



# **DM536 / DM550 Part I**

## **Introduction to Programming**

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# LIST PROCESSING

# Lists as Sequences

- lists are sequences of values
- lists can be constructed using “[” and “]”
- Example:
  - `[42, 23]`
  - `["Hello", "World", "!"]`
  - `["strings and", int, "mix", 2]`
  - `[]`
- lists can be nested, i.e., a list can contain other lists
- Example: `[[1, 2, 3], [4, 5, 6], [7, 8, 9]]`
- lists are normal values, i.e., they can be printed, assigned etc.
- Example:
  - `x = [1, 2, 3]`
  - `print x, [x, x], [[x, x], x]`

# Mutable Lists

- lists can be accessed using indices
- lists are mutable, i.e., they can be changed destructively
- Example:

```
x = [1, 2, 3]
```

```
print x[1]
```

```
x[1] = 4
```

```
print x, x[1]
```

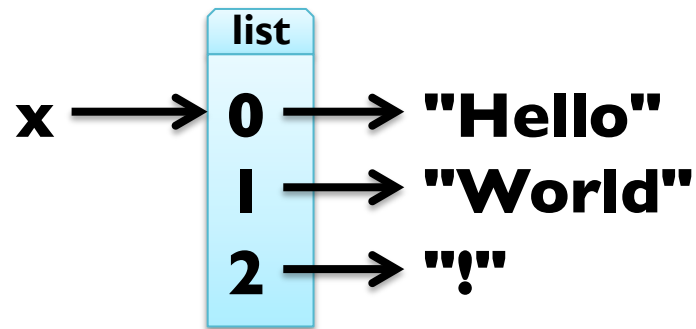
- `len(object)` and negative values work like for strings
- Example:

```
x[2] == x[-1]
```

```
x[1] == x[len(x)-2]
```

# Stack Diagrams with Lists

- lists can be viewed as mappings from indices to elements
- Example 1:  $x = ["\text{Hello}", "\text{World}", "!"]$



- Example 2:  $x = [[23, 42, -3.0], "\text{Bye!}"]$



# Traversing Lists

- `for` loop consecutively assigns variable to elements of list
- Example: print squares of numbers from 1 to 10  
for x in [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]:  
    print x\*\*2
- arithmetic sequences can be generated using `range` function:
  - `range([start,] stop[, step])`
- Example:  
    `range(4) == [0, 1, 2, 3]`  
    `range(1, 11) == [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]`  
    `range(9, 1, -2) == [9, 7, 5, 3]`  
    `range(1, 10, 2) == [1, 3, 5, 7, 9]`

# Traversing Lists

- `for` loop consecutively assigns variable to elements of list

- general form

```
for element in my_list:  
    print element
```

- iteration through list with indices:

```
for index in range(len(my_list)):  
    element = my_list[index]  
    print element
```

- Example: in-situ update of list

```
x = [8388608, 43980465 | | | 04, 0.125]
```

```
for i in range(len(x)):
```

```
    x[i] = math.log(x[i], 2)
```

# List Operations

- like for strings, “+” concatenates two lists

- Example:

$[1, 2, 3] + [4, 5, 6] == \text{range}(1, 7)$

$[[23, 42] + [-3.0]] + ["Bye!"] == [[23, 42, -3.0], "Bye!"]$

- like for strings, “\* n” with integer n produces n copies

- Example:

$\text{len}(["I", "love", "penguins!"] * 100) == 300$

$(\text{range}(1, 3) + \text{range}(3, 1, -1)) * 2 == [1, 2, 3, 2, 1, 2, 3, 2]$



# List Slices

- slices work just like for strings
- Example: 

```
x = ["Hello", 2, "u", 2, "!"]  
x[2:4] == ["u", 2]  
x[2:] == x[-3:len(x)]  
y = x[:]      # make a copy (lists are mutable!)
```
- **BUT:** we can also assign to slices!
- Example: 

```
x[1:4] = ["to", "you", "too"]  
x == ["Hello", "to", "you", "too", "!"]  
x[1:3] = ["to me"]  
x == ["Hello", "to me", "too", "!"]  
x[2:3] = []  
x == ["Hello", "to me", "!"]
```

