



DM550/DM857

Introduction to Programming

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Operator Precedence

- expressions are evaluated left-to-right
 - Example: $64 - 24 + 2 == 42$
- **BUT**: like in mathematics, “*” binds more strongly than “+”
 - Example: $2 + 8 * 5 == 42$
- parentheses have highest precedence: $64 - (24 + 2) == 38$
- **PEMDAS** rule:
 - **P**arentheses “(<expr>)”
 - **E**xponentiation “**”
 - **M**ultiplication “*” and **D**ivision “/”, “//”, “%”
 - **A**ddition “+” and **S**ubtraction “-”

String Operations

- Addition “+” works on strings:
 - Example 1: `print("Hello w" + "orld!")`
 - Example 2: `print("4" + "2")`
- Multiplication “*” works on strings, if 2nd operands is integer:
 - Example: `print("Hej!" * 10)`
- Subtraction “-”, Division “/”, and Exponentiation “**” do **NOT** work on strings

Debugging Expressions

- most beginners struggle with common Syntax Errors:
 - check that all parentheses and quotes are closed
 - check that operators have two operands
 - sequential instruction should start on the same column or be separated by a semicolon “;”
- common Runtime Error due to misspelling variable names:
 - Example:

```
a = float(input()); b = float(input())  
reslut = a**b+b**a  
print(result)
```

Statements

- instructions in Python are called *statements*
- so far we know 2 different statements:
 - assignments “=”:
 - any expression is a statement

`c = a**2+b**2`

- as a grammar rule:

`<stmt> => <var> = <expr> | <expr>`

Comments

- programs are not only written, they are also read
- document program to provide intuition:
 - Example 1: `c = sqrt(a**2+b**2) # use Pythagoras`
 - Example 2: `x, y = y, x # swap x and y`
- all characters after the comment symbol “#” are ignored
 - Example: `x = 23 #+19`
results in `x` referring to the value `23`

Many Ways to Python Development

- browser-based development:
 - <https://trinket.io/features/python3>
- browser-based visualization:
 - <http://www.pythontutor.com/visualize.html>
- standard IDE for Python NOT recommend (IDLE)
- other Python(-enabled) IDEs:
<https://wiki.python.org/moin/IntegratedDevelopmentEnvironments>
- Thonny (incl. visualization): <http://thonny.org/>
- Pyzo + Miniconda/Anaconda: <http://pyzo.org/>
- or for something else: <https://ipython.org/>
- hardcore: use command line and a text editor :)

Code Café

- manned Code Cafe for students
- first time Wednesday, September 6
- last time Wednesday, December 20
- closed in Week 42 (efterårsferie)

- Mondays, 15.00 – 17.00, Nicky Cordua Mattsson
- Wednesdays, 15.00 – 17.00, Troels Risum Vigsøe Frimer
-
- Nicky and Troels can help with any coding related issues
- issues have to be related to some IMADA course (fx this one)



CALLING FUNCTIONS

Calling Functions

- so far we have seen four different *function calls*:
 - `input()`: reads a value from the keyboard
 - `sqrt(x)`: computes the square root of `x`
 - `type(x)`: returns the type of the value of `x`
 - `print(x)`: prints argument and returns `None`
- in general, a function call is also an expression:
 - `<expr> => ... | <function>(<arg1>, ..., <argn>)`
 - Example 1: `x = input()`
`print(type(x))`
 - Example 2: `from math import log`
`print(log(4398046511104, 2))`

Importing Modules

- we imported the `sqrt` function from the `math` module:

```
from math import sqrt
```

- alternatively, we can import the whole module:

```
import math
```

- using the built-in function “`dir(x)`” we see `math`’s functions:

```
acos  ceil  expm1  gamma  ldexp  pow  trunc
acosh cos   fabs   gcd    lgamma radians
asin  cosh  factorial  hypot  log    sin
asinh degrees floor  isclose  log10  sinh
atan  erf   fmod   isfinite  log1p  sqrt
atan2 erfc  frexp  isinf    log2   tan
atanh exp   fsum   isnan   modf   tanh
```

