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Color Histograms as Feature Spaces for Representation of Images

A First Glimpse on Clustering

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Introduction to Computer Science

Melih Kandemir

University of Southern Denmark

DM534, Fall 2021





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SDU Categories of Feature Descriptors for Images

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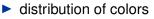
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texture

shapes (contoures)









SDU SOLO Color Histogram

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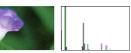
Color Histograms as Feature Spaces for Representation of Images

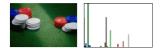
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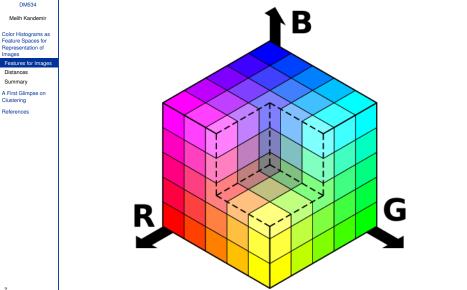
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- a histogram represents the distribution of colors over the pixels of an image
- definition of an color histogram:
 - choose a color space (RGB, HSV, HLS, ...)
 - choose number of representants (sample points) in the color space
 - possibly normalization (to account for different image sizes)

SDU 🎓 Color Space Example: RGB cube SYDDANSK UNIVERSITET





Impact of Number of Representants

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original images in full RGB space $(256^3 = 16, 777, 216)$



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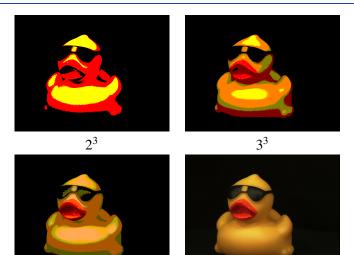
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 16^{3}

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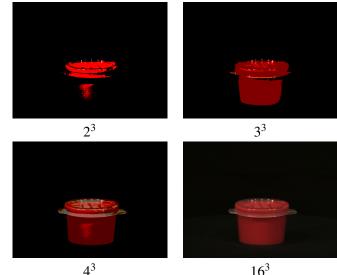
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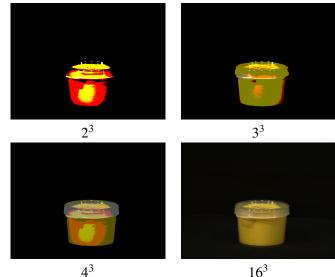
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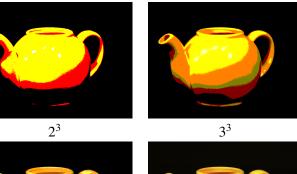
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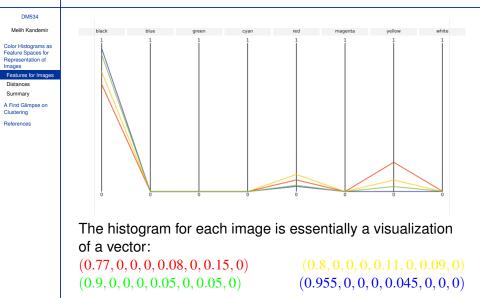


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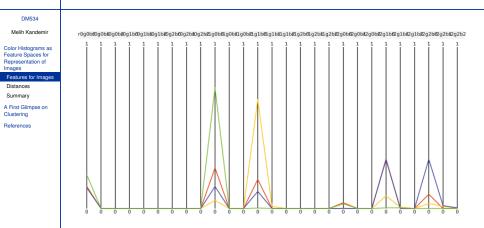


 16^{3}

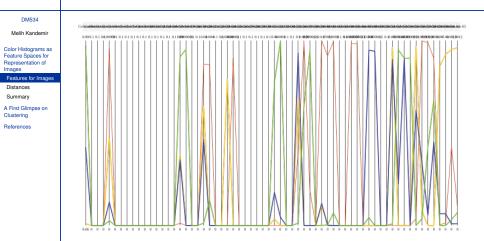
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SDU STREAM Impact of Number of Representants



SDU STRUCTURE Impact of Number of Representants







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Distances for Color Histograms

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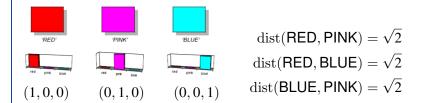
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Euclidean distance for images *P* and *Q* using the color histograms h_P and h_Q :

$$\operatorname{dist}(P,Q) = \sqrt{(h_P - h_Q) \cdot (h_P - h_Q)}$$



A 'psychologic' distance would consider that red is (in our perception) more similar to pink than to blue.