# List Methods

- appending elements to the end of the list (destructive)
- Example: `x = [5, 3, 1]`  
`y = [2, 4, 6]`  
for e in y: `x.append(e)`
- Note: `x += [e]` would create new list in each step!
- also available as method: `x.extend(y)`
- sorting elements in ascending order (destructive)
- Example: `x.sort()`  
`x == range(1, 7)`
- careful with destructive updates: `x = x.sort()`

# Higher-Order Functions (map)

- Example 1: new list with squares of all elements of a list

```
def square_all(x):
```

```
    res = []
```

```
    for e in x:    res.append(e**2)
```

```
    return res
```

- Example 2: new list with all elements increased by one

```
def increment_all(x):
```

```
    res = []
```

```
    for e in x:    res.append(e+1)
```

```
    return res
```

# Higher-Order Functions (map)

- these *map* operations have an identical structure:

```
res = []
```

```
for e in x: res.append(e**2)
```

```
return res
```

```
res = []
```

```
for e in x: res.append(e+1)
```

```
return res
```

- Python has generic function `map(function, sequence)`
- Implementation idea:

```
def map(function, sequence):
```

```
    res = []
```

```
    for e in sequence:
```

```
        res.append(function(e))
```

```
    return res
```

# Higher-Order Functions (map)

- these *map* operations have an identical structure:

```
res = []  
for e in x: res.append(e**2)  
return res
```

```
res = []  
for e in x: res.append(e+1)  
return res
```

- Python has generic function `map(function, sequence)`
- Example:

```
def square(x):      return x**2
```

```
def increment(x):   return x+1
```

```
def square_all(x):  
    return map(square, x)
```

```
def increment_all(x):  
    return map(increment, x)
```

# Higher-Order Functions (filter)

- Example 1: new list with elements greater than 42

```
def filter_greater42(x):
```

```
    res = []
```

```
    for e in x:
```

```
        if e > 42:    res.append(e)
```

```
    return res
```

- Example 2: new list with elements whose length is smaller 3

```
def filter_len_smaller3(x):
```

```
    res = []
```

```
    for e in x:
```

```
        if len(e) < 3:    res.append(e)
```

```
    return res
```

# Higher-Order Functions (filter)

- these *filter* operations have an identical structure:

```
res = []
```

```
for e in x:
```

```
    if e > 42: res.append(e)
```

```
return res
```

```
res = []
```

```
for e in x:
```

```
    if len(e) < 3: res.append(e)
```

```
return res
```

- Python has generic function `filter(function, iterable)`
- Implementation idea:

```
def filter(function, iterable):
```

```
    res = []
```

```
    for e in iterable:
```

```
        if function(e): res.append(e)
```

```
    return res
```

# Higher-Order Functions (filter)

- these *filter* operations have an identical structure:

```
res = []
```

```
for e in x:
```

```
    if e > 42: res.append(e)
```

```
return res
```

```
res = []
```

```
for e in x:
```

```
    if len(e) < 3: res.append(e)
```

```
return res
```

- Python has generic function `filter(function, iterable)`
- Example:

```
def greater42(x):
```

```
    return x > 42
```

```
def len_smaller3(x):
```

```
    return len(x) < 3
```

```
def filter_greater42(x):
```

```
    return filter(greater42, x)
```

```
def filter_len_smaller3(x):
```

```
    return filter(len_smaller3, x)
```



# Higher-Order Functions (reduce)

- Example 1: computing factorial using range

```
def mul_all(x):
```

```
    prod = 1
```

```
    for e in x:    prod *= e           # prod = prod * e
```

```
    return prod
```

```
def factorial(n):
```

```
    return mul_all(range(1,n+1))
```

- Example 2: summing all elements in a list

```
def add_all(x):
```

```
    sum = 0
```

```
    for e in x:    sum += e           # sum = sum + e
```

```
    return sum
```

# Higher-Order Functions (reduce)

- these *reduce* operations have an identical structure:

```
prod = 1
```

```
for e in x: prod *= e
```

```
return prod
```

```
sum = 0
```

```
for e in x: sum += e
```

```
return sum
```

- Python has generic function `reduce(function, sequence, initial)`
- Implementation idea:

```
def reduce(function, sequence, initial):
```

```
    result = initial
```

```
    for e in sequence:
```

```
        result = function(result, e)
```

```
    return result
```