- access using “`math.<function>`”:
`c = math.sqrt(a**2+b**2)`

The Math Module

- contains 25 functions (trigonometric, logarithmic, ...):
 - Example:

```
x = input()
print(math.sin(x)**2+math.cos(x)**2)
```
- contains 2 constants (`math.e` and `math.pi`):
 - Example:

```
print(math.sin(math.pi / 2))
```
- contains 3 meta data (`__doc__`, `__file__`, `__name__`):
 - `print(math.__doc__)`
 - `print(math.frexp.__doc__)`
 - `print(type.__doc__)`

Type Conversion Functions

- Python has pre-defined functions for converting values
- `int(x)`: converts `x` into an integer
 - Example 1: `int("1234") == int(1234.9999)`
 - Example 2: `int(-3.999) == -3`
- `float(x)`: converts `x` into a float
 - Example 1: `float(42) == float("42")`
 - Example 2: `float("Hej!")` results in Runtime Error
- `str(x)`: converts `x` into a string
 - Example 1: `str(23+19) == "42"`
 - Example 2: `str(type(42)) == "<type 'int'>"`

DEFINING FUNCTIONS

Function Definitions

- functions are defined using the following grammar rule:

```
<func.def> => def <function>(<arg1>, ..., <argn>):  
                <instr1>; ...; <instrk>
```

- can be used to reuse code:

- Example:

```
def pythagoras():  
    c = math.sqrt(a**2+b**2)  
    print("Result:", c)  
a = 3; b = 4; pythagoras()  
a = 7; b = 15; pythagoras()
```

- functions are values: `type(pythagoras)`

Functions Calling Functions

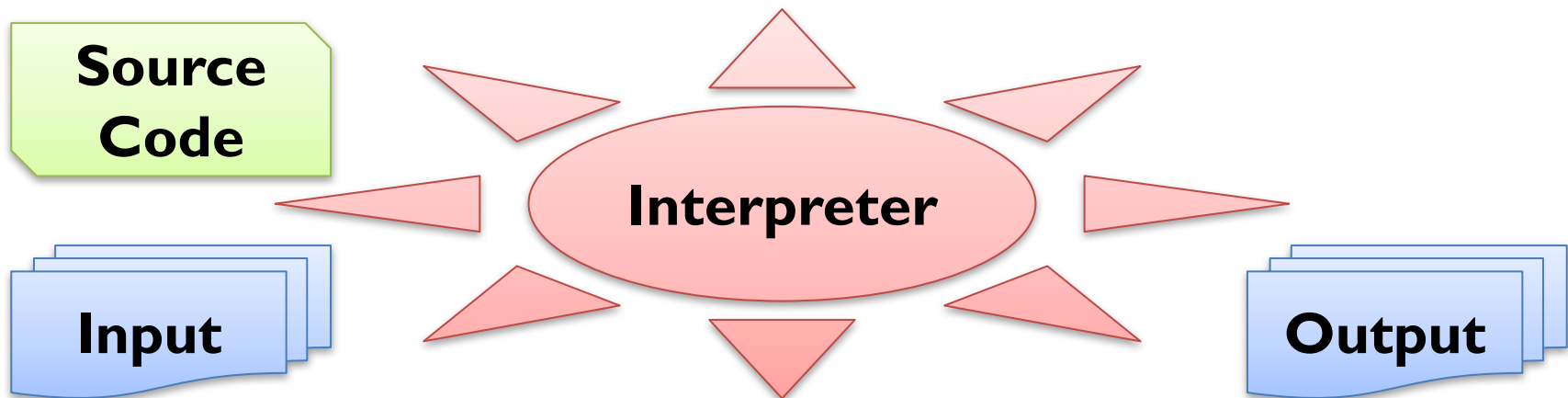
- functions can call other functions

- Example:

```
def white():  
    print("#" * 8)  
def black():  
    print("# " * 8)  
def all():  
    white(); black(); white(); black()  
    white(); black(); white(); black()  
all()
```


Executing Programs (Revisited)

- Program stored in a file (*source code* file)
- Instructions in this file executed top-to-bottom
- Interpreter executes each instruction



Functions Calling Functions

- functions can call other functions

- Example:



create new function
variable "white"

```
def white():  
    print("#" * 8)  
def black():  
    print("# " * 8)  
def all():  
    white(); black(); white(); black()  
    white(); black(); white(); black()  
all()
```