SDU Example for the Distance Computation of Histograms

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$$\operatorname{dist}(P,Q) = \sqrt{(h_P - h_Q) \cdot (h_P - h_Q)}$$

dist(RED, PINK) =
$$\sqrt{((1,0,0) - (0,1,0)) \cdot ((1,0,0) - (0,1,0))}$$

= $\sqrt{(1,-1,0) \cdot (1,-1,0)}$
= $\sqrt{(1 \cdot 1 + (-1) \cdot (-1) + 0 \cdot 0)}$
= $\sqrt{2}$



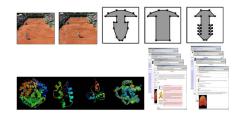
Similarity

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- Similarity (as given by some distance measure) is a central concept in data mining, e.g.:
 - clustering: group similar objects in the same cluster, separate dissimilar objects to different clusters
 - outlier detection: identify objects that are dissimilar (by some characteristic) from most other objects
- definition of a suitable distance measure is often crucial for deriving a meaningful solution in the data mining task
 - images
 - CAD objects
 - proteins
 - texts



SDU Spaces and Distance Functions

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Common distance measure for (Euclidean) feature vectors: L_P -norm

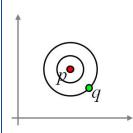
$$\operatorname{list}_{P}(p,q) = \left(|p_{1} - q_{1}|^{P} + |p_{2} - q_{2}|^{P} + \ldots + |p_{n} - q_{n}|^{P} \right)^{\frac{1}{P}}$$

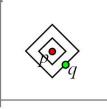
Euclidean norm (L_2) :

(

Manhattan norm (L_1) :

Maximum norm $(L_{\infty}, \text{ also: } L_{\text{max}}, \text{ supremum dist.}, Chebyshev dist.})$







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Weighted Euclidean norm:

dist
$$(p,q) = (w_1|p_1 - q_1|^2 + w_2|p_2 - q_2|^2 + \ldots + w_n|p_n - q_n|^2)^{\frac{1}{2}}$$

1

* note that we assume vectors to be row vectors here





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Ver Choice of a Distance Measure

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There are hundreds of distance functions [Deza and Deza, 2009].

- ▶ For time series: DTW, EDR, ERP, LCSS, ...
- For texts: Cosine and normalizations
- ► For sets based on intersection, union, ... (Jaccard)
- For clusters (single-link, average-link, etc.)
- For histograms: histogram intersection, "Earth movers distance", quadratic forms with color similarity
- ▶ With normalization: Canberra, ...

Note that:

Choosing the appropriate distance function can be seen as a part of "preprocessing".



Summary

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You learned in this section:

- distances (L_p-norms, weighted norms)
- color histograms as feature (vector) descriptors for images
- impact of the granularity of color histograms on similarity measures





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Purpose of Clustering

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- identify a finite number of categories (classes, groups: clusters) in a given dataset
- similar objects shall be grouped in the same cluster, dissimilar objects in different clusters
- "similarity" is highly subjective, depending on the application scenario



SDU A Dataset can be Clustered in Different Meaningful Ways



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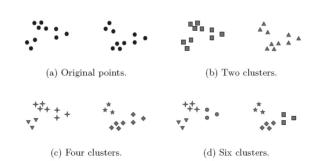


Figure 8.1. Different ways of clustering the same set of points.

(Figure from Tan et al. [2006].)





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DU Criteria of Quality: Cohesion and Separation

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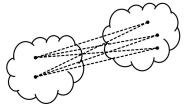
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- cohesion: how strong are the cluster objects connected (how similar, pairwise, to each other)?
- separation: how well is a cluster separated from other clusters?



small within cluster distances



large between cluster distances



Optimization of Cohesion

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Partitional clustering algorithms partition a dataset into *k* clusters, typically minimizing some cost function (compactness criterion), i.e., optimizing cohesion.