# Higher-Order Functions (reduce)

- these *reduce* operations have an identical structure:

```
prod = 1
```

```
for e in x: prod *= e
```

```
return prod
```

```
sum = 0
```

```
for e in x: sum += e
```

```
return sum
```

- Python has generic function `reduce(function, sequence, initial)`
- Example:

```
def add(x,y): return x+y
```

```
def mul(x,y): return x*y
```

```
def add_all(x):
```

```
    return reduce(add, x, 0)
```

```
def mul_all(x):
```

```
    return reduce(mul, x, 1)
```

# Deleting Elements

- there are three different ways to delete elements from list
- if you know index and want the element, use `pop(index)`
- Example: 

```
my_list = [23, 42, -3.0, 47 | | ]  
my_list.pop(1) == 42  
my_list == [23, -3.0, 47 | | ]
```
- if you do not know index, but the element, use `remove(value)`
- Example: 

```
my_list.remove(-3.0)  
my_list == [23, 47 | | ]
```
- if you know the index, you can use the `del` statement
- Example: 

```
del my_list[0]  
my_list == [47 | | ]
```

# Deleting Elements

- there are three different ways to delete elements from list
- as we have seen, you can also use slices to delete elements
- Example: 

```
my_list = [23, 42, -3.0, 47 | | ]  
my_list[2:] = []  
my_list == [23, 42]
```
- alternatively, you can use `del` together with slices
- Example: 

```
my_list = my_list * 3  
del my_list[:3]  
my_list == [42, 23, 42]
```

# Lists vs Strings

- string = sequence of letters
- list = sequence of values
- convert a string into a list using the built-in `list()` function
- Example: `list("Hej hop") == ["H", "e", "j", " ", "h", "o", "p"]`
- split up a string into a list using the `split(sep)` method
- Example: `"Slartibartfast".split("a") == ["Sl", "rtib", "rtf", "st"]`
- reverse operation is the `join(sequence)` method
- Example: `" and ".join(["A", "B", "C"]) == "A and B and C"`  
`"".join(["H", "e", "j", " ", "h", "o", "p"]) = "Hej Hop"`

# Objects and Values

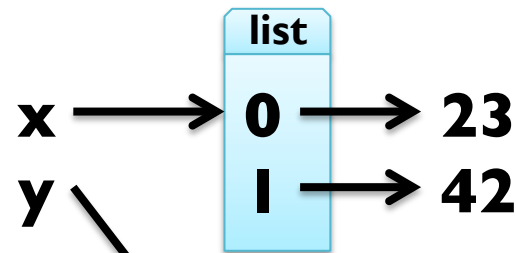
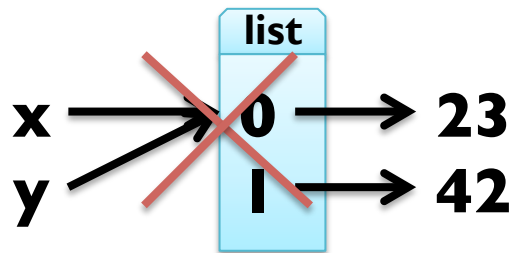
- two possible stack diagrams for `a = "mango"; b = "mango"`



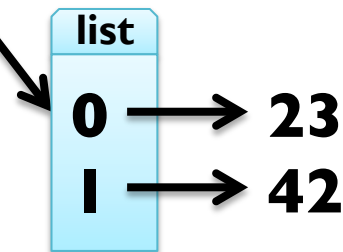
- we can check identity of objects using the `is` operator

- Example: `a is b == True`

- two possible stack diagrams for `x = [23, 42]; y = [23, 42]`



- Example: `x is y == False`



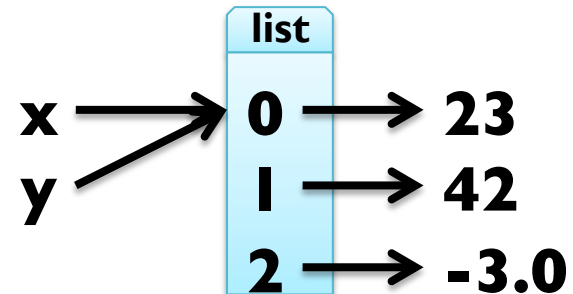
# Aliasing

- when assigning  $y = x$ , both variables refer to same object

- Example:  $x = [23, 42, -3.0]$

$y = x$

$x \text{ is } y == \text{True}$



- here, there are two *references* to one (*aliased*) object

- fine for immutable objects (like strings)