Functions Calling Functions

- functions can call other functions

- Example:

```
def white():
```

```
    print("#" * 8)
```



```
def black():
```

```
    print("# " * 8)
```

```
def all():
```

```
    white(); black(); white(); black()
```

```
    white(); black(); white(); black()
```

```
all()
```

create new function
variable "black"

Functions Calling Functions

- functions can call other functions

- Example:

```
def white():
```

```
    print("#" * 8)
```

```
def black():
```


```
    print("# " * 8)
```

```
def all():
```

```
    white(); black(); white(); black()
```

```
    white(); black(); white(); black()
```

```
all()
```



create new function
variable "all"

Functions Calling Functions

- functions can call other functions

- Example:

```
def white():
```

```
    print("#" * 8)
```

```
def black():
```

```
    print("# " * 8)
```

```
def all():
```

```
    white(); black(); white(); black()
```

```
    white(); black(); white(); black()
```



call function "all"

```
all()
```

Functions Calling Functions

- functions can call other functions

- Example:

```
def white():  
    print("#" * 8)
```

```
def black():  
    print("# " * 8)
```

```
def all():
```

```
    white(); black(); white(); black()
```

```
    white(); black(); white(); black()
```

```
all()
```



call function
"white"



Functions Calling Functions

- functions can call other functions

- Example:

```
def white():
```

```
    print("#" * 8)
```

```
def black():
```

```
    print("# " * 8)
```

```
def all():
```

```
    white(); black(); white(); black()
```

```
    white(); black(); white(); black()
```

```
all()
```



print

"#####"

Functions Calling Functions

- functions can call other functions

- Example:

```
def white():
```

```
    print("#" * 8)
```

```
def black():
```

```
    print("# " * 8)
```

```
def all():
```

```
    white() black(); white(); black()
```

```
    white(); black(); white(); black()
```

```
all()
```

call function "black"



Functions Calling Functions

- functions can call other functions

- Example:

```
def white():
```

```
    print("#" * 8)
```

```
def black():
```

```
    print("# " * 8)
```

```
def all():
```

```
    white(); black(); white(); black()
```

```
    white(); black(); white(); black()
```

```
all()
```



print

"# # # # # # # # "

Functions Calling Functions

- functions can call other functions

- Example:

```
def white():
```

```
    print("#" * 8)
```

```
def black():
```

```
    print("# " * 8)
```

```
def all():
```

```
    white(); black(); white(); black()
```

```
    white(); black(); white(); black()
```

```
all()
```

call function
"white"



Functions Calling Functions

- functions can call other functions

- Example:

```
def white():
```

```
    print("#" * 8)
```

```
def black():
```

```
    print("# " * 8)
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```
def all():
```

```
    white(); black(); white(); black()
```

```
    white(); black(); white(); black()
```

```
all()
```



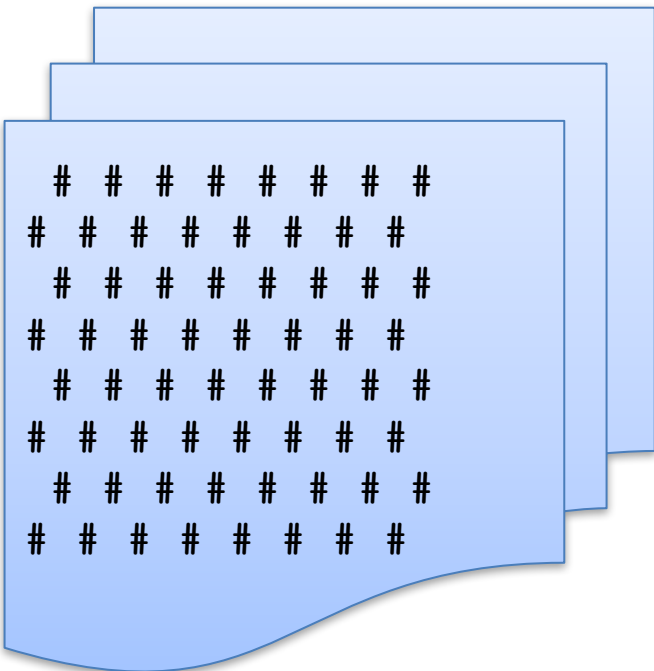
print

"#####"