Assumptions for Partitioning Clustering

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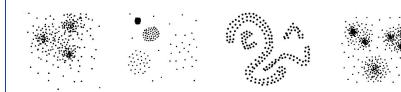
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Central assumptions for approaches in this family are typically:

- number k of clusters known (i.e., given as input)
- clusters are characterized by their compactness
- compactness measured by some distance function (e.g., distance of all objects in a cluster from some cluster representative is minimal)
- criterion of compactness typically leads to convex or even spherically shaped clusters







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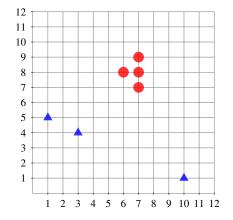
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- ▶ objects are points x = (x₁,..., x_d) in Euclidean vector space ℝ^d, dist = Euclidean distance (L₂)
- centroid μ_C : mean vector of all points in cluster C



$$u_{C_i} = \frac{1}{|C_i|} \cdot \sum_{o \in C_i} o$$

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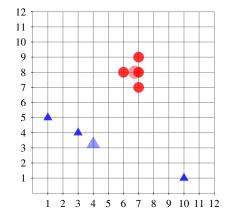
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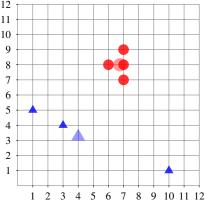
References

measure of compactness for a cluster C:

$$TD^2(C) = \sum_{p \in C} \operatorname{dist}(p, \mu_C)^2$$

(a.k.a. SSQ: sum of squares)

 measure of compactness for a clustering



$$TD^{2}(C_{1}, C_{2}, ..., C_{k}) = \sum_{i=1}^{k} TD^{2}(C_{i})$$

1.

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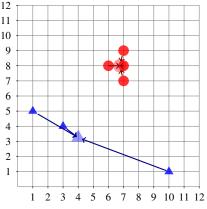
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measure of compactness for a cluster C:

$$TD^2(C) = \sum_{p \in C} \operatorname{dist}(p, \mu_C)^2$$

(a.k.a. SSQ: sum of squares)

 measure of compactness for a clustering



$$TD^{2}(C_{1}, C_{2}, \dots, C_{k}) = \sum_{i=1}^{k} TD^{2}(C_{i})$$

1.

Basic Algorithm [Forgy, 1965, Lloyd, 1982]

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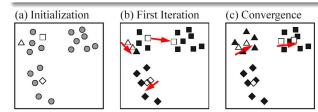
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Algorithm 2.1 (Clustering by Minimization of Variance)

- start with k (e.g., randomly selected) points as cluster representatives (or with a random partition into k "clusters")
- *repeat:*
 - assign each point to the closest representative
 - compute new representatives based on the given partitions (centroid of the assigned points)
- until there is no change in assignment





k-means

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k-means [MacQueen, 1967] is a variant of the basic algorithm:

- a centroid is immediately updated when some point changes its assignment
- k-means has very similar properties, but the result now depends on the order of data points in the input file

Note that:

The name "k-means" is often used indifferently for any variant of the basic algorithm, in particular also for Algorithm 2.1 [Forgy, 1965, Lloyd, 1982].





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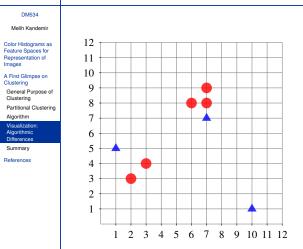
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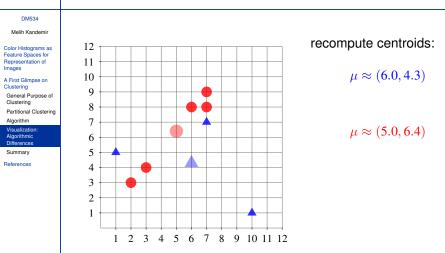
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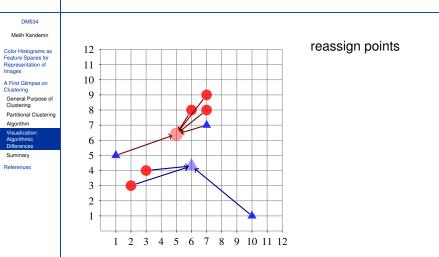
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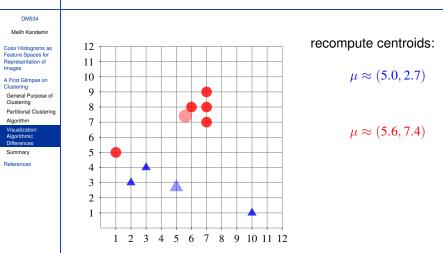