- problematic for mutable objects (like lists)

- Example:  $y[2] = 4711$

$x == [23, 42, 4711]$

- HINT: when unsure, always copy list using  $y = x[:]$



# List Arguments

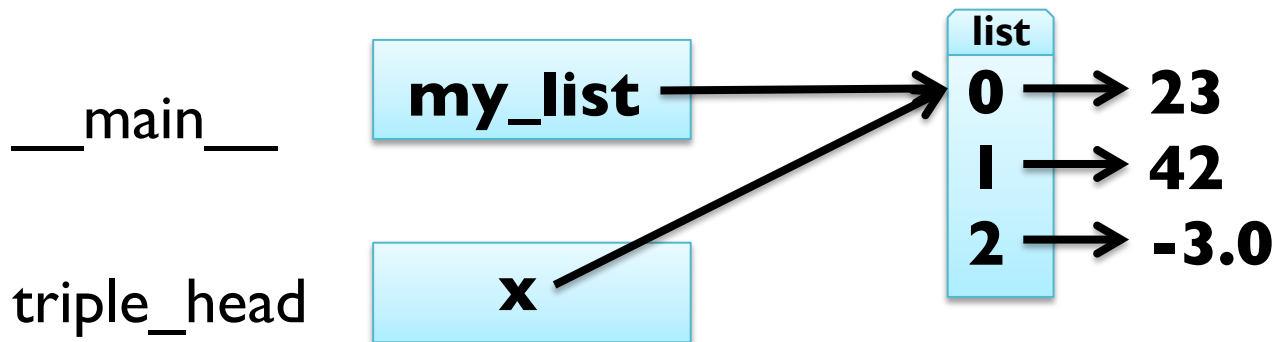
- lists passed as arguments to functions can be changed
- Example: tripling the first element

```
def triple_head(x):
```

```
    x[:1] = [x[0]]*3
```

```
my_list = [23, 42, -3.0]
```

```
triple_head(my_list)
```



# List Arguments

- lists passed as arguments to functions can be changed
- Example: tripling the first element

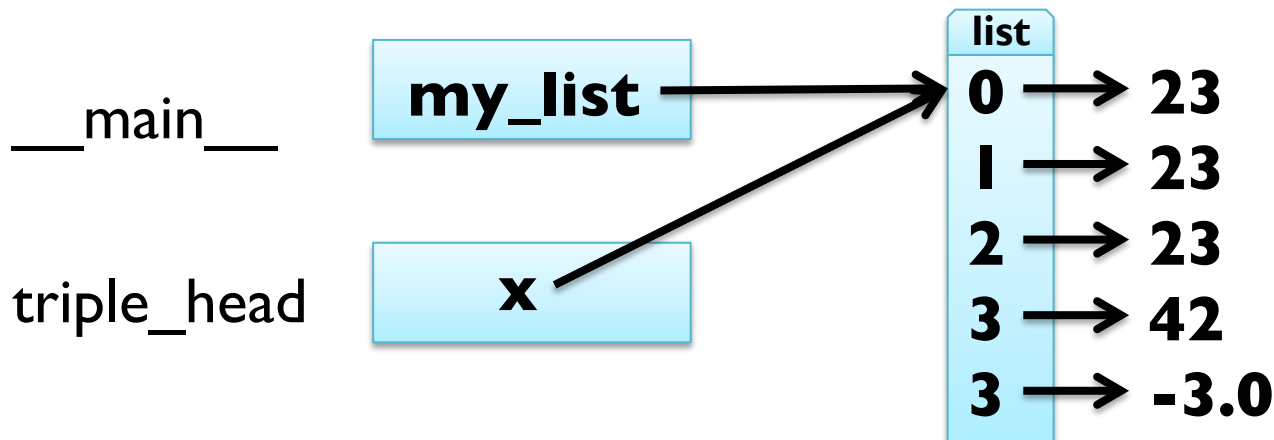
```
def triple_head(x):
```

```
    x[:1] = [x[0]]*3
```

```
my_list = [23, 42, -3.0]
```

```
triple_head(my_list)
```

```
my_list == [23, 23, 23, 42, -3.0]
```