Functions Calling Functions

- functions can call other functions

- Example:



```
def white():
```

```
    print("#" * 8)
```

```
def black():
```

```
    print("# " * 8)
```

```
def all():
```

```
    white(); black(); white(); black()
```

```
    white(); black(); white(); black()
```

```
all()
```

Parameters and Arguments

- we have seen functions that need arguments:
 - `math.sqrt(x)` computes square root of `x`
 - `math.log(x, base)` computes logarithm of `x` w.r.t. `base`
- arguments are assigned to parameters of the function
 - Example:

```
def pythagoras():  
    c = math.sqrt(a**2+b**2)  
    print("Result:", c)  
a = 3; b = 4; pythagoras()  
a = 7; b = 15; pythagoras()
```

Parameters and Arguments

- we have seen functions that need arguments:
 - `math.sqrt(x)` computes square root of `x`
 - `math.log(x, base)` computes logarithm of `x` w.r.t. `base`
- arguments are assigned to parameters of the function
 - Example:

```
def pythagoras(a, b):  
    c = math.sqrt(a**2+b**2)  
    print("Result:", c)  
a = 3; b = 4; pythagoras(a, b)  
a = 7; b = 15; pythagoras(a, b)
```

Parameters and Arguments

- we have seen functions that need arguments:
 - `math.sqrt(x)` computes square root of `x`
 - `math.log(x, base)` computes logarithm of `x` w.r.t. `base`
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 - Example:

```
def pythagoras(a, b):  
    c = math.sqrt(a**2+b**2)  
    print("Result:", c)  
  
pythagoras(3, 4)  
pythagoras(7, 15)
```

Parameters and Arguments

- we have seen functions that need arguments:
 - `math.sqrt(x)` computes square root of `x`
 - `math.log(x, base)` computes logarithm of `x` w.r.t. `base`
- arguments are assigned to parameters of the function
 - Example:

```
def pythagoras(a, b):  
    c = math.sqrt(a**2+b**2)  
    print("Result:", c)  
  
pythagoras(3, 4)  
pythagoras(2**3-1, 2**4-1)
```


Parameters and Arguments

- we have seen functions that need arguments:
 - `math.sqrt(x)` computes square root of `x`
 - `math.log(x, base)` computes logarithm of `x` w.r.t. `base`
- arguments are assigned to parameters of the function
 - Example:

```
def pythagoras(a, b):  
    c = math.sqrt(a**2+b**2)  
    print("Result:", c)  
  
pythagoras(3, 4)  
x = 2**3-1; y = 2**4-1  
pythagoras(x, y)
```

Variables are Local

- parameters and variables are local
- local = only available in the function defining them
- Example:

in module math:

```
def sqrt(x):
```

```
    ...
```

**x local to
math.sqrt**

**a local to
pythagora
s**

in our program:

```
def pythagoras(a, b):
```

```
    c = math.sqrt(a**2+b**2)
```

```
    print("Result:", c)
```

```
x = 3; y =4; pythagoras(x, y)
```

**b local to
pythagora
s**

**c local to
pythagora
s**

**x,y local to
__main__**

Stack Diagrams

`__main__`

x	→	3
y	→	4

`pythagoras`

a	→	3
b	→	4

`math.sqrt`

x	→	25
----------	----------	-----------

Tracebacks

- stack structure printed on runtime error
- Example:

```
def broken(x):  
    print(x / 0)
```

```
def caller(a, b):  
    broken(a**b)
```

```
caller(2,5)
```

```
Traceback (most recent call last):  
  File "test.py", line 5, in <module>  
    caller(2,5)  
  File "test.py", line 4, in caller  
    broken(a**b)  
  File "test.py", line 2, in broken  
    print(x/0)
```

ZeroDivisionError: integer division or modulo by zero

Return Values

- we have seen functions that return values:
 - `math.sqrt(x)` returns the square root of `x`
 - `math.log(x, base)` returns the logarithm of `x` w.r.t. `base`
- What is the return value of our function `pythagoras(a, b)`?
- special value `None` returned, if no return value given (*void*)
- declare return value using return statement: `return <expr>`
- Example:

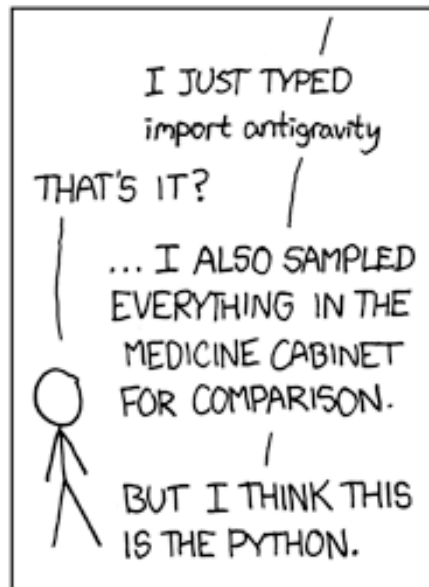
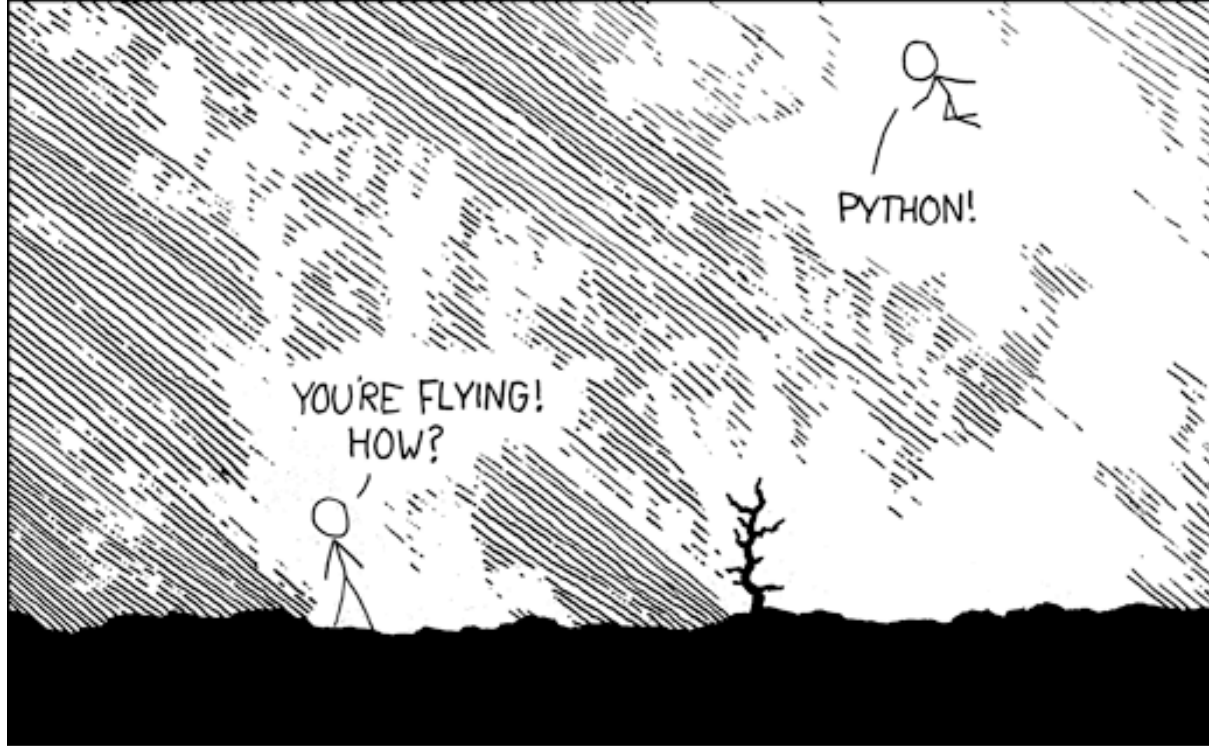
```
def pythagoras(a, b):  
    c = math.sqrt(a**2+b**2)  
    return c  
  
print(pythagoras(3, 4))
```

Motivation for Functions

- functions give names to blocks of code
 - easier to read
 - easier to debug
- avoid repetition
 - easier to make changes
- functions can be debugged separately
 - easier to test
 - easier to find errors
- functions can be reused (for other programs)
 - easier to write new programs