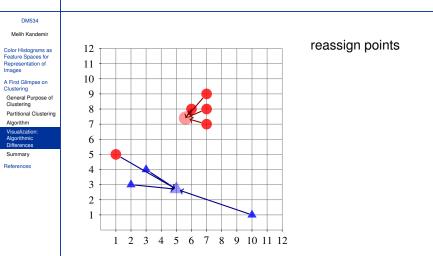


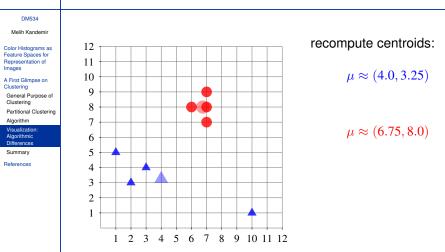




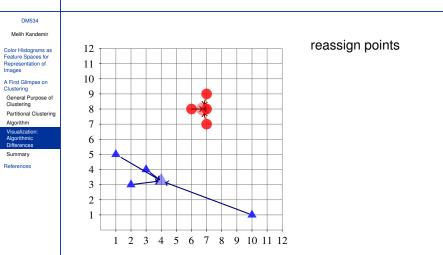




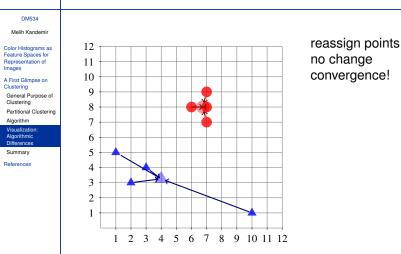




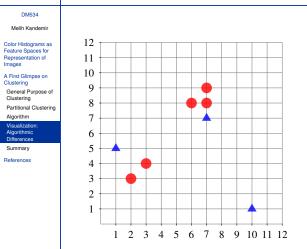




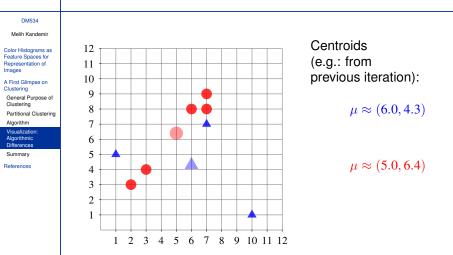




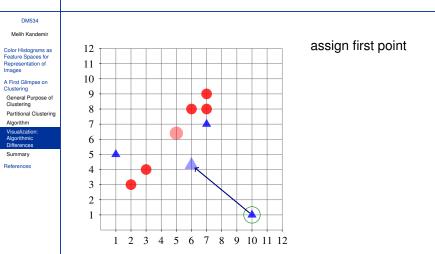




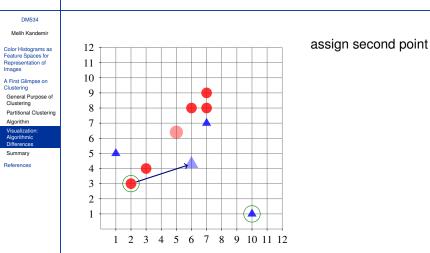


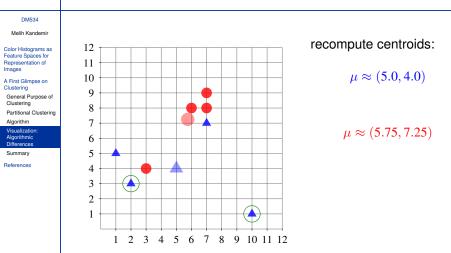




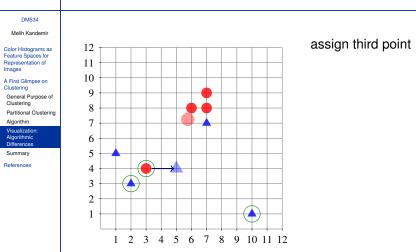


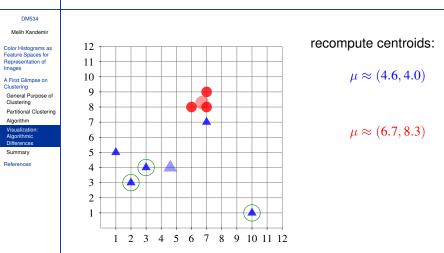




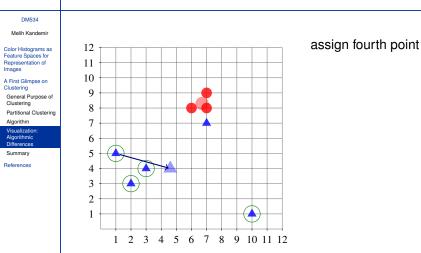




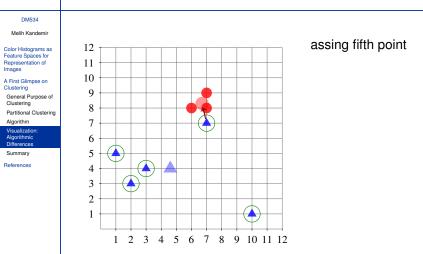


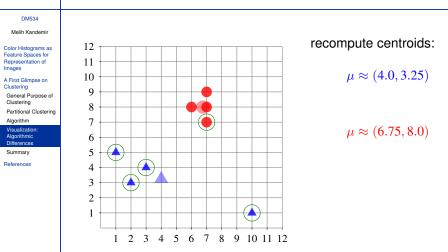




