.remove(i-1);  
    }  
}
```

List ADT: Implementation 4

- Implementation 4 (continued)

```
public void remove(int i) {  
    if (i == 0) {  
        if (this.next == null) { throw new RuntimeException(); }  
        this.elem = this.next.elem;  
        this.next = this.next.next;  
    } ...  
}
```

remove(1)



List ADT: Implementation 4

- Implementation 4 (continued):

```
public class LinkedList<E> implements List<E> {  
    private ListNode<E> head = null;  
  
    public E get(int i) {  
        if (i < 0) { throw new IllegalArgumentException(); }  
        if (head == null) { throw new Index...Exception(); }  
        return head.get(i);  
    }  
  
    ...  
}
```

List ADT: Implementation 4

- Implementation 4 (continued):

```
public class LinkedList<E> implements List<E> {  
    private ListNode<E> head = null; ...  
  
    public void set(int i, E elem) {  
        if (i < 0) { throw new IllegalArgumentException(); }  
        if (head == null) { throw new Index...Exception(); }  
        head.set(i, elem);  
    }  
    ...  
}
```

List ADT: Implementation 4

- Implementation 4 (continued):

```
public class LinkedList<E> implements List<E> {  
    private ListNode<E> head = null; ...  
  
    public int size() {  
        if (head == null) { return 0; }  
        return head.size();  
    }  
  
    ...  
}
```

List ADT: Implementation 4

- Implementation 4 (continued):

```
public class LinkedList<E> implements List<E> {  
    private ListNode<E> head = null; ...  
  
    public void add(E elem) {  
        if (head == null) {  
            head = new ListNode<E>(elem, null);  
        } else {  
            head.add(elem);  
        }  
    }  
    ...  
}
```

List ADT: Implementation 4

- Implementation 4 (continued):

```
public class LinkedList<E> implements List<E> { ...  
    public void add(int i, E elem) {  
        if (i < 0) { throw new IllegalArgumentException(); }  
        if (head == null) {  
            if (i > 0) { throw new Index...Exception(); }  
            head = new ListNode<E>(elem, null);  
        } else {  
            head.add(i, elem);  
        }  
    } ...  
}
```

List ADT: Implementation 4

- Implementation 4 (continued):

```
public class LinkedList<E> implements List<E> { ...  
    public void remove(int i) {  
        if (i < 0) { throw new IllegalArgumentException(); }  
        if (head == null) { throw new Index...Exception(); }  
        else if (head.getNext() == null) {  
            if (i > 0) { throw new Index...Exception(); }  
            head = null;  
        } else {  
            head.remove(i);  
        }  
    } }
```