# List Arguments

- lists passed as arguments to functions can be changed
- some operations change object
  - assignment using indices
  - `append(object)` method
  - `extend(iterable)` method
  - `sort()` method
  - `del` statement
- some operations return a new object
  - access using slices
  - `strip()` method
  - “+” on strings and lists
  - “\* n” on strings and lists

# Debugging Lists

- working with mutable objects like lists requires attention!
  1. many list methods return **None** and modify destructively
    - `word = word.strip()` makes sense
    - `t = t.sort()` does **NOT!**
  2. there are many ways to do something – stick with one!
    - `t.append(x)` or `t = t + [x]`
    - use either `pop`, `remove`, `del` or slice assignment for deletion
  3. make copies when you are unsure!
    - Example:

```
...
sorted_list = my_list[:]
sorted_list.sort()
...
```

# DICTIONARIES

# Generalized Mappings

- list = mapping from integer indices to values
- dictionary = mapping from (almost) any type to values
- indices are called *keys* and pairs of keys and values *items*
- empty dictionaries created using curly braces “{}”
- Example: `en2da = {}`
- keys are assigned to values using same syntax as for sequences
- Example: `en2da["queen"] = "dronning"`  
`print en2da`
- curly braces “{” and “}” can be used to create dictionary
- Example: `en2da = {"queen" : "dronning", "king" : "konge"}`

# Dictionary Operations

- printing order can be different: `print en2da`
- access using indices: `en2da["king"] == "konge"`
- `KeyError` when key not mapped: `print en2da["prince"]`
- length is number of items: `len(en2da) == 2`
- `in` operator tests if key mapped: `"king" in en2da == True`  
`"prince" in en2da == False`
- `keys()` method gives list of keys:  
`en2da.keys() == ["king", "queen"]`
- `values()` method gives list of values:  
`en2da.values() == ["konge", "dronning"]`
- useful e.g. for test if value is used:  
`"prins" in en2da.values() == False`

# Dictionaries as Sets

- dictionaries can be used as sets
- **Idea:** assign `None` to all elements of the set
- Example: representing the set of primes smaller than 20  
`primes = {2: None, 3: None, 5: None, 7: None, 11: None, 13: None, 17: None, 19: None}`
- then `in` operator can be used to see if value is in set
- Example:  
`15 in primes == False`  
`17 in primes == True`
- for lists, needs steps proportional to number of elements
- for dictionary, needs (almost) constant number of steps



# Counting Letter Frequency

- **Goal:** count frequency of letters in a string (*histogram*)
- many possible implementations, e.g.:
  - create 26(+3?) counter variables for each letter!; use chained conditionals (`if ... elif ... elif ...`) to increment
  - create a list of length 26(+3?); increment the element at index  $n-1$  if the  $n$ -th letter is encountered
  - create a dictionary with letters as keys and integers as values; increment using index access
- all these implementations work (differently)
- big differences in *runtime* and *ease of implementation*
- choice of data structure is a *design decision*

# Counting with Dictionaries

- fast and counts all characters – no need to fix before!

```
def histogram(word):
```

```
    d = {}
```

```
    for char in word:
```

```
        if char not in d:
```

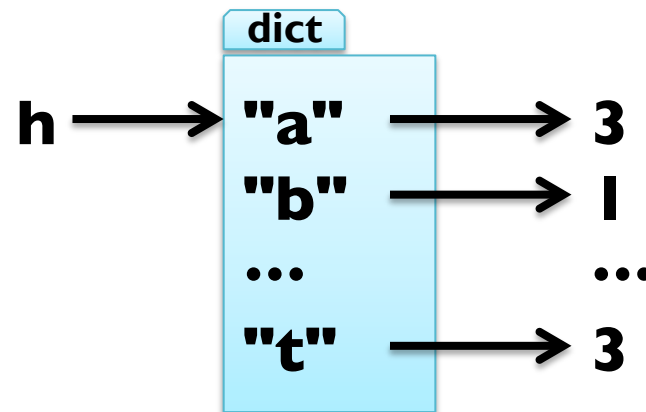
```
            d[char] = 1
```

```
        else:
```

```
            d[char] += 1
```

```
    return d
```