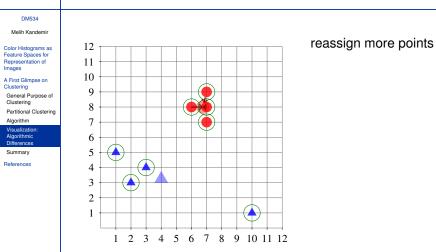




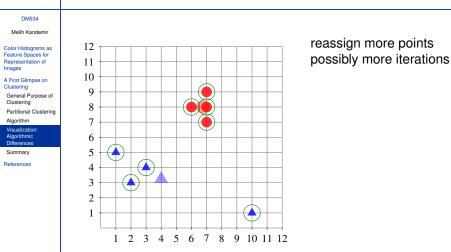




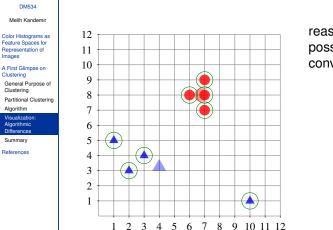






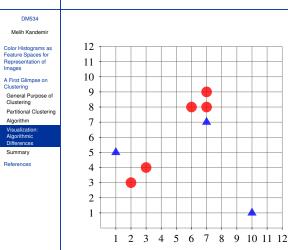


k-means Clustering – MacQueen Algorithm

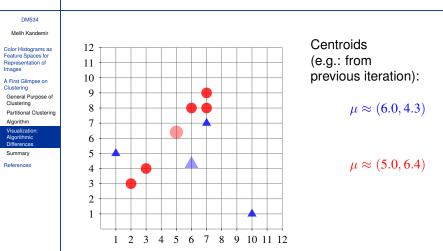


reassign more points possibly more iterations convergence

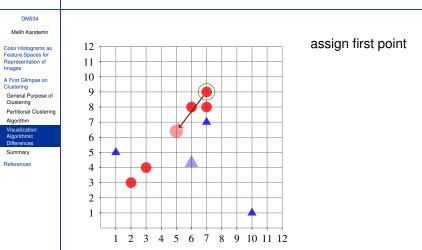
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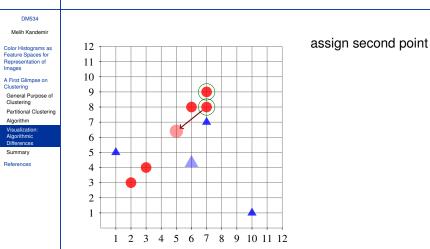
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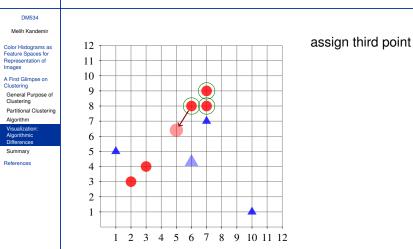
k-means Clustering – MacQueen Algorithm