Debugging Function Definitions

- make sure you are using latest files (save, then run `python -i`)
- biggest problem for beginners is *indentation*
 - all lines on the same level must have the same indentation
 - mixing spaces and tabs is very dangerous
 - try to use only spaces – a good editor helps!
- do not forget to use “:” at end of first line
- indent body of function definition by e.g. 4 spaces



TURTLE GRAPHICS & INTERFACE DESIGN

Turtle Module

- available in most Python distributions
- easy to use (although requires some faith at the moment)
 - can be imported using `import turtle`
 - `t = turtle.Turtle()` creates new turtle `t`
 - `turtle.mainloop()` can be used at the end of the program
- two basic commands to the turtle
 - `t.fd(x)` advances turtle `t` by `x` units
 - `t.lt(x)` turns turtle `t` `x` degrees to the left

Simple Repetition

- drawing a square by e.g. 4x drawing a line and turning left
`t.fd(100); t.lt(90); t.fd(100); t.lt(90);`
`t.fd(100); t.lt(90); t.fd(100); t.lt(90)`
- simple repetition using for-loop `for <var> in range(<expr>):`
 `<instr1>; <instr2>`
- Example: `for i in range(4):`
 `print(i)`

Simple Repetition

- drawing a square by e.g. 4x drawing a line and turning left
t.fd(100); t.lt(90); t.fd(100); t.lt(90);
t.fd(100); t.lt(90); t.fd(100); t.lt(90)
- simple repetition using for-loop for <var> in range(<expr>):
 <instr₁>; <instr₂>
- Example: for i in range(4):
 t.fd(100)
 t.lt(90)

Encapsulation

- **Idea:** wrap up a block of code in a function
 - documents use of this block of code
 - allows reuse of code by using parameters
- **Example:**

```
def square(t):  
    for i in range(4):  
        t.fd(100)  
        t.lt(90)  
square(t)  
u = turtle.Turtle(); u.rt(90); u.fd(10); u.lt(90);  
square(u)
```

Generalization

- `square(t)` can be reused, but size of square is fixed
- **Idea:** generalize function by adding parameters
 - more flexible functionality
 - more possibilities for reuse

- Example 1:

```
def square(t, length):  
    for i in range(4):  
        t.fd(length)  
        t.lt(90)  
square(t, 100)  
square(t, 50)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def square(t, length):  
    for i in range(4):  
        t.fd(length)  
        t.lt(90)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, length):
```

```
    for i in range(4):
```

```
        t.fd(length)
```

```
        t.lt(90)
```


Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):  
    for i in range(n):  
        t.fd(length)  
        t.lt(90)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):  
    for i in range(n):  
        t.fd(length)  
        t.lt(360/n)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):
```

```
    angle = 360/n
```

```
    for i in range(n):
```

```
        t.fd(length)
```

```
        t.lt(angle)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):
```

```
    angle = 360/n
```

```
    for i in range(n):
```

```
        t.fd(length)
```

```
        t.lt(angle)
```

```
polygon(t, 4, 100)
```

```
polygon(t, 6, 50)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):  
    angle = 360/n  
    for i in range(n):  
        t.fd(length)  
        t.lt(angle)  
polygon(t, n=4, length=100)  
polygon(t, n=6, length=50)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):
```

```
    angle = 360/n
```

```
    for i in range(n):
```

```
        t.fd(length)
```

```
        t.lt(angle)
```

```
square(t, 100)
```

Generalization

- Example 2: replace square by regular polygon with n sides

```
def polygon(t, n, length):
```

```
    angle = 360/n
```

```
    for i in range(n):
```

```
        t.fd(length)
```

```
        t.lt(angle)
```

```
def square(t, length):
```

```
    polygon(t, 4, length)
```

```
square(t, 100)
```

Interface Design

- **Idea:** interface = parameters + semantics + return value
- should be general (= easy to reuse)
- but as simple as possible (= easy to read and debug)
- Example:

```
def circle(t, r):  
    circumference = 2*math.pi*r  
    n = 10  
    length = circumference / n  
    polygon(t, n, length)  
circle(t, 10)  
circle(t, 100)
```


Interface Design

- **Idea:** interface = parameters + semantics + return value
- should be general (= easy to reuse)
- but as simple as possible (= easy to read and debug)

- Example:

```
def circle(t, r, n):
```

```
    circumference = 2*math.pi*r
```

```
#    n = 10
```

```
    length = circumference / n
```

```
    polygon(t, n, length)
```

```
circle(t, 10, 10)
```

```
circle(t, 100, 40)
```

Interface Design

- **Idea:** interface = parameters + semantics + return value
- should be general (= easy to reuse)
- but as simple as possible (= easy to read and debug)

- Example:

```
def circle(t, r):
```

```
    circumference = 2*math.pi*r
```

```
    n = int(circumference // 3) + 1
```

```
    length = circumference / n
```

```
    polygon(t, n, length)
```

```
circle(t, 10)
```

```
circle(t, 100)
```

Refactoring

- we want to be able to draw arcs
- Example:

```
def arc(t, r, angle):  
    arc_length = 2*math.pi*r*angle/360  
    n = int(arc_length / 3) + 1  
    step_length = arc_length / n  
    step_angle = float(angle) / n
```

```
for i in range(n):  
    t.fd(step_length)  
    t.lt(step_angle)
```

Refactoring

- we want to be able to draw arcs
- Example:

```
def arc(t, r, angle):  
    arc_length = 2*math.pi*r*angle/360  
    n = int(arc_length / 3) + 1  
    step_length = arc_length / n  
    step_angle = float(angle) / n
```

```
def polyline(t, n, length, angle):  
    for i in range(n):  
        t.fd(length)  
        t.lt(angle)
```

Refactoring

- we want to be able to draw arcs
- Example:

```
def arc(t, r, angle):  
    arc_length = 2*math.pi*r*angle/360  
    n = int(arc_length / 3) + 1  
    step_length = arc_length / n  
    step_angle = float(angle) / n  
    polyline(t, n, step_length, step_angle)  
def polyline(t, n, length, angle):  
    for i in range(n):  
        t.fd(length)  
        t.lt(angle)
```

Refactoring

- we want to be able to draw arcs
- Example:

```
def polyline(t, n, length, angle):  
    for i in range(n):  
        t.fd(length)  
        t.lt(angle)
```

Refactoring

- we want to be able to draw arcs
- Example:

```
def polyline(t, n, length, angle):
```

```
    for i in range(n):
```

```
        t.fd(length)
```

```
        t.lt(angle)
```

```
def polygon(t, n, length):
```

```
    angle = 360/n
```

```
    polyline(t, n, length, angle):
```

Refactoring

- we want to be able to draw arcs
- Example:

```
def arc(t, r, angle):  
    arc_length = 2*math.pi*r*angle/360  
    n = int(arc_length / 3) + 1  
    step_length = arc_length / n  
    step_angle = float(angle) / n  
    polyline(t, n, step_length, step_angle)
```


Refactoring

- we want to be able to draw arcs
- Example:

```
def arc(t, r, angle):  
    arc_length = 2*math.pi*r*angle/360  
    n = int(arc_length / 3) + 1  
    step_length = arc_length / n  
    step_angle = float(angle) / n  
    polyline(t, n, step_length, step_angle)  
def circle(t, r):  
    arc(t, r, 360)
```

Simple Iterative Development

- first structured approach to develop programs:
 1. write small program without functions
 2. encapsulate code in functions
 3. generalize functions (by adding parameters)
 4. repeat steps 1–3 until functions work
 5. refactor program (e.g. by finding similar code)
- copy & paste helpful
 - reduces amount of typing
 - no need to debug same code twice

Debugging Interfaces

- interfaces simplify testing and debugging
- I. test if pre-conditions are given:
 - do the arguments have the right type?
 - are the values of the arguments ok?
- I. test if the post-conditions are given:
 - does the return value have the right type?
 - is the return value computed correctly?
- I. debug function, if pre- or post-conditions violated

GETTING YOUR HANDS DIRTY

Programming by Checklist ☺

1. Do you have an editor installed? (Preferably with syntax highlighting!)
2. Do you have a Python distribution installed?
3. Test the following programs:
 - a. `print("My name is Slartibartfast!")`
 - b. `import turtle; t = turtle.Turtle()
for i in range(4):
 t.fd(10); t.lt(270)`
 - c. `import turtle; t = turtle.Turtle()
list(map(lambda x:(t.fd(5*x),t.lt(120)),range(20)))`
4. Extend to a meaningful program and save it !