- Example: `h = histogram("slartibartfast")`  
`h == {"a":3, "b":1, "f":1, "i":1, "l":1, "s":2, "r":2, "t":3}`



# Counting with Dictionaries

- fast and counts all characters – no need to fix before!

```
def histogram(word):
```

```
    d = {}
```

```
    for char in word:
```

```
        if char not in d:
```

```
            d[char] = 1
```

```
        else:
```

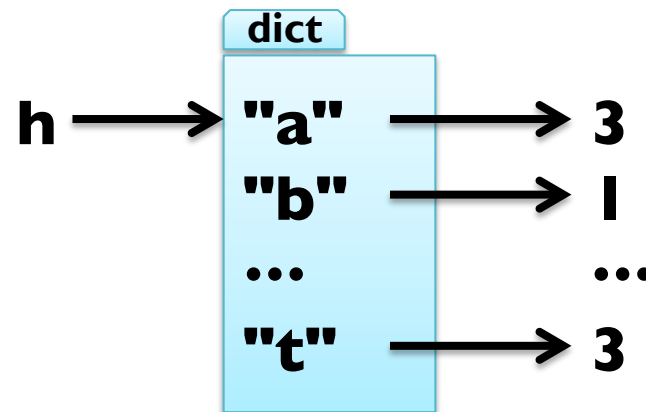
```
            d[char] += 1
```

```
    return d
```

- access using the `get(k, d)` method:

```
h.get("t", 0) == 3
```

```
h.get("z", 0) == 0
```



# Traversing Dictionaries

- using a `for` loop, you can traverse all keys of a dictionary

- Example: 

```
for key in en2da:  
    print key, en2da[key]
```

- you can also traverse all values of a dictionary

- Example: 

```
for value in en2da.values():  
    print value
```

- finally, you can traverse all items of a dictionary

- Example: 

```
for item in en2da.items():  
    print item[0], item[1]    # key, value
```

# Reverse Lookup

- given dict. `d` and key `k`, finding value `v` with `v == d[k]` easy
- this is called a dictionary *lookup*
- given dict. `d` and value `v`, finding key `k` with `v == d[k]` hard
- there might be more than one key mapping to `v` (cf. example)
- Possible implementation I:

```
def reverse_lookup(d, v):  
    result = []  
    for key in d:  
        if d[key] == v:  
            result.append(key)  
    return result
```

- returns empty list, when no key maps to value `v`

# Reverse Lookup

- given dict.  $d$  and key  $k$ , finding value  $v$  with  $v == d[k]$  easy
- this is called a dictionary *lookup*
- given dict.  $d$  and value  $v$ , finding key  $k$  with  $v == d[k]$  hard
- there might be more than one key mapping to  $v$  (cf. example)
- Possible implementation 2:

```
def reverse_lookup(d, v):
```

```
    for k in d:
```

```
        if d[k] == v:
```

```
            return k
```

```
    raise ValueError
```

- gives error when no key maps to value  $v$

# Reverse Lookup

- given dict.  $d$  and key  $k$ , finding value  $v$  with  $v == d[k]$  easy
- this is called a dictionary *lookup*
- given dict.  $d$  and value  $v$ , finding key  $k$  with  $v == d[k]$  hard
- there might be more than one key mapping to  $v$  (cf. example)
- Possible implementation 2:

```
def reverse_lookup(d, v):  
    for k in d:  
        if d[k] == v:  
            return k  
    raise ValueError, "value not found in dictionary"
```

- gives error when no key maps to value  $v$

# Dictionaries and Lists

- lists cannot be keys, as they are mutable
- list can be values stored in dictionaries
- Example: inverting a dictionary

```
def invert_dict(d):
```

```
    inv = {}
```

```
    for key in d:
```

```
        val = d[key]
```

```
        if val not in inv:
```

```
            inv[val] = [key]
```

```
        else:
```

```
            inv[val].append(key)
```

```
    return inv
```