k-means Clustering – MacQueen Algorithm

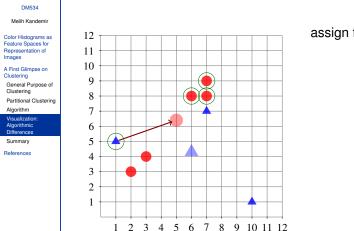


k-means Clustering – MacQueen Algorithm



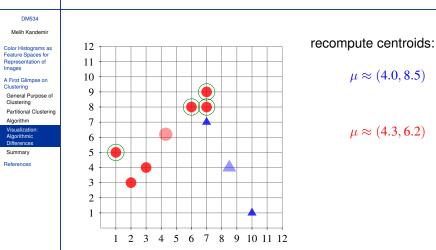
k-means Clustering – MacQueen Algorithm

Alternative Run – Different Order



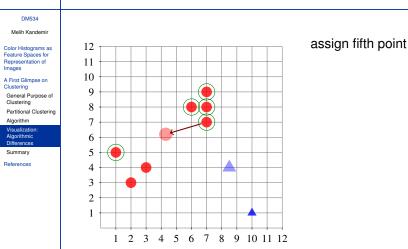
assign fourth point

k-means Clustering – MacQueen Algorithm



k-means Clustering – MacQueen Algorithm

Alternative Run – Different Order

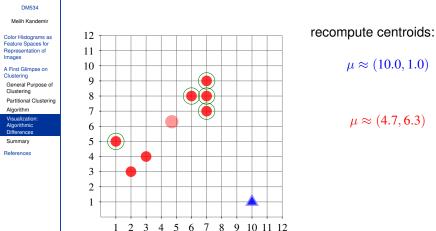


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k-means Clustering – MacQueen Algorithm

Alternative Run – Different Order

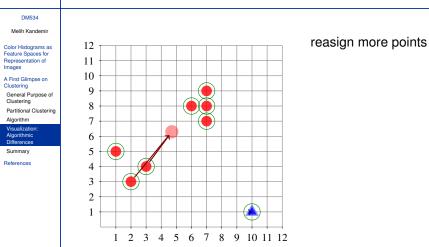


 $\mu \approx (10.0, 1.0)$

 $\mu \approx (4.7, 6.3)$

k-means Clustering – MacQueen Algorithm

Alternative Run – Different Order

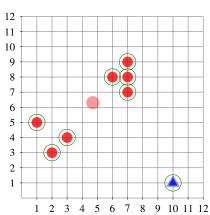


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Alternative Run – Different Order

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reasign more points possibly more iterations

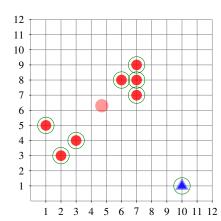
k-means Clustering – MacQueen Algorithm

Alternative Run – Different Order



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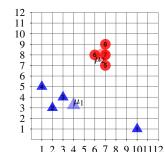
reasign more points possibly more iterations convergence

SDU ***** *k*-means Clustering – Quality

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First solution: $TD^2 = 61\frac{1}{2}$

$$\begin{split} & SSQ(\mu_1, p_1) = |4 - 10|^2 + |3.25 - 1|^2 = 36 + 5\frac{1}{16} = 41\frac{1}{16} \\ & SSQ(\mu_1, p_2) = |4 - 2|^2 + |3.25 - 3|^2 = 4 + \frac{1}{16} = 4\frac{1}{16} \\ & SSQ(\mu_1, p_3) = |4 - 3|^2 + |3.25 - 4|^2 = 1 + \frac{9}{16} = 1\frac{9}{16} \\ & SSQ(\mu_1, p_4) = |4 - 1|^2 + |3.25 - 5|^2 = 9 + 3\frac{1}{16} = 12\frac{1}{16} \\ & TD^2(C_1) = 58\frac{3}{4} \end{split}$$

$$\begin{split} &SSQ(\mu_2, p_5) = |6.75 - 7|^2 + |8 - 7|^2 = \frac{1}{16} + 1 = 1\frac{1}{16} \\ &SSQ(\mu_2, p_6) = |6.75 - 6|^2 + |8 - 8|^2 = \frac{9}{16} + 0 = \frac{9}{16} \\ &SSQ(\mu_2, p_7) = |6.75 - 7|^2 + |8 - 8|^2 = \frac{1}{16} + 0 = \frac{1}{16} \\ &SSQ(\mu_2, p_8) = |6.75 - 7|^2 + |8 - 9|^2 = \frac{1}{16} + 1 = 1\frac{1}{16} \\ &TD^2(C_2) = 2\frac{3}{4} \end{split}$$

Note:
$$SSQ(\mu, p) = Euclidean(\mu, p)^2 = L_2^2(\mu, p)$$
.

SDU ***** k-means Cl

k-means Clustering – Quality

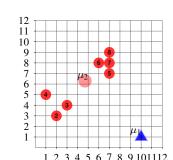
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 $SSQ(\mu_1, p_1) = |10 - 10|^2 + |1 - 1|^2 = 0$ $TD^2(C_1) = 0$

$$\begin{split} & SSQ(\mu_2,p_2) \approx |4.7-2|^2 + |6.3-3|^2 \approx 18.2 \\ & SSQ(\mu_2,p_3) \approx |4.7-3|^2 + |6.3-4|^2 \approx 8.2 \\ & SSQ(\mu_2,p_4) \approx |4.7-1|^2 + |6.3-5|^2 \approx 15.4 \\ & SSQ(\mu_2,p_5) \approx |4.7-7|^2 + |6.3-8|^2 \approx 5.7 \\ & SSQ(\mu_2,p_6) \approx |4.7-7|^2 + |6.3-8|^2 \approx 4.6 \\ & SSQ(\mu_2,p_7) \approx |4.7-7|^2 + |6.3-8|^2 \approx 8.2 \\ & SSQ(\mu_2,p_7) \approx |4.7-7|^2 + |6.3-9|^2 \approx 12.6 \\ & TD^2(C_2) \approx 72.86 \end{split}$$

First solution: $TD^2 = 61\frac{1}{2}$ Second solution: $TD^2 \approx 72.68$

Note:
$$SSQ(\mu, p) = Euclidean(\mu, p)^2 = L_2^2(\mu, p).$$

k-means Clustering – Quality

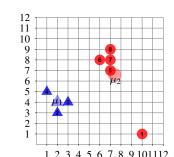
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 $SSQ(\mu_1, p_2) = |2 - 2|^2 + |4 - 3|^2 = 0 + 1 = 1$ $SSQ(\mu_1, p_3) = |2 - 3|^2 + |4 - 4|^2 = 1 + 0 = 1$ $SSQ(\mu_1, p_4) = |2 - 1|^2 + |4 - 5|^2 = 1 + 1 = 2$ $TD^2(C_1) = 4$

$$\begin{split} & SSQ(\mu_2, p_1) = |7.4 - 10|^2 + |6.6 - 1|^2 = 6\frac{19}{25} + 31\frac{9}{25} = 38\frac{3}{25} \\ & SSQ(\mu_2, p_5) = |7.4 - 7|^2 + |6.6 - 7|^2 = \frac{4}{25} + \frac{4}{25} = \frac{8}{25} \\ & SSQ(\mu_2, p_6) = |7.4 - 6|^2 + |6.6 - 8|^2 = 1\frac{24}{25} + 1\frac{24}{25} = 3\frac{23}{23} \\ & SSQ(\mu_2, p_7) = |7.4 - 7|^2 + |6.6 - 8|^2 = \frac{4}{25} + 1\frac{24}{25} = 2\frac{3}{25} \\ & SSQ(\mu_2, p_8) = |7.4 - 7|^2 + |6.6 - 9|^2 = \frac{4}{25} + 5\frac{19}{25} = 5\frac{23}{25} \\ & TD^2(C_2) = 50\frac{2}{5} \end{split}$$

First solution: $TD^2 = 61\frac{1}{2}$ Second solution: $TD^2 \approx 72.68$ Optimal solution: $TD^2 = 54\frac{2}{5}$

Note:
$$SSQ(\mu, p) = Euclidean(\mu, p)^2 = L_2^2(\mu, p).$$





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pros

- ► efficient: *O*(*k* · *n*) per iteration, number of iterations is usually in the order of 10.
- easy to implement, thus very popular

cons

- k-means converges towards a local minimum
- k-means (MacQueen-variant) is order-dependent
- deteriorates with noise and outliers (all points are used to compute centroids)
- clusters need to be convex and of (more or less) equal extension
- number k of clusters is hard to determine
- strong dependency on initial partition (in result quality as well as runtime)



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You learned in this section:

- What is Clustering?
- Basic idea for identifying "good" partitions into k clusters
- selection of representative points
- iterative refinement
- Iocal optimum
- k-means variants [Forgy, 1965, Lloyd, 1982, MacQueen, 1967]



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