# Dictionaries and Lists

- lists cannot be keys, as they are mutable
- list can be values
- Example: inverting a dictionary

```
def invert_dict(d):
```

```
    inv = {}
```

```
    for key in d:
```

```
        val = d[key]
```

```
        if val not in inv:
```

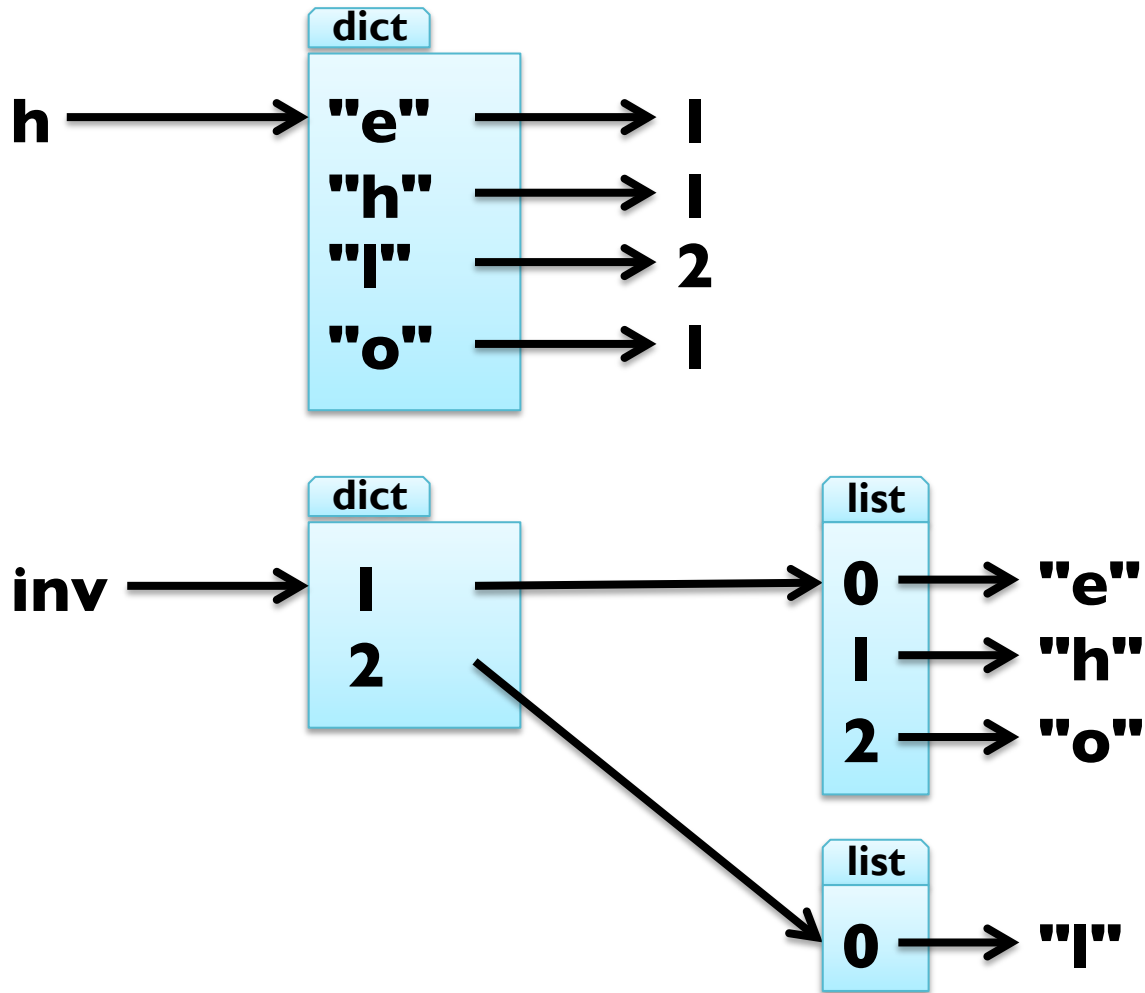
```
            inv[val] = []
```

```
            inv[val].append(key)
```

```
    return inv
```

- Example: `print invert_dict(histogram("hello"))`

# Dictionarys and Lists



- Example: `print invert_dict(histogram("hello